

# Neutrino Interaction Physics

Lecture 1: Introduction of neutrino interactions

1. Overview
2. Neutrino lepton scattering
3. Neutrino quark scattering (DIS)
4. Neutrino nucleus reactions

Lecture 2: Neutrino interactions for long baseline oscillation experiments

1. Overview
2. CCQE interaction
3. Baryonic resonances
4. Shallow inelastic scattering (SIS)

Teppei Katori  
King's College London  
Oct. 10, 2023

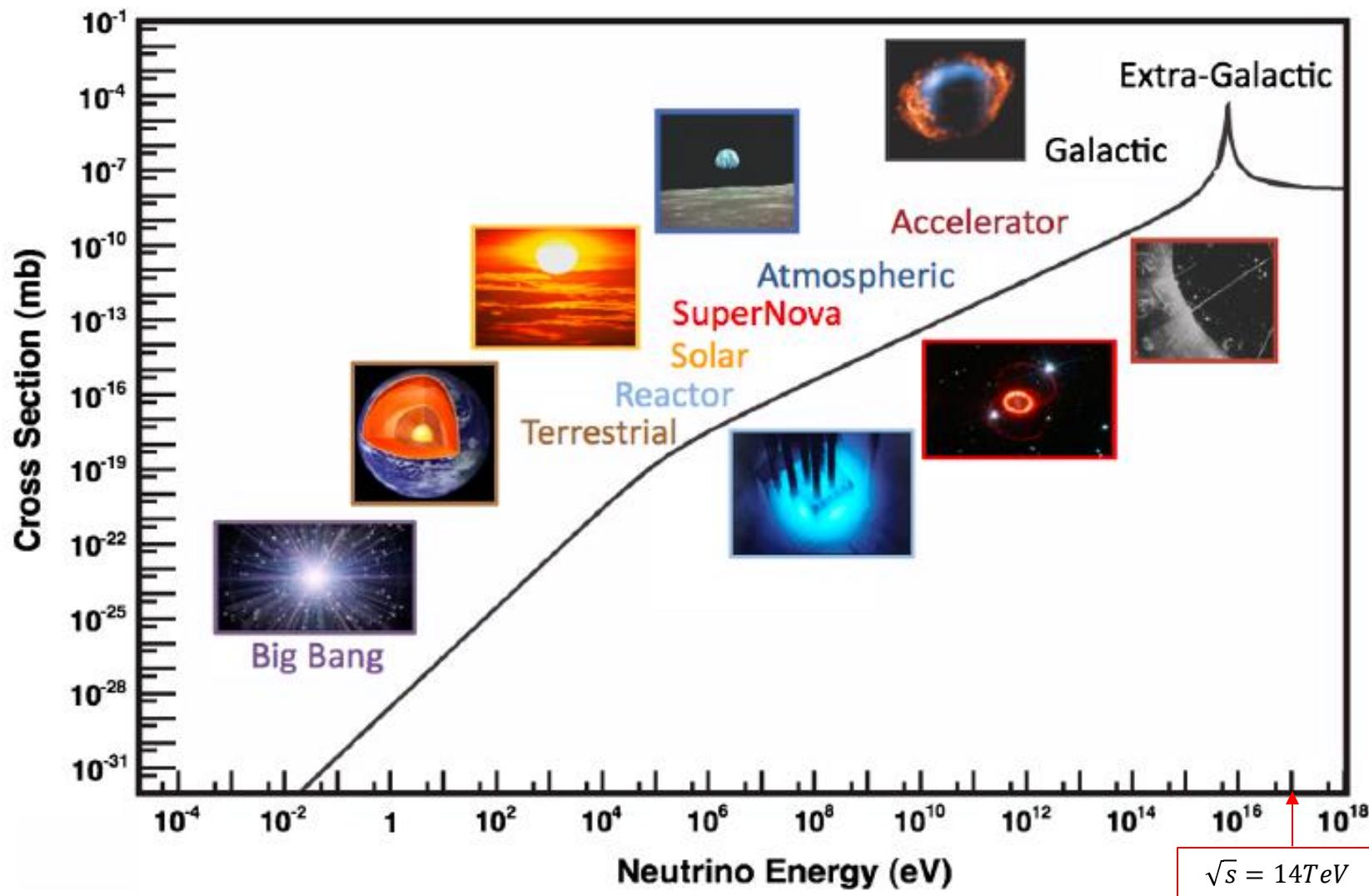
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# 1. From eV to EeV: Neutrino cross sections across energy scales



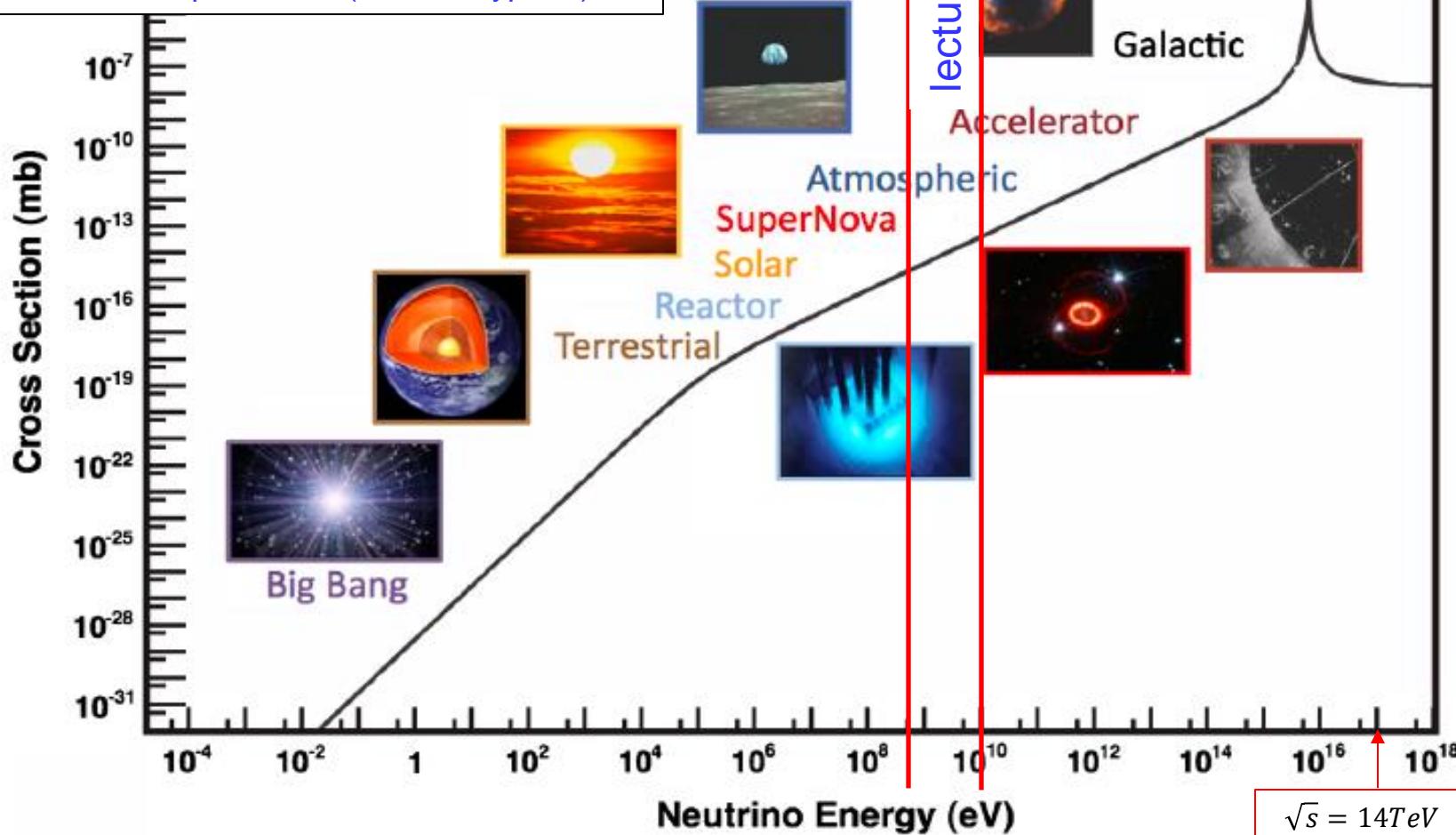
# 1. From eV to EeV: Neutrino cross sections across energy scales

lecture 1: Everything not relevant with long-baseline neutrino oscillation experiments  
 lecture 2: nuxsec for long-baseline neutrino oscillation experiments (DUNE, HyperK)

lecture 1

lecture 1

lecture 2

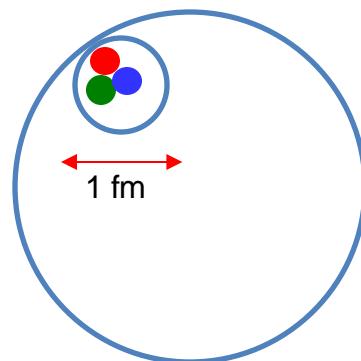
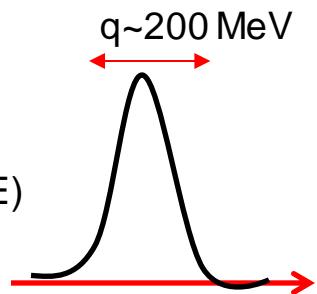


# 1. Scattering measurements

Size of wave packet ~ momentum transfer (~energy)

$\hbar c = 197 \text{ MeV} \cdot \text{fm} \rightarrow 200 \text{ MeV} \sim 1 \text{ fm}$  (size of nucleon)

~1 GeV neutrino beam  
(T2K, NOvA, HyperK, DUNE)

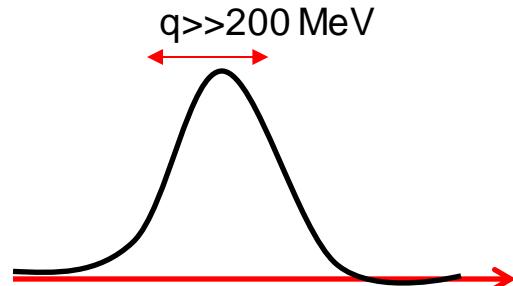


# 1. Scattering measurements

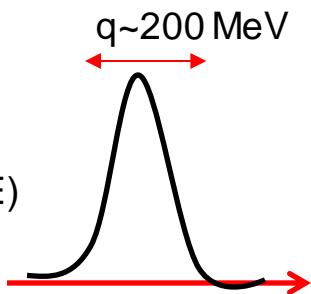
Size of wave packet  $\sim$  momentum transfer ( $\sim$ energy)

$$\hbar c = 197 \text{ MeV} \cdot \text{fm} \rightarrow 200 \text{ MeV} \sim 1 \text{ fm} \text{ (size of nucleon)}$$

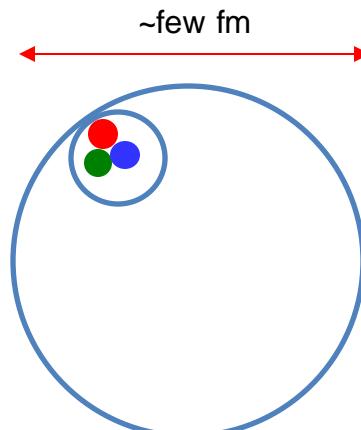
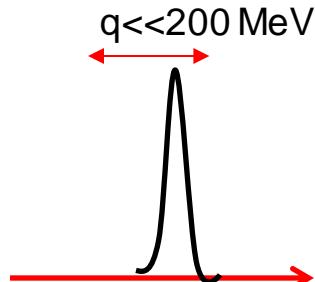
$\ll 1 \text{ GeV}$  neutrino beam  
(solar neutrinos, etc)



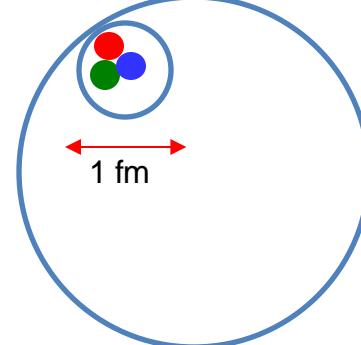
$\sim 1 \text{ GeV}$  neutrino beam  
(T2K, NOvA, HyperK, DUNE)



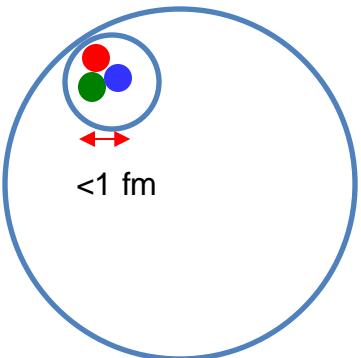
$\gg 1 \text{ GeV}$  neutrino beam  
(IceCube, FASERnu)



$\nu\text{-A}$



$\nu\text{-N}$



$\nu\text{-q}$

# 1. Scattering measurements

Size of wave packet ~ momentum transfer (~energy)

$\hbar c = 197 \text{ MeV} \cdot \text{fm} \rightarrow 200 \text{ MeV} \sim 1 \text{ fm}$  (size of nucleon)

Lecture 1: Introduction of neutrino interactions

1. Overview
2. Neutrino lepton scattering (Standard Model)
3. Neutrino quark scattering ( $\nu$ -q scattering)
4. Neutrino nucleus reactions ( $\nu$ -A scattering)

Lecture 2: Neutrino interactions for long baseline oscillation experiments ( $\nu$ -N scattering)

1. Overview
2. CCQE interaction
3. Baryonic resonances
4. Shallow inelastic scattering

## 2. Neutrino-electron scattering

Neutrino – electron differential cross section

$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[ c_L^2 + c_R^2 \left( \frac{E - T}{E} \right)^2 - C_L C_R \frac{m_e T}{E^2} \right]$$

T=recoil electron kinetic energy

E=neutrino energy

	$C_L$	$C_R$
$\nu_e - e^-$	$\frac{1}{2} + \sin^2 \theta_w$	$\sin^2 \theta_w$
$\bar{\nu}_e - e^-$	$\sin^2 \theta_w$	$\frac{1}{2} + \sin^2 \theta_w$
$\nu_\mu - e^-$	$-\frac{1}{2} + \sin^2 \theta_w$	$\sin^2 \theta_w$
$\bar{\nu}_\mu - e^-$	$\sin^2 \theta_w$	$-\frac{1}{2} + \sin^2 \theta_w$

## 2. MINERvA neutrino flux tuning

Neutrino – electron differential cross section

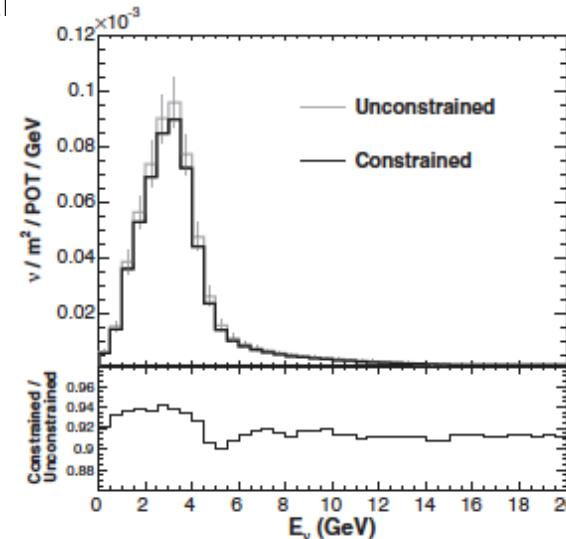
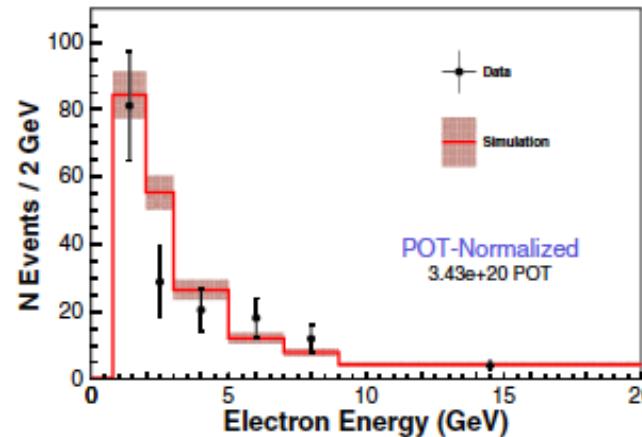
$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[ c_L^2 + c_R^2 \left( \frac{E - T}{E} \right)^2 - C_L C_R \frac{m_e T}{E^2} \right]$$

T=recoil electron kinetic energy

E=neutrino energy

$$\#events = \left( \int \text{flux} \otimes \text{cross section} \otimes \text{efficiency} \right) \times \text{target number} \times \text{exposure}$$

By assuming detector efficiency and cross-section are known, you can measure neutrino flux



## 2. Neutrino magnetic moment

# Neutrino – electron differential cross section

$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[ c_L^2 + c_R^2 \left( \frac{E - T}{E} \right)^2 - C_L C_R \frac{m_e T}{E^2} \right]$$

T=recoil electron kinetic energy

E=neutrino energy

Neutrino – electron differential cross section with neutrino magnetic moment

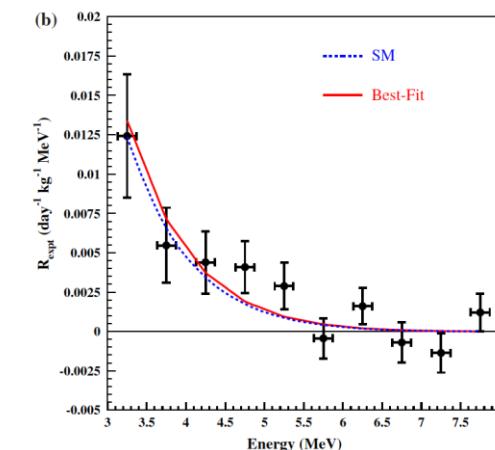
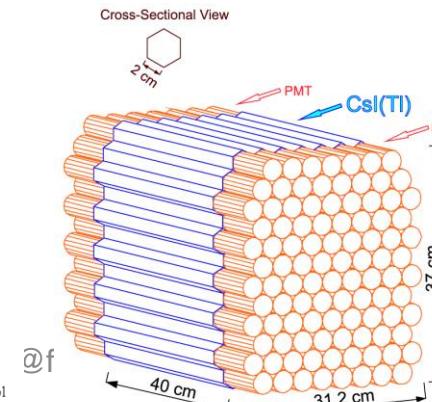
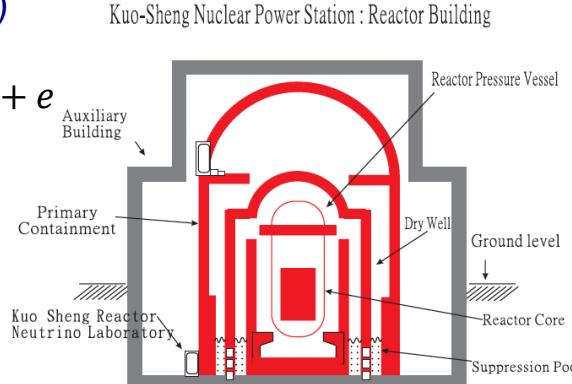
$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[ c_L^2 + c_R^2 \left( \frac{E-T}{E} \right)^2 - C_L C_R \frac{m_e T}{E^2} \right] + \frac{\pi \alpha \mu_\nu^2}{m_e^2} \left( \frac{1}{T} - \frac{1}{E} \right)$$

SM large neutrino magnetic moment (BSM)

Lepton-only process (pure Standard Model) is often used to test new physics

TEXONO (Taiwan)

- reactor neutrino
  - ES:  $\bar{\nu}_e + e \rightarrow \bar{\nu}_e + e$
  - CsI (Tl) crystal array (187kg)



### 3. Neutrino-DIS cross section

Neutrino – single d-quark cross section

$$\frac{d\sigma}{dy} (\nu d \rightarrow \mu u) = \frac{G_F^2 \chi s}{\pi}$$

Neutrino – d-quark cross section

$$\frac{d\sigma}{dy} (\nu d \rightarrow \mu u) = \int_0^1 \frac{G_F^2 \chi s}{\pi} d(x) dx$$

Neutrino-nucleon DIS cross section

$$\frac{d\sigma}{dy} (\nu N \rightarrow \mu X) = \int_0^1 \frac{G_F^2 \chi s}{\pi} [(d(x) + s(x) \dots) + [\bar{u}(x) + \bar{c}(x) \dots] (1-y)^2] dx$$

Neutrino-nucleus DIS cross section with **isoscalar** assumption

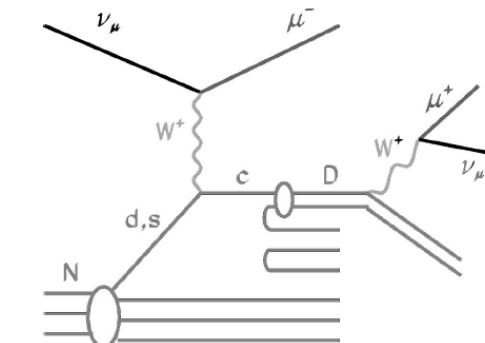
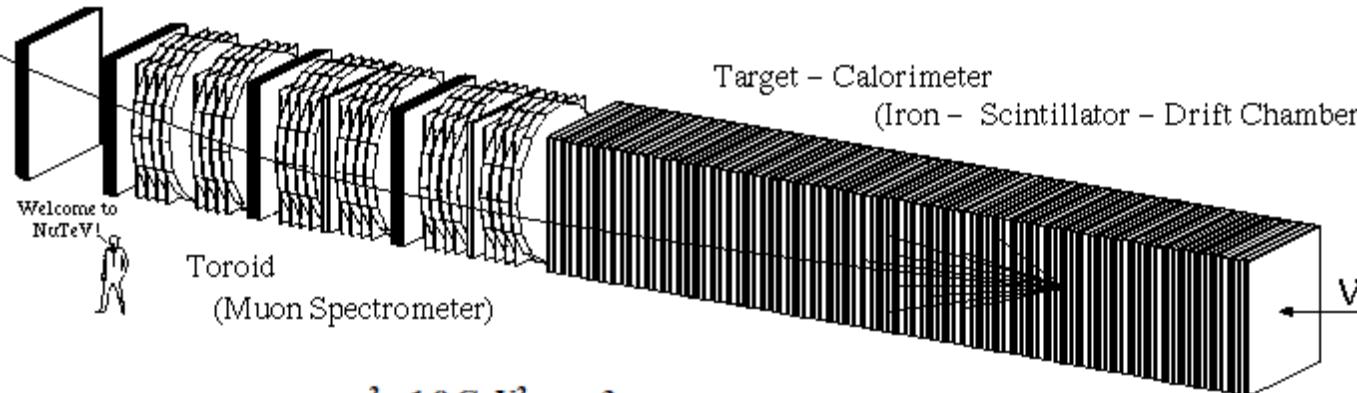
$$\frac{d\sigma}{dy} (\nu A \rightarrow \mu X) = A \int_0^1 \frac{G_F^2 \chi s}{\pi} [Q(x) + \bar{Q}(x)(1-y)^2] dx$$

$$u^p(x) + u^n(x) = d^n(x) + d^p(x) = u(x) + d(x) \equiv Q(x)$$

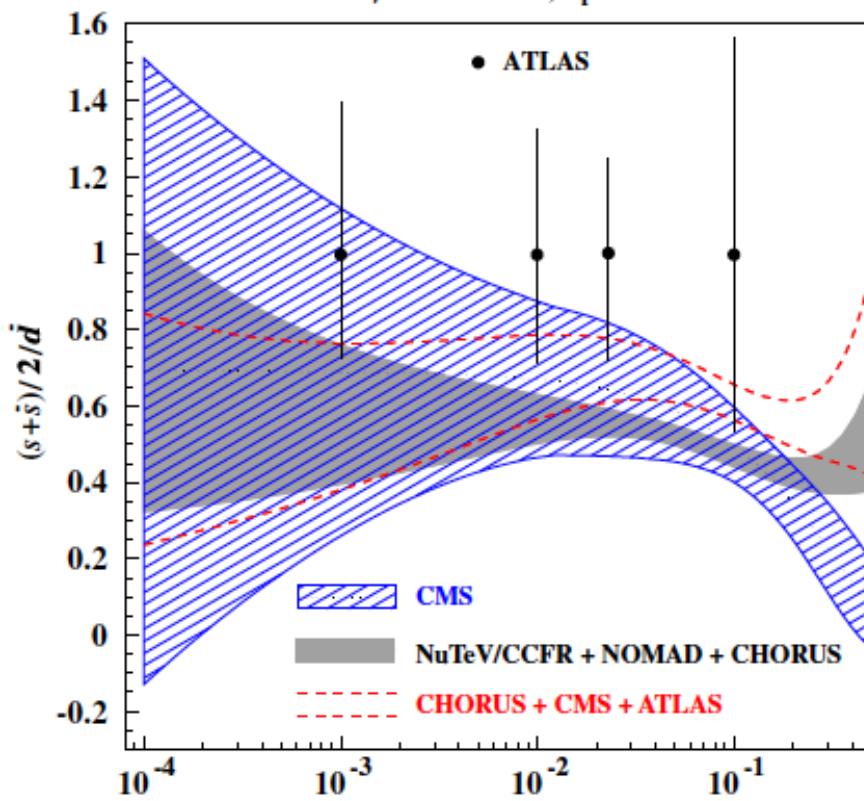
$$\bar{u}^p(x) + \bar{u}^n(x) = \bar{u}^n(x) + \bar{u}^p(x) = \bar{u}(x) + \bar{d}(x) \equiv \bar{Q}(x)$$

### 3. Di-muon production

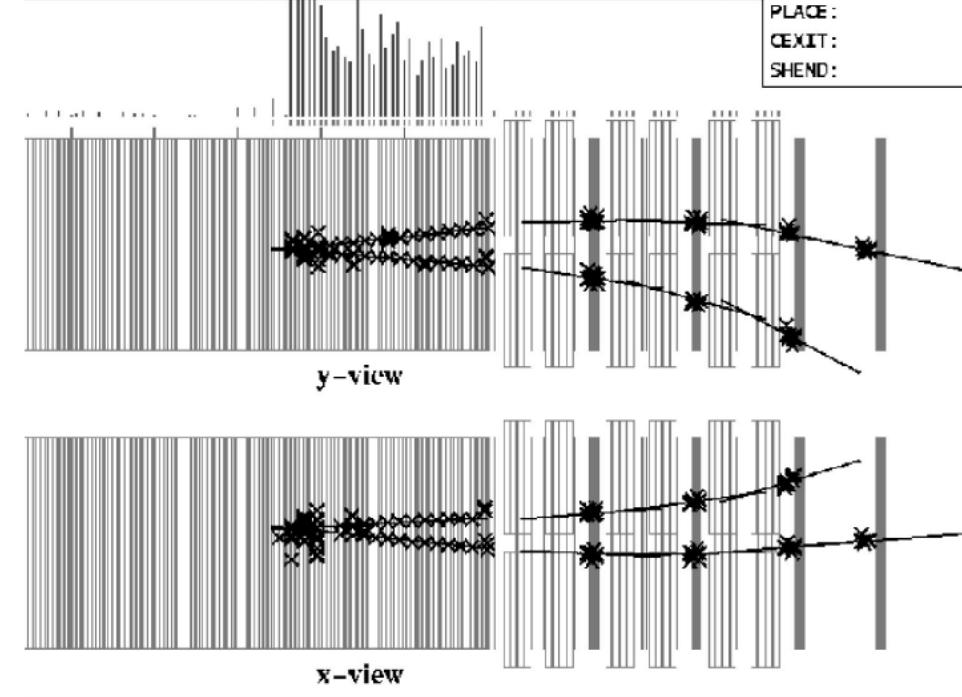
Blue Cart



$$\mu^2 = 1.9 \text{ GeV}^2, n_f = 3$$



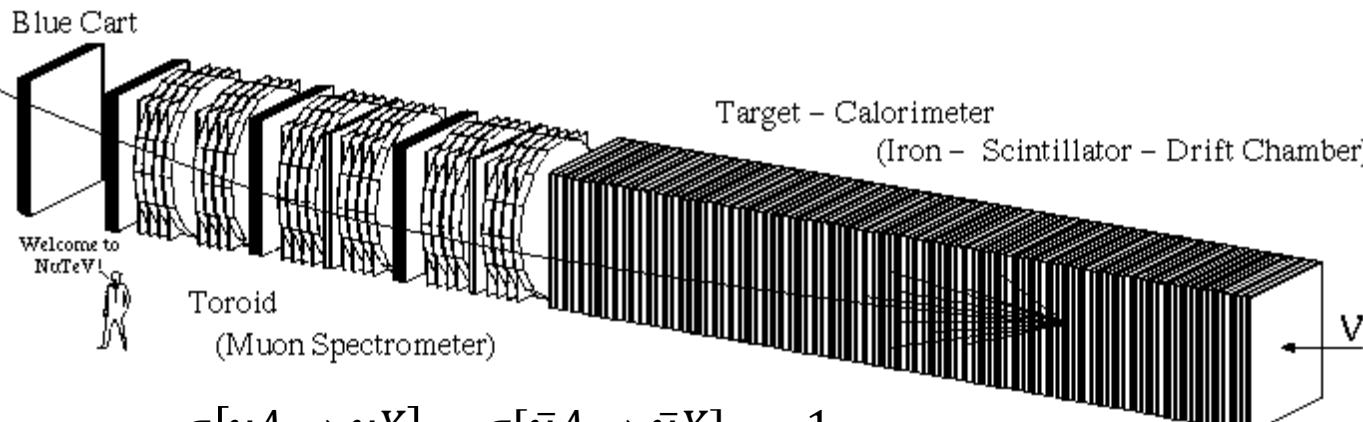
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 Vers: [1 2 3 4 5 6 7 8 9 10 11 12 13] EMU1: 33.13  
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 PLACE:  
 CEXIT:  
 SHEND:



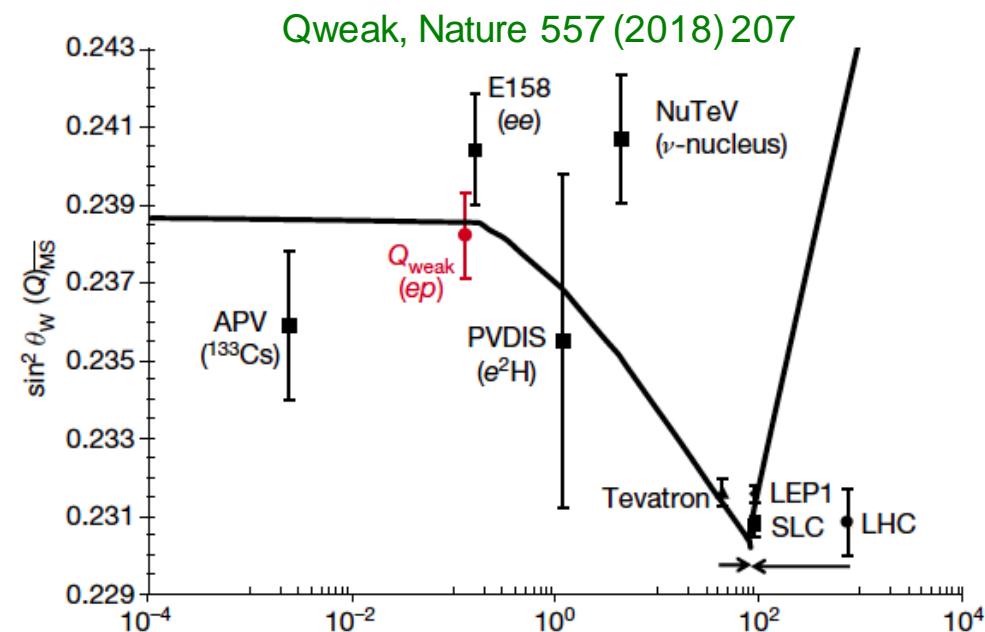
### 3. Paschos-Wolfenstein ratio and NuTeV anomaly



Manny Paschos  
(Dortmund)



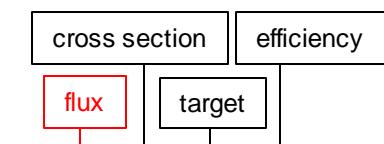
$$R_{PW} = \frac{\sigma[\nu A \rightarrow \nu X] - \sigma[\bar{\nu} A \rightarrow \bar{\nu} X]}{\sigma[\nu A \rightarrow \mu X] - \sigma[\bar{\nu} A \rightarrow \mu^+ X]} = \frac{1}{2} - \sin^2 \theta_W$$



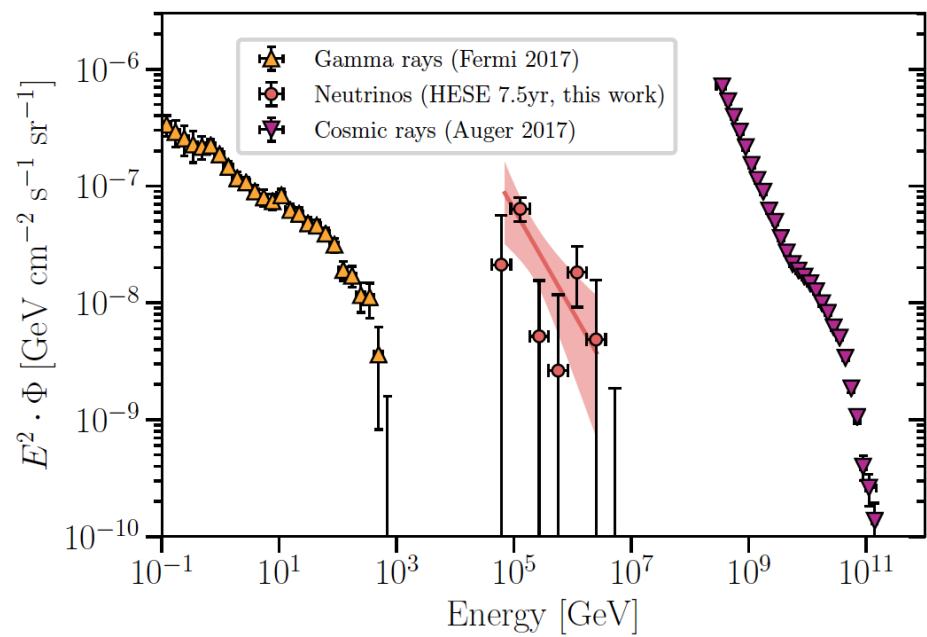
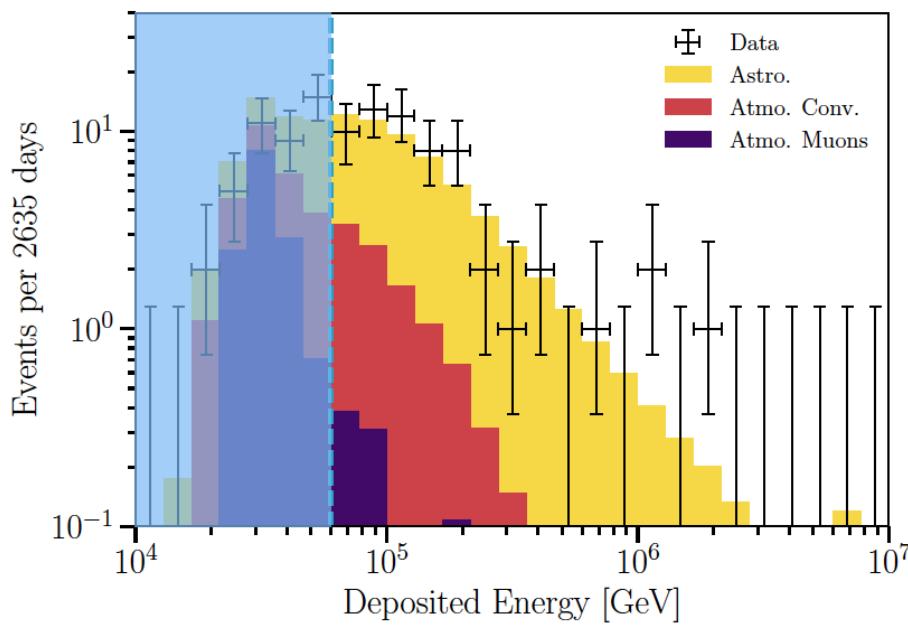
### 3. Astrophysical high-energy neutrino measurement

Data and MC agree up to  $\sim$ PeV.

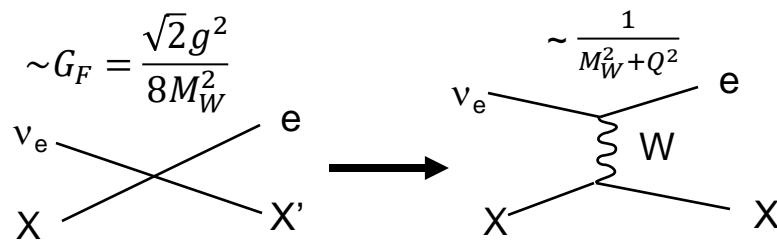
→ We more or less understand neutrino interactions up to  $\sim$ PeV.



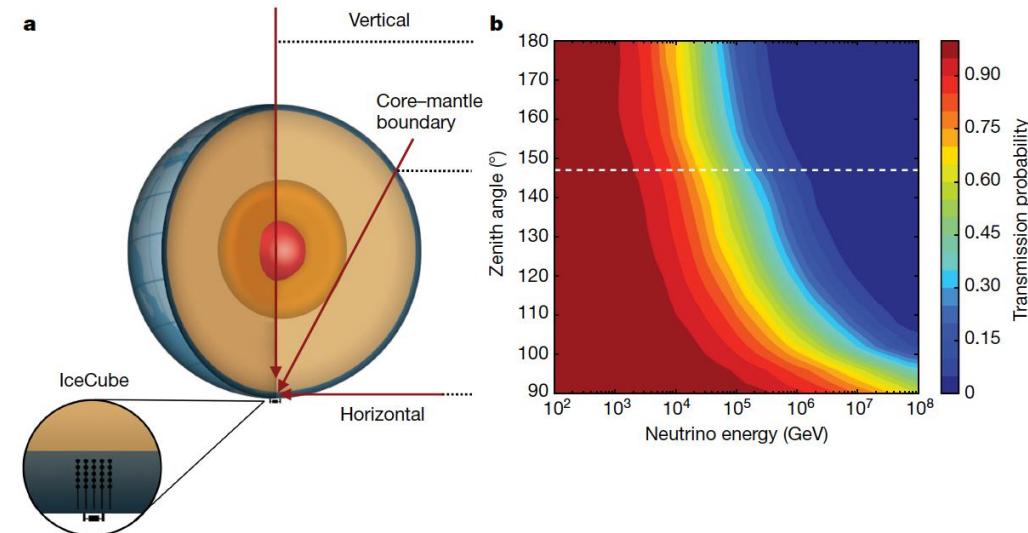
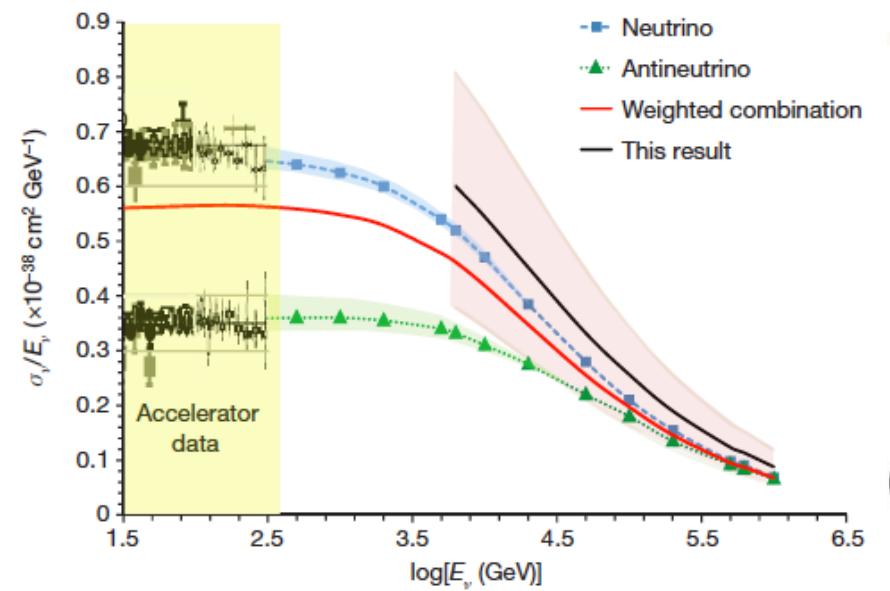
$$\text{Event rate } N = \Phi \times \sigma \times T \times \epsilon$$



### 3. Neutrino DIS saturation



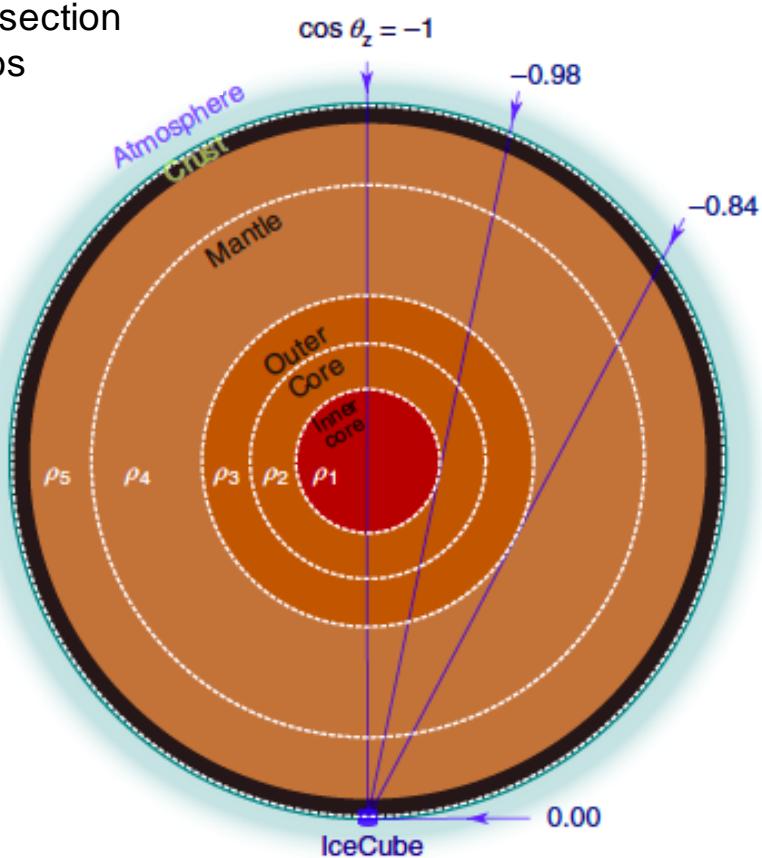
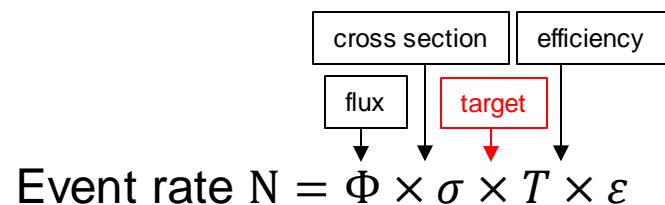
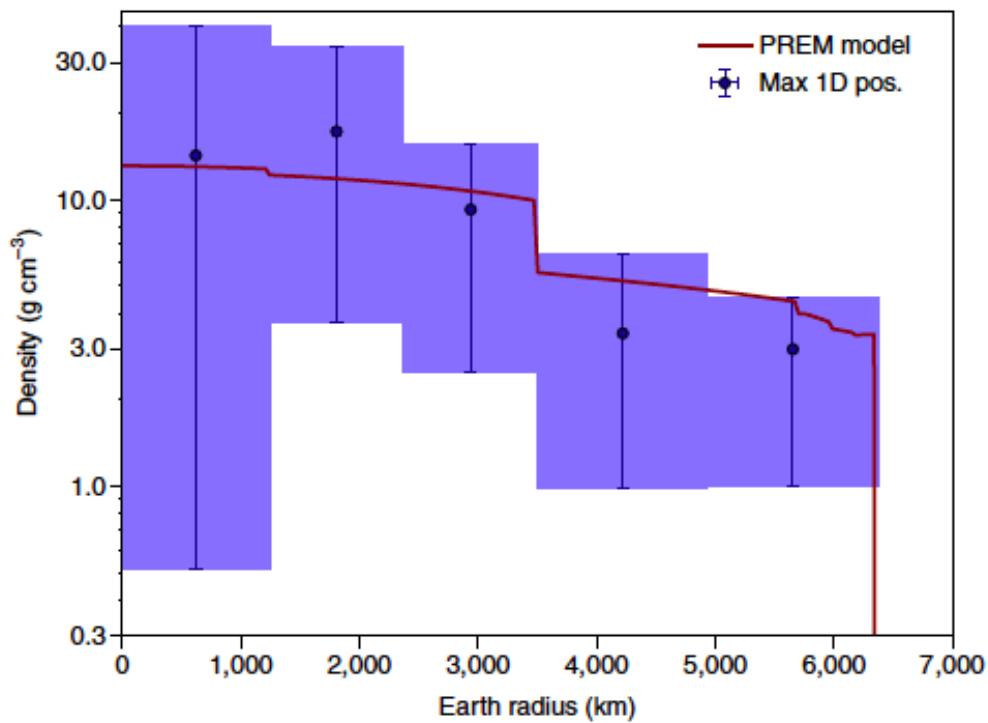
$$\text{Event rate } N = \Phi \times \sigma \times T \times \varepsilon$$



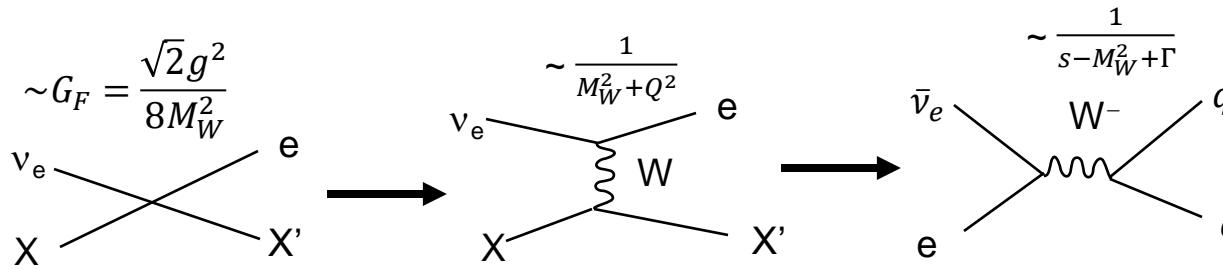
### 3. Earth tomography

#### Earth absorption for Earth density measurement

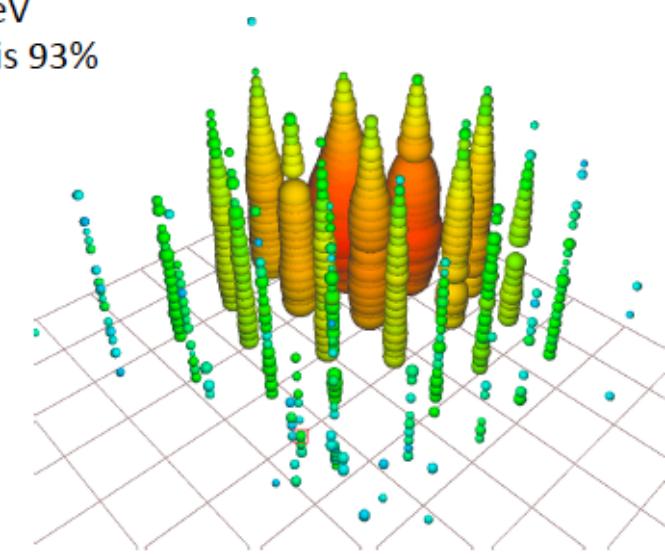
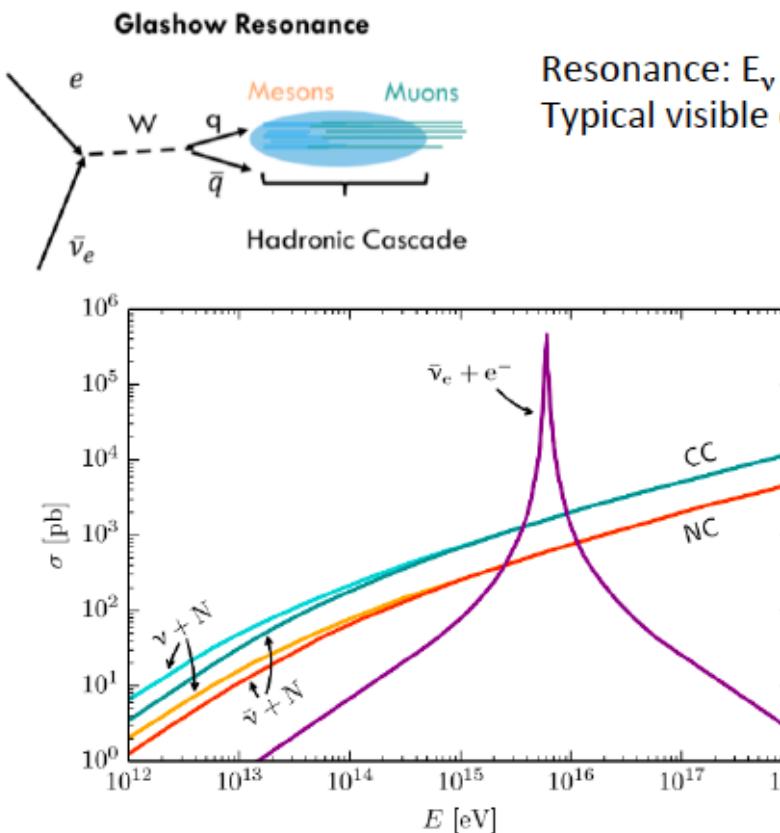
- PREM (Preliminary reference Earth model)
- Standard earth density model used by T2K, NOvA, etc
- Earth density profile is extracted by assuming flux and cross section
- Measure Earth moment of inertia and Earth mass by neutrinos



### 3. Glashow resonance



## A 5.9 PeV event in IceCube

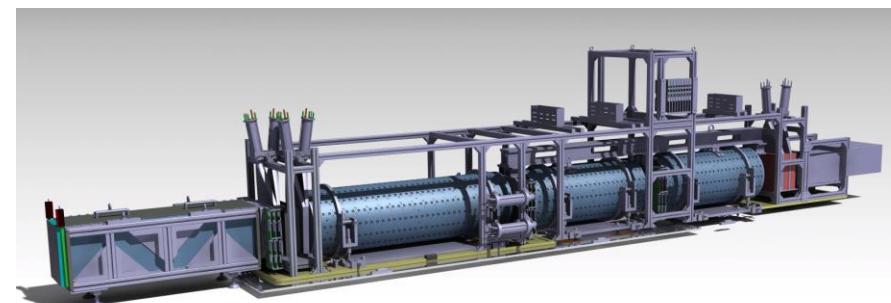
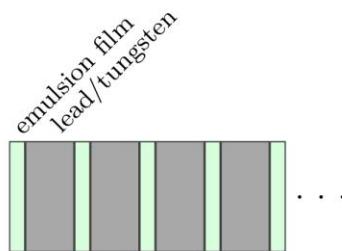
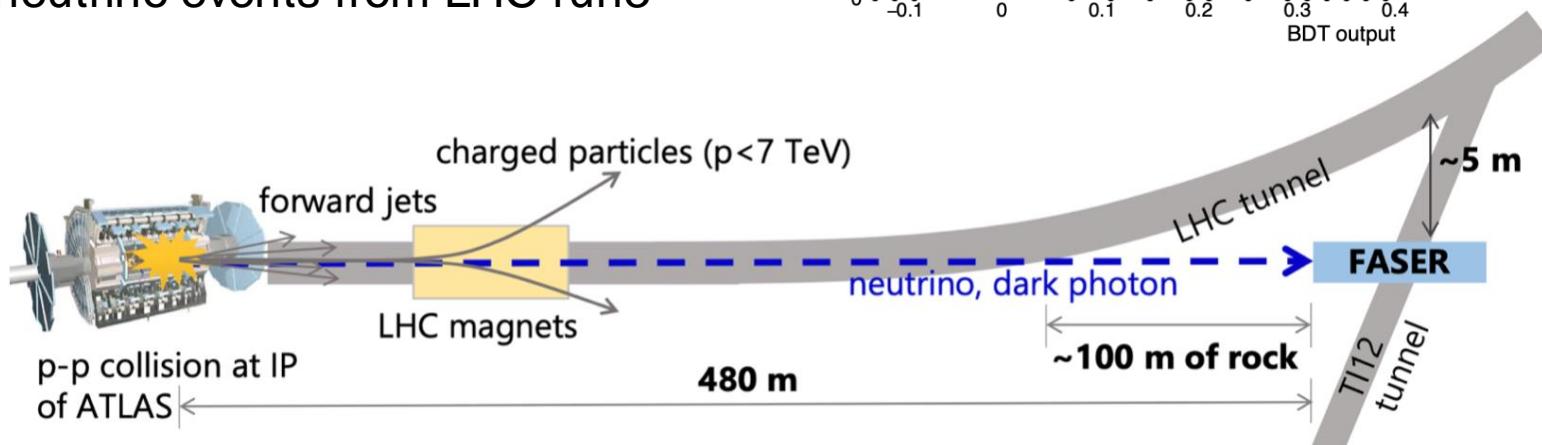
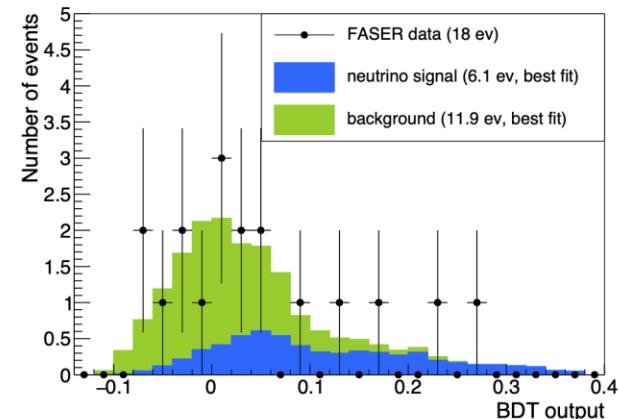


Event identified in a partially-contained PeV search (PEPE)  
Deposited energy:  $5.9 \pm 0.18$  PeV (stat only)  
ICRC 2017 arXiv:1710.01191

### 3. Collider neutrino

#### FASERnu

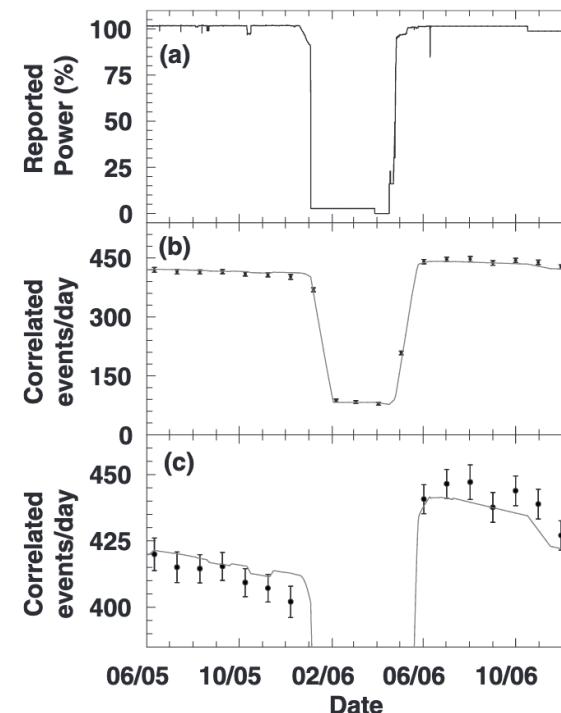
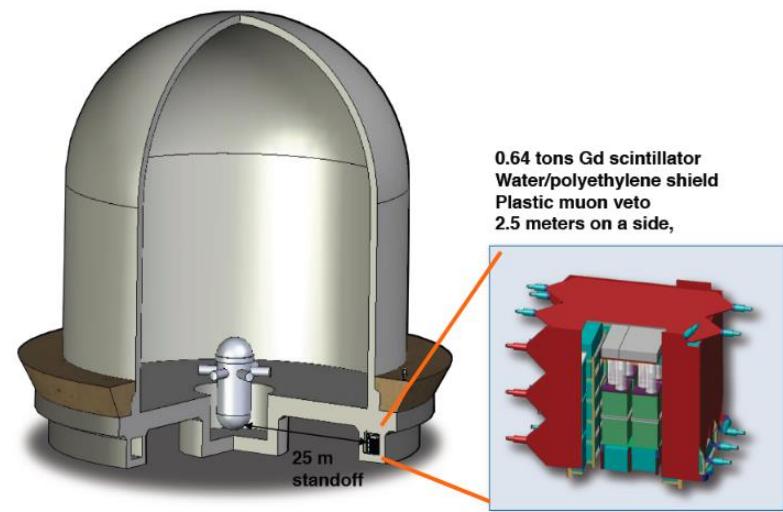
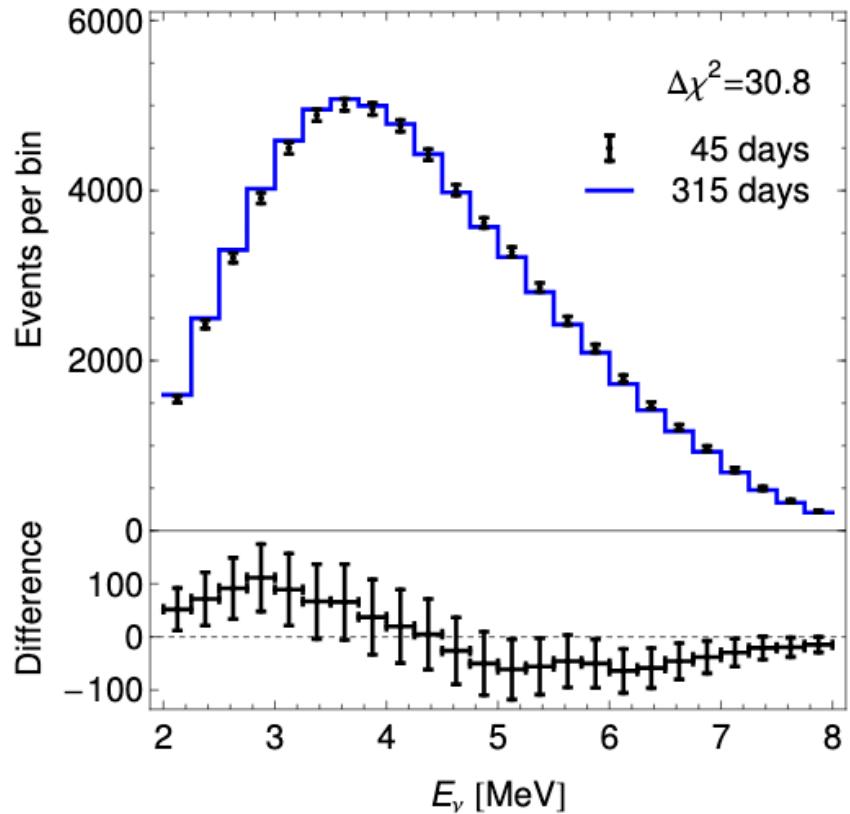
- Emulsion detector (high-resolution)
- neutrinos from ATLAS collision point
- neutrino excess from pilot run
- ~10,000 neutrino events from LHC run3



## 4. Reactor neutrino

### Low energy electron anti-neutrinos

- High-precision spectrum prediction
- Monitoring fission reactor



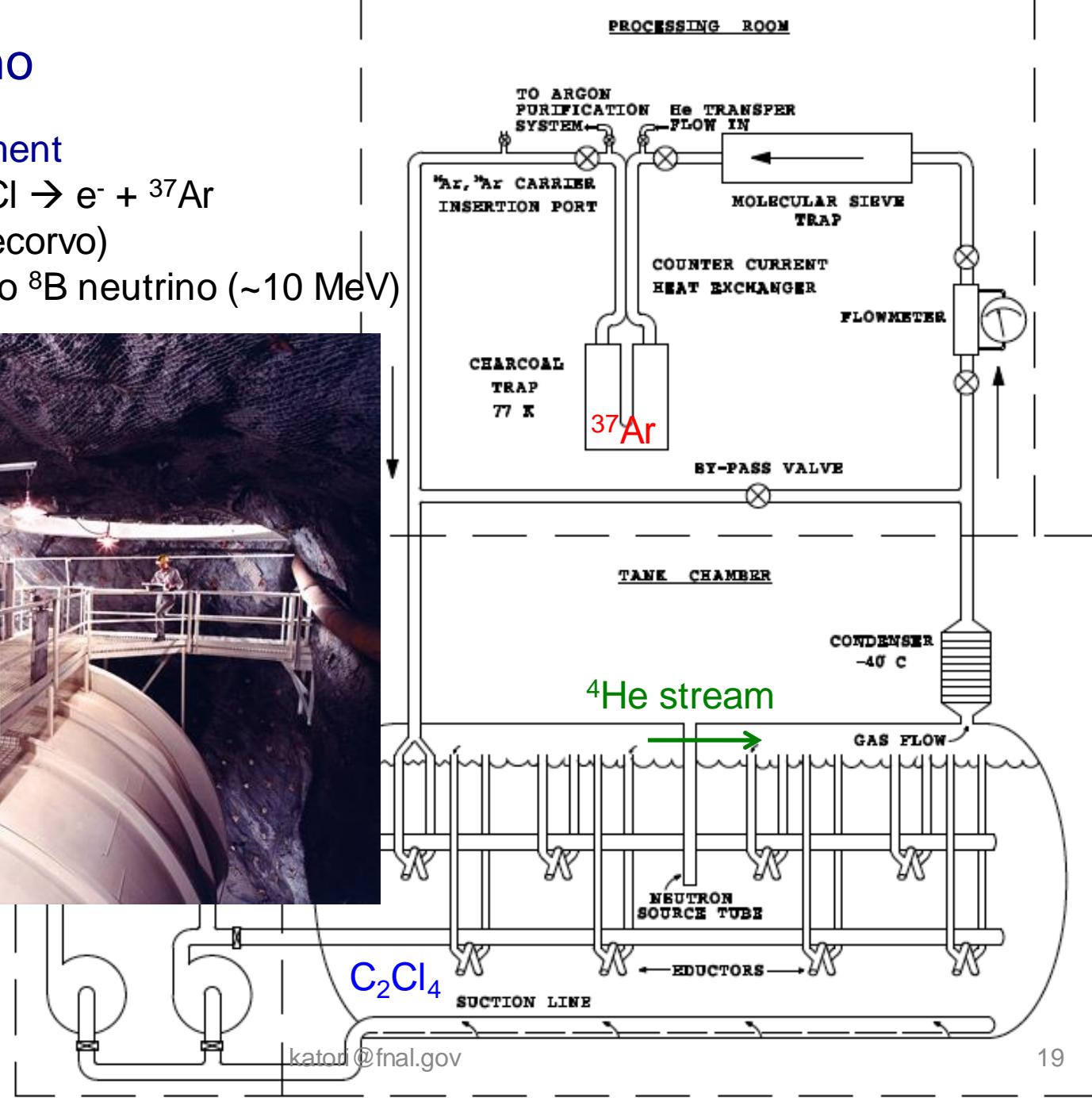
## 4. Solar neutrino

### Homestake experiment



(proposed by Pontecorvo)

- mainly sensitive to  ${}^8\text{B}$  neutrino ( $\sim 10$  MeV)

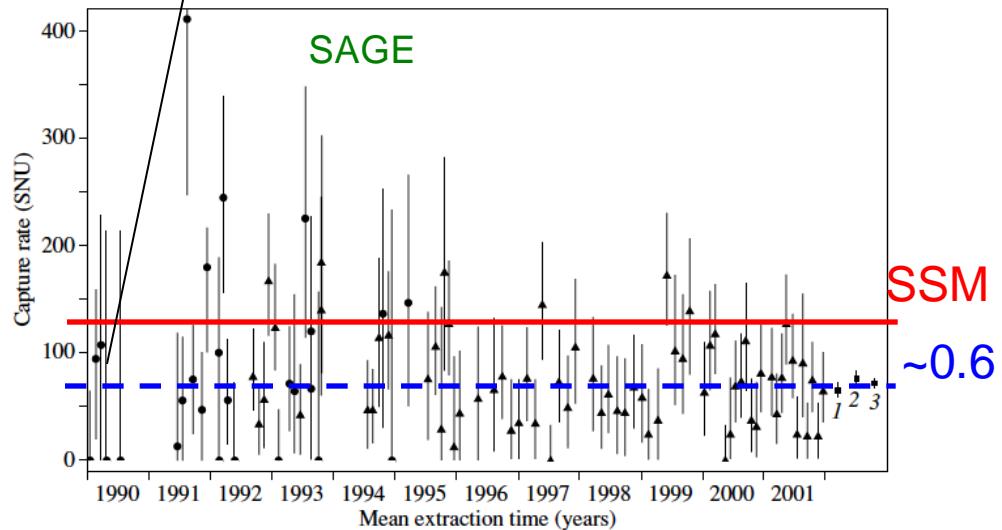
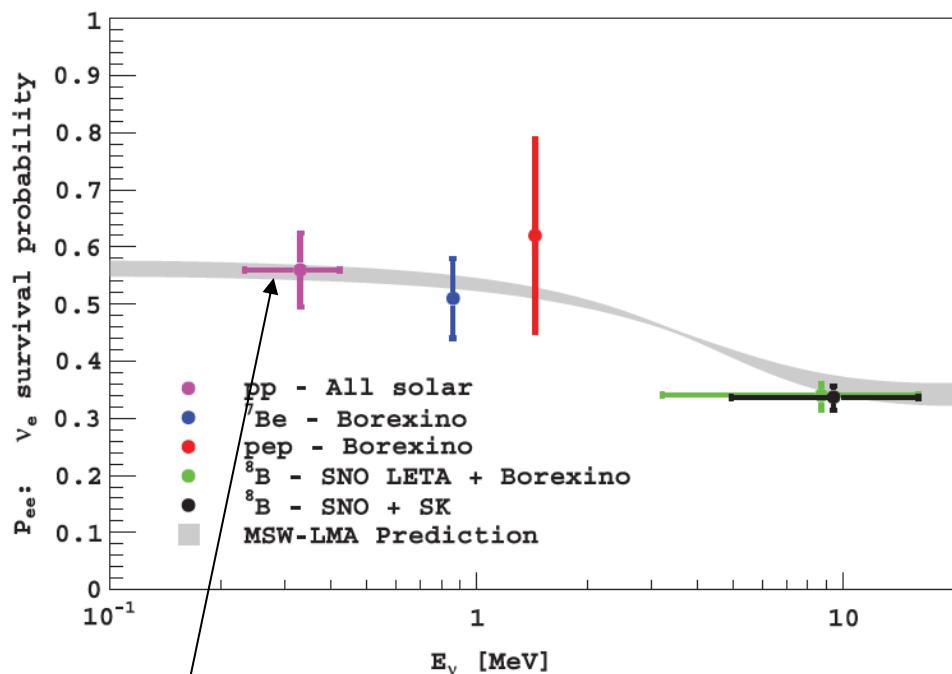
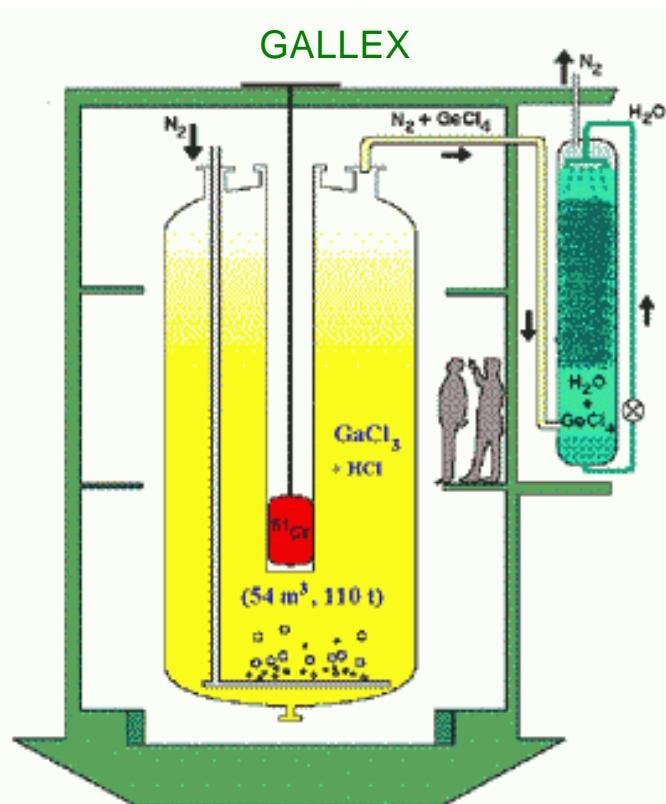


## 4. Solar neutrino

### Gallium experiment

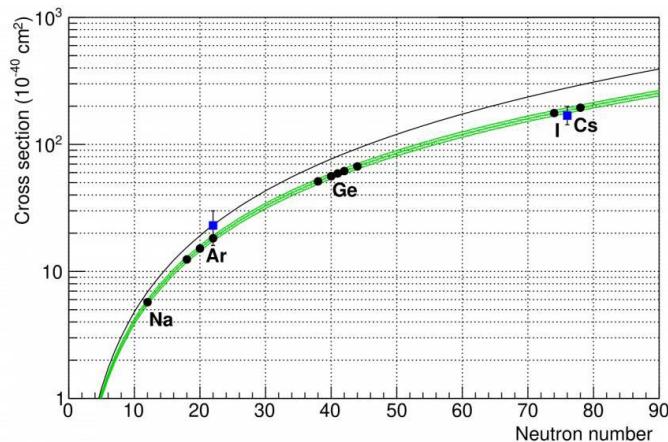


- Sensitive to pp-neutrino (0.42 MeV), 90% of total solar neutrino flux.
- Both experiments observed deficit, but higher than Homestake result



# 4. Neutrino-Nucleus coherent scattering

Low energy neutrinos from neutron sources at SNS (spallation neutron source), ORNL (Oak Ridge National Lab)

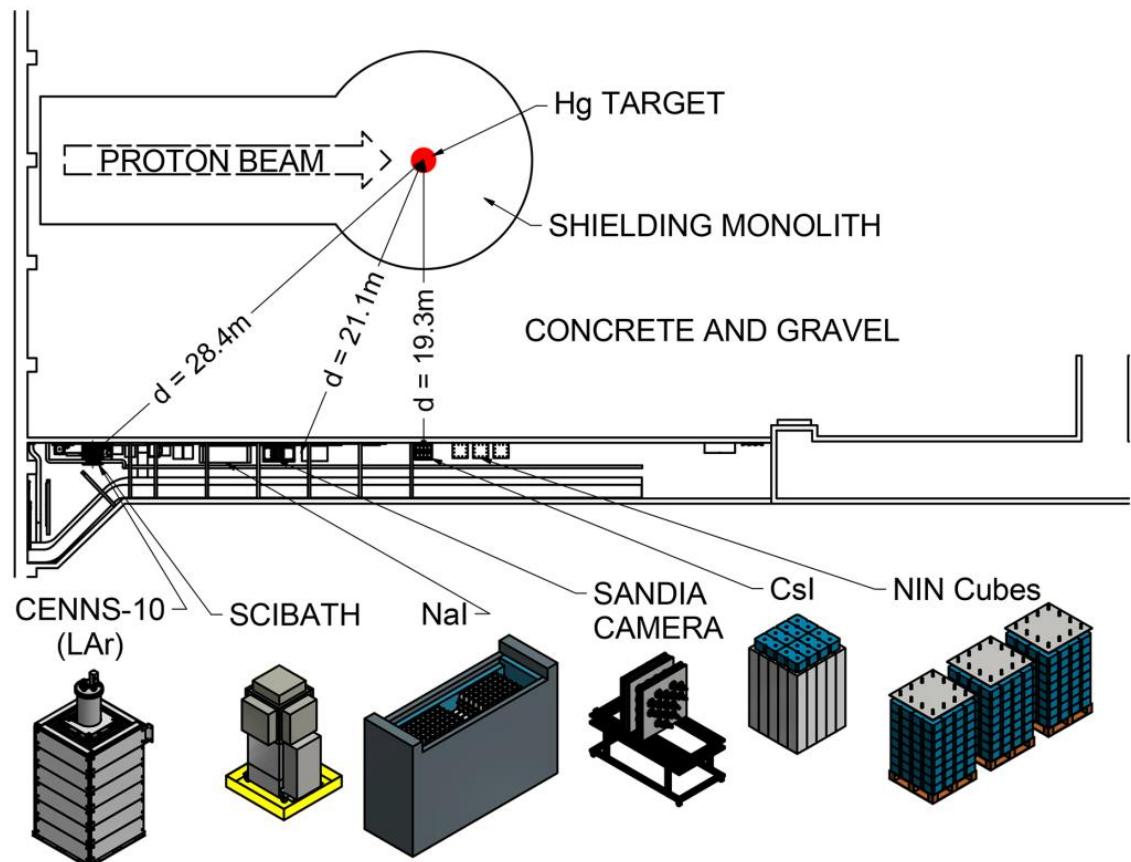


Science

REPORTS

Cite as: D. Akimov *et al.*, *Science*  
10.1126/science.aa0990 (2017).

## Observation of coherent elastic neutrino-nucleus scattering



# Conclusion

$\nu$ -l scattering : well-known, test of weak theory

- Neutrino-electron scattering for neutrino flux measurement

- Anti-electron neutrino scattering for neutrino magnetic moment search (BSM)

$\nu$ -q scattering : test of weak theory, test of quark model

- DIS cross sections

- Di-muon production

- Paschos-Wolfenstein ratio

- Astrophysical neutrinos

- collider neutrinos

$\nu$ -A scattering :

- Reactor neutrino experiments

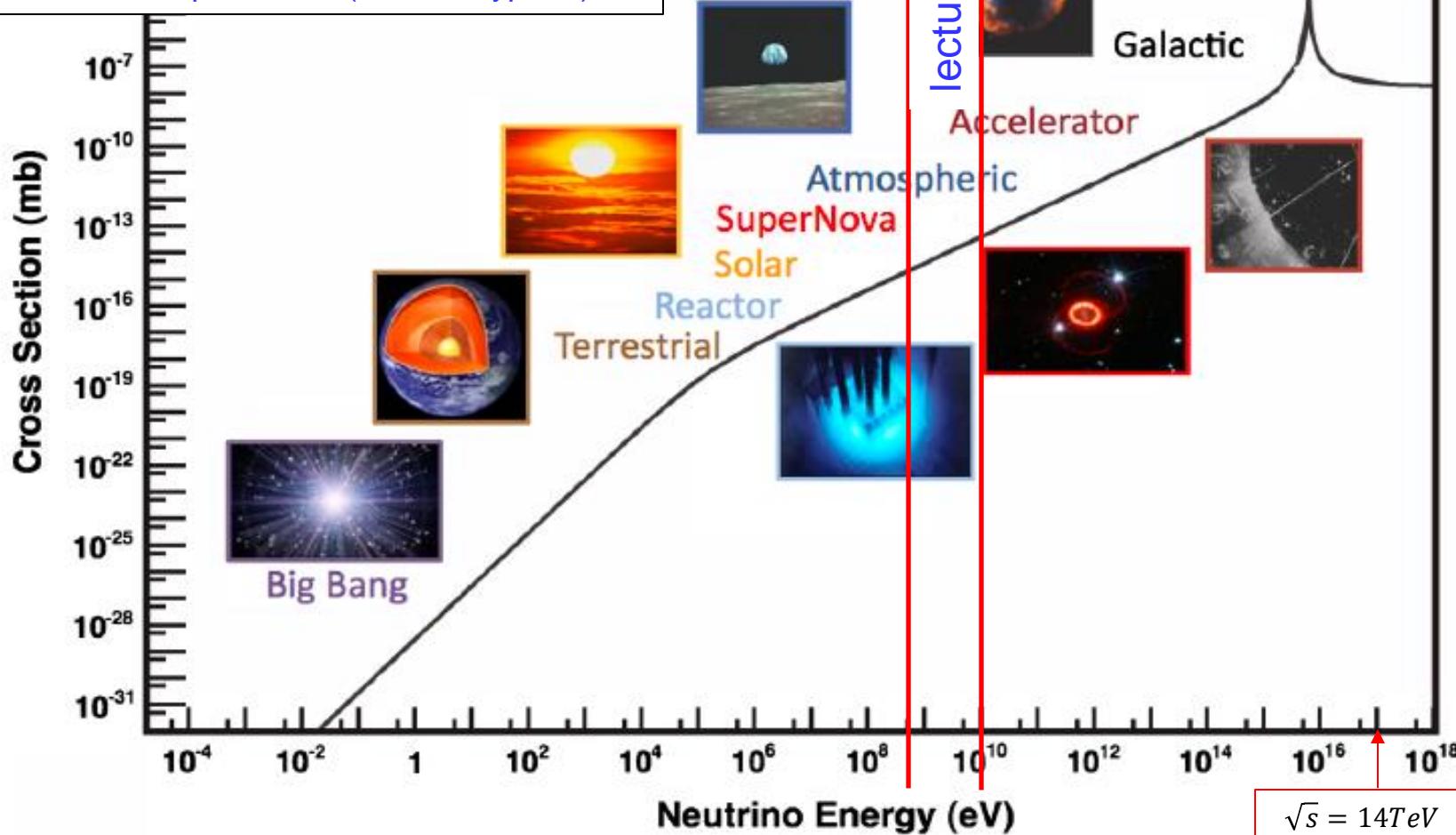
- Neutrino nuclear capture by Cl and Ga, important for solar neutrinos

- Neutrino coherent scattering, important for supernova (2017)

$\nu$ -N scattering : important reactions for long baseline neutrino oscillation experiment  
(T2K, NOvA, DUNE, Hyper-Kamiokande)

# 1. From eV to EeV: Neutrino cross sections across energy scales

lecture 1: Everything not relevant with long-baseline neutrino oscillation experiments  
 lecture 2: nuxsec for long-baseline neutrino oscillation experiments (DUNE, HyperK)



# 1. NuInt22 in Seoul (Oct. 24-29, 2022)

Neutrino interaction physics community

<https://nuint22.org/>



## NuINT 2022

The 13th International Workshop on Neutrino-Nucleus Interactions  
in the Few GeV Regions

October 24 to 29, 2022 (OFFLINE)

Hoam Faculty House  
Seoul National University  
Seoul, Korea

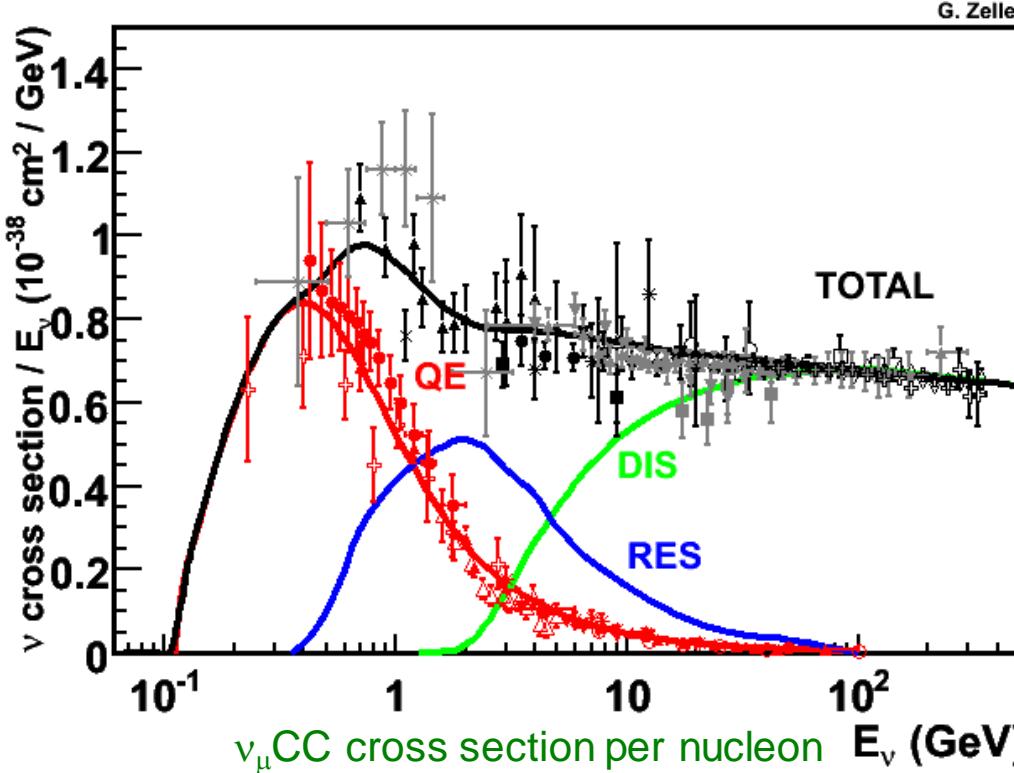
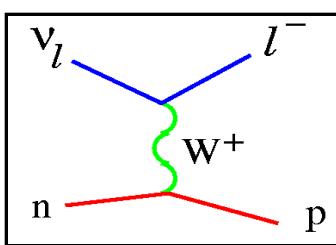


# 1. Next generation neutrino oscillation experiments

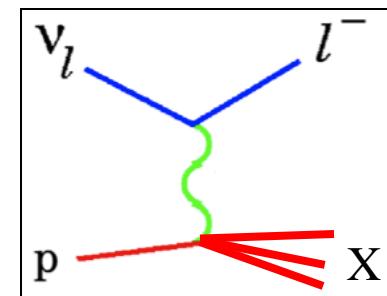
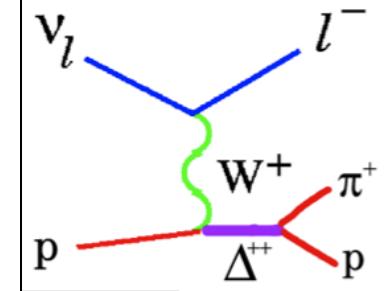
Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE

Quasi Elastic



baryonic  
RESonance

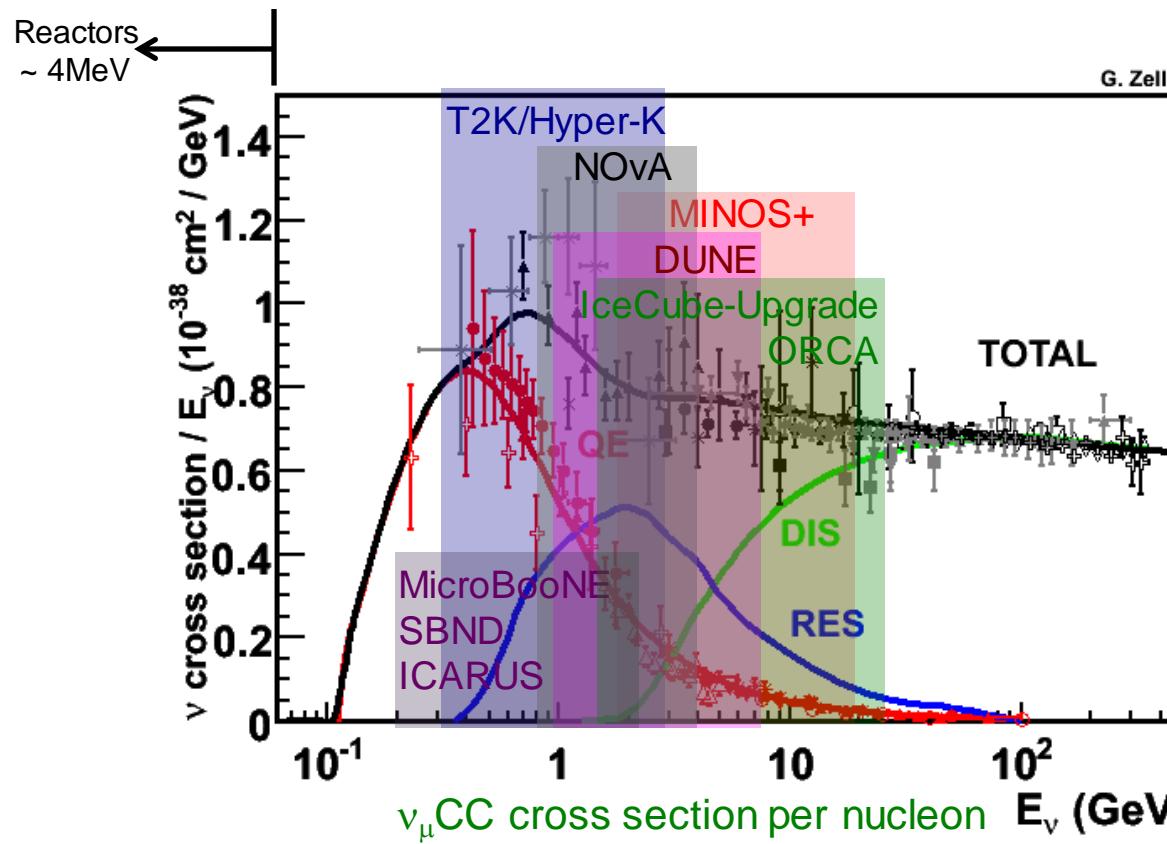


Deep  
Inelastic  
Scattering

# 1. Next generation neutrino oscillation experiments

## Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE...



$$P_{m \rightarrow e}(L / E) = \sin^2 2\theta \sin^2 \left( 1.27 D m^2 (eV^2) \frac{L(km)}{E(GeV)} \right)$$

# 1. Next generation neutrino oscillation experiments

## Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE...

### Most of data are from muon neutrino beam

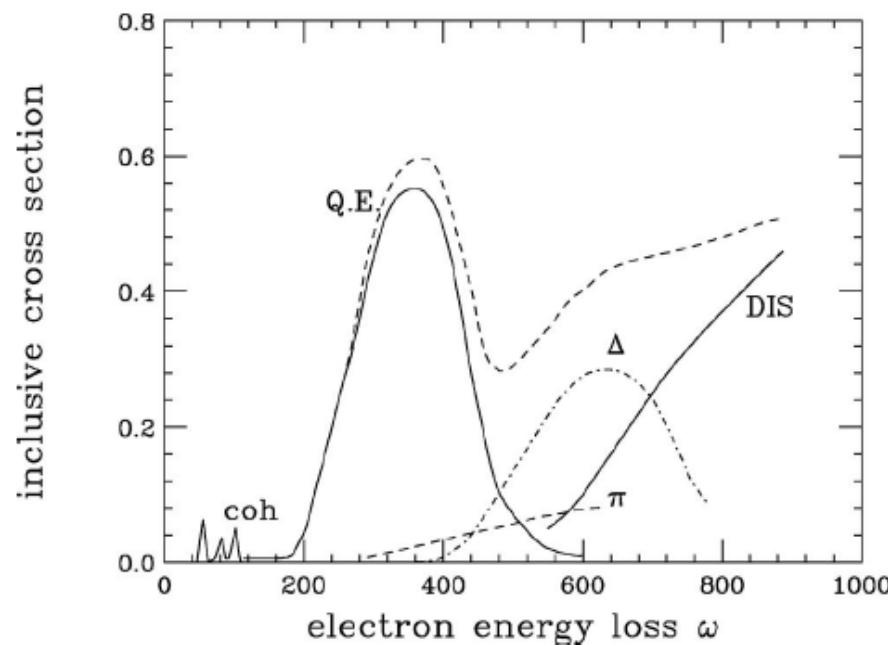
- create by  $\pi$ -DIF, K-DIF (pion and kaon decay-in-flight)
- $\Phi(\nu_\mu) > \Phi(\bar{\nu}_\mu)$ : more  $\pi^+$  and  $K^+$  than  $\pi^-$  and  $K^-$  (for low energy accelerators)
- $\mu$ -decay can make electro-neutrinos but they are background
- $\delta_{CP}$  study need electro-neutrino and antineutrino cross-sections ( $\nu_e$  appearance)

### Nuclear physics sucks

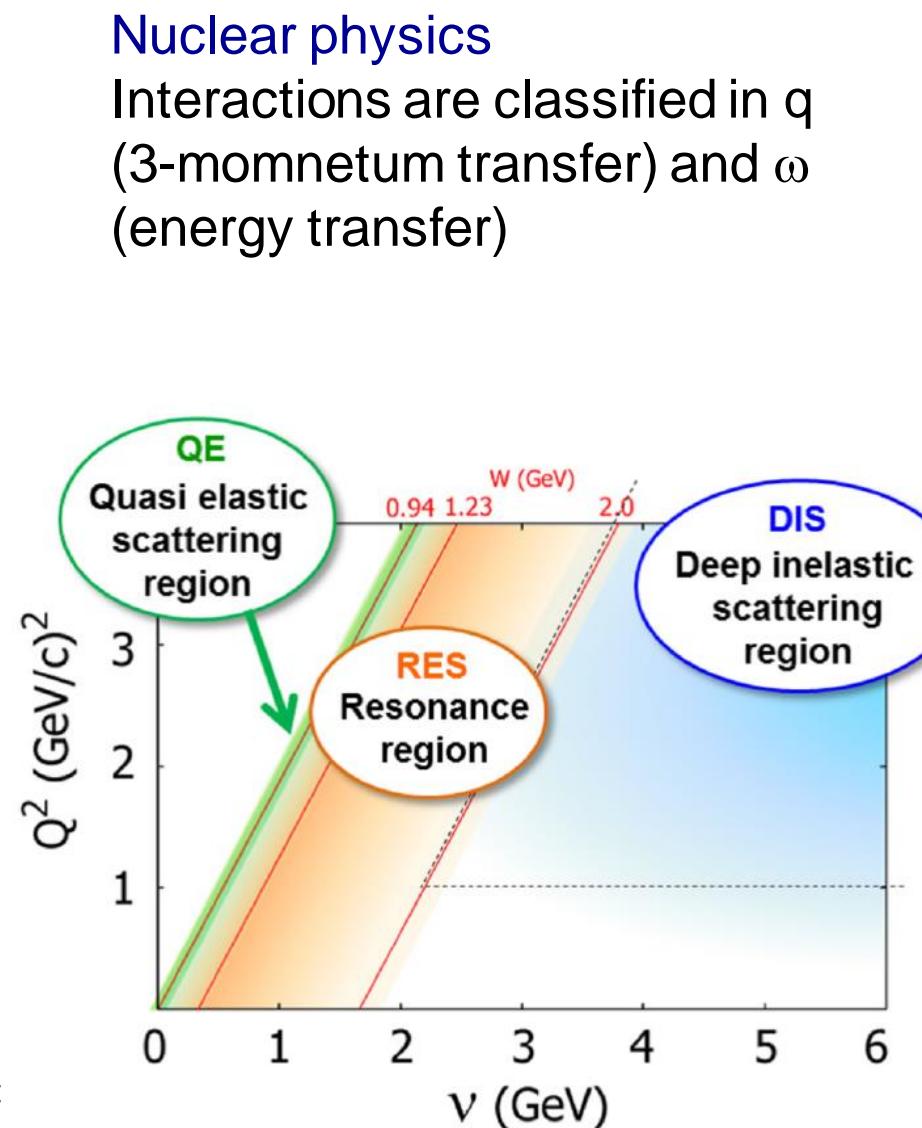
- Simple extrapolation may be broken due to nuclear physics
- We are not good at nuclear physics because we are not nuclear physicists
- Nuclear physics = non-perturbative QCD (many models, no theory)
- Particle physics is developed by avoiding nuclear physics...

$$P_{m \rightarrow e}(L / E) = \sin^2 2q \sin^2 \left( 1.27 D m^2 (eV^2) \frac{L(km)}{E(GeV)} \right)$$

# 1. Particle Physics vs. Nuclear Physics



**Particle physics (neutrino physics)**  
Interactions are classified in  $Q^2$  (4-momentum transfer) and  $v$  (energy transfer) or  $W^2$  (invariant mass)



# 1. Neutrino cross-section formula

Cross-section

- product of Leptonic and Hadronic tensor

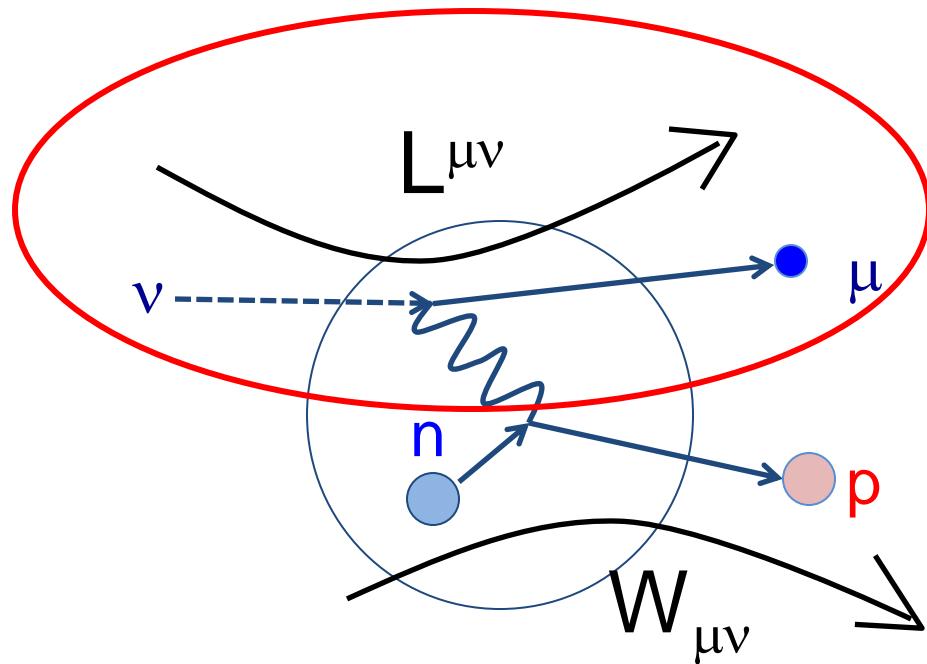
$$d\sigma \sim L^{\mu\nu} W_{\mu\nu}$$

Leptonic tensor

→ the Standard Model (easy)

Hadronic tensor

→ nuclear physics (hard)



# 1. Neutrino cross-section formula

Cross-section

- product of Leptonic and Hadronic tensor

$$d\sigma \sim L^{\mu\nu} W_{\mu\nu}$$

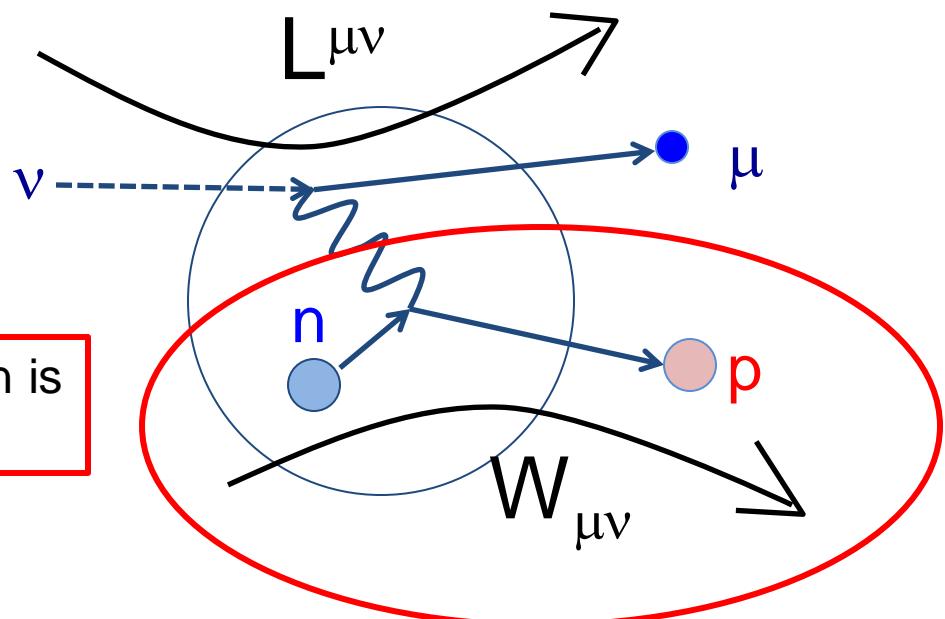
Leptonic tensor

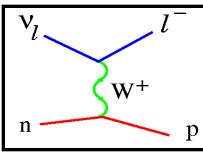
→ the Standard Model (easy)

Hadronic tensor

→ nuclear physics (hard)

All complication of neutrino cross-section is how to model the hadronic tensor part

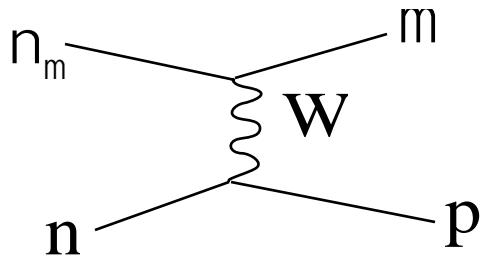




## 2. Charged Current Quasi-Elastic scattering (CCQE)

The simplest and the most abundant interaction around  $\sim 1$  GeV.

$$n_m + n \xrightarrow{\text{R}} p + m^- \quad (n_m + X \xrightarrow{\text{R}} X' + m^-)$$



$$d\sigma \sim L_{\mu\nu} T^{\mu\nu}$$

$L_{\mu\nu} \sim J_\mu J_\nu$ : Lepton tensor

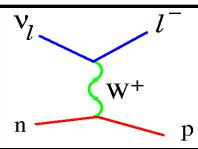
$W_{\mu\nu} = \int f(\vec{k}, \vec{q}, \omega) T_{\mu\nu} dE$ : hadronic tensor

$f(\vec{k}, \vec{q}, \omega)$ : nucleon phase space

$T_{\mu\nu} = T_{\mu\nu}(F_1, F_2, F_A, F_P)$ : form factors

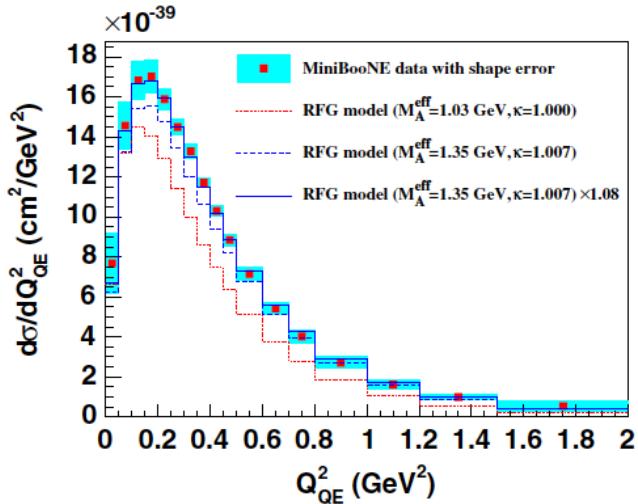
Form factors can be parameterized with **dipole form**

$$F(Q^2) = \frac{g}{\left(1 + \frac{Q^2}{M^2}\right)^2}$$



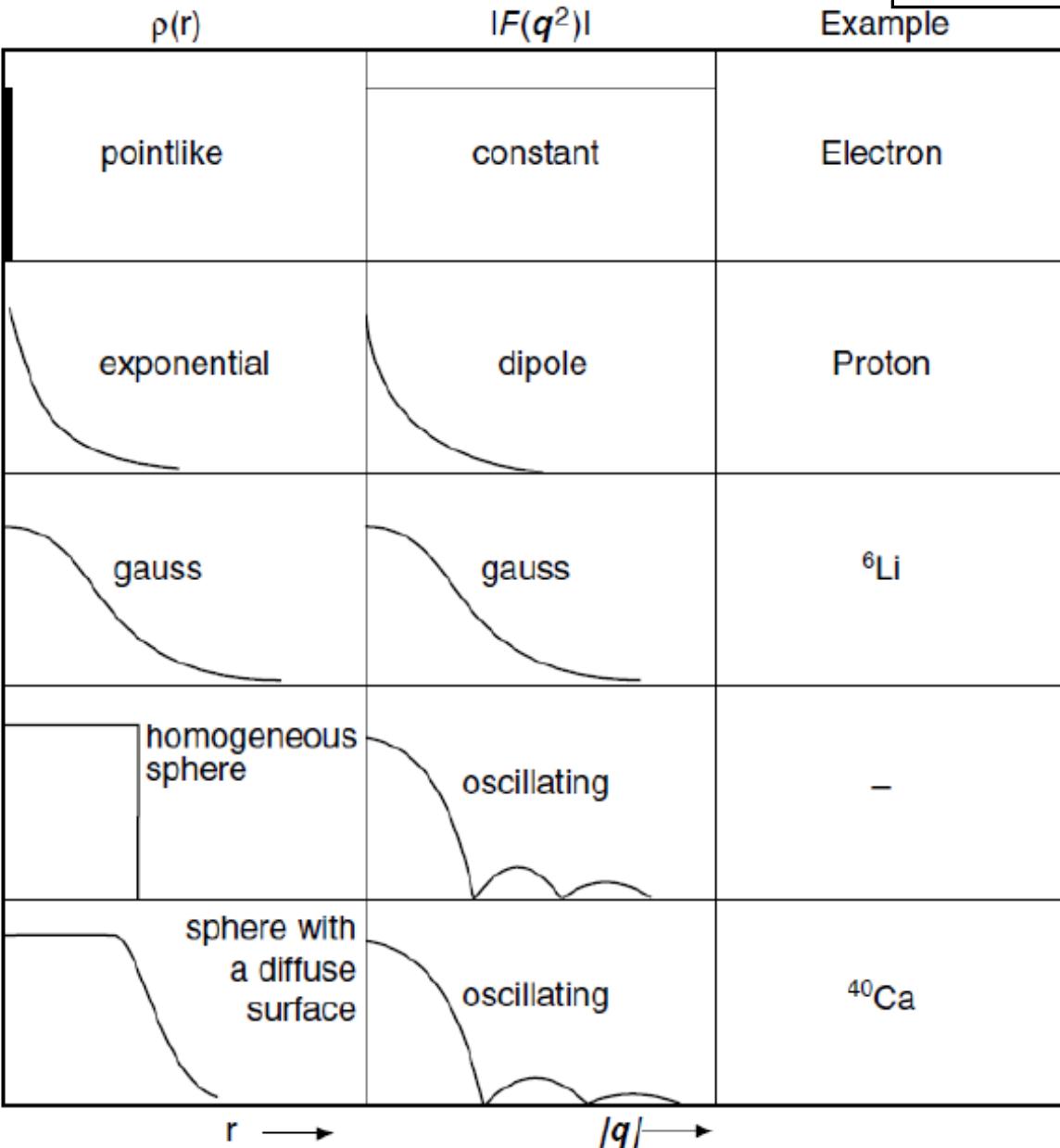
## 2. Form factors

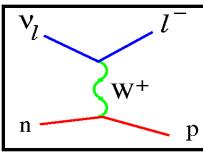
MiniBooNE CCQE cross section  
PRD81(2010)092005



Form factors can be parameterized with **dipole form**

$$F(Q^2) = \frac{g}{\left(1 + \frac{Q^2}{M^2}\right)^2}$$

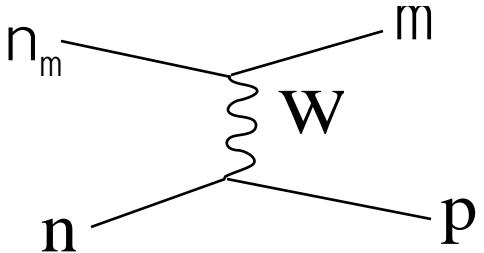




## 2. Charged Current Quasi-Elastic scattering (CCQE)

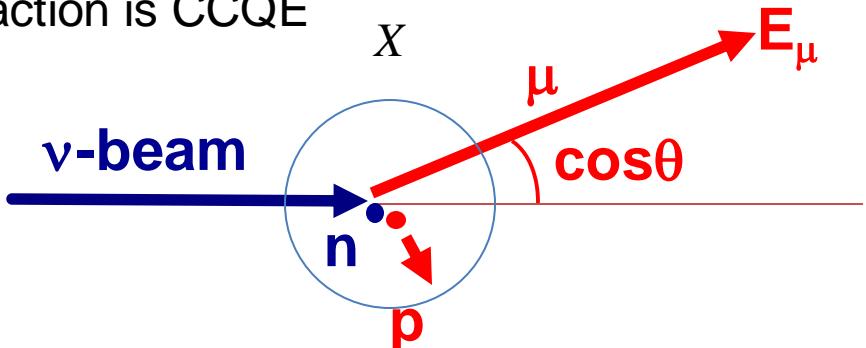
The simplest and the most abundant interaction around  $\sim 1$  GeV.

$$n_m + n \xrightarrow{\text{QE}} p + m^- \quad (n_m + X \xrightarrow{\text{QE}} X' + m^-)$$



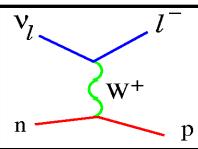
Neutrino energy is reconstructed from the observed lepton kinematics  
**“QE assumption”**

1. assuming neutron at rest
2. assuming interaction is CCQE



$$E_\nu^{QE} = \frac{M E_\nu - 0.5 m_\mu^2}{M - E_\mu + p_\mu \cos\theta}$$

Neutrinos hit nucleons inside of nucleus, and the energy reconstruction is possible only with QE assumption



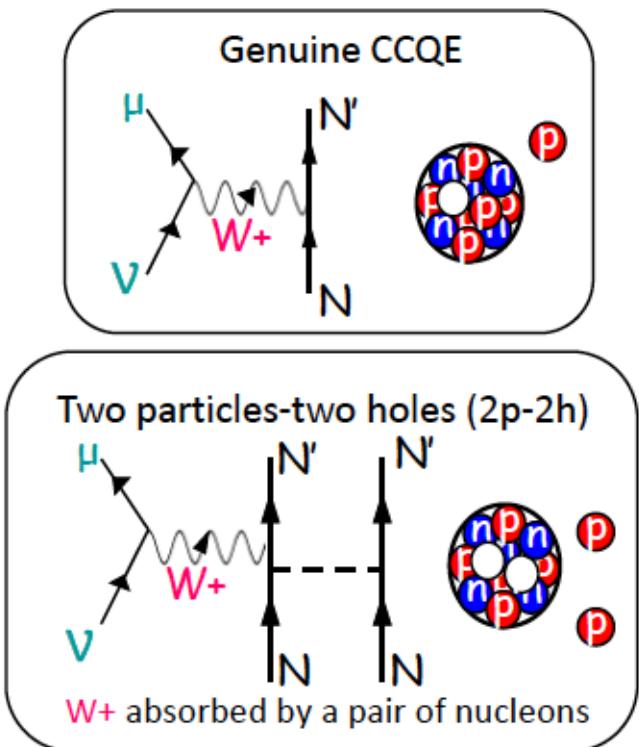
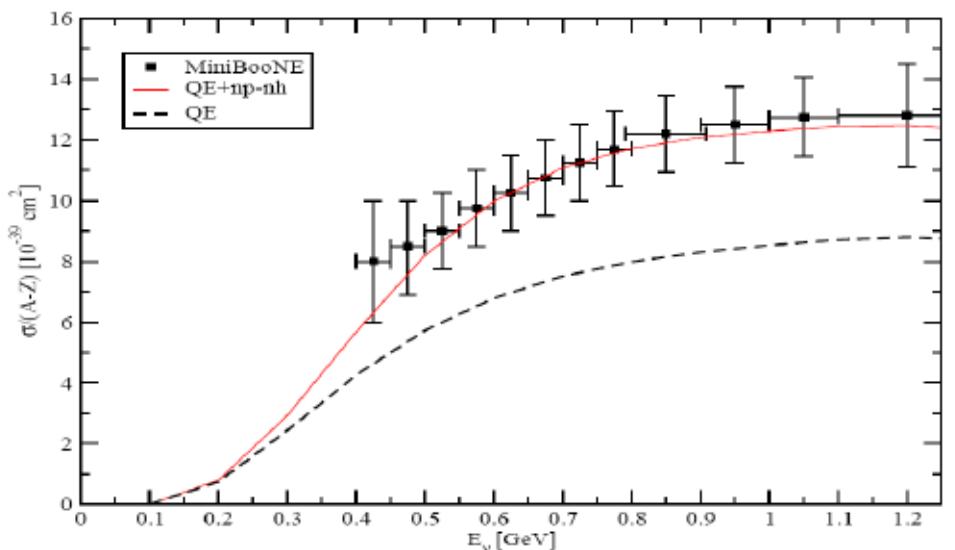
## 2. Nucleon correlations

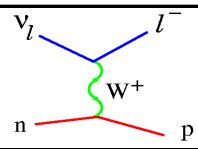
### 2-particle 2-hole (2p2h) effect

- Mimic CCQE interaction, significant change cross section (both shape and normalization)
- The biggest topic in nuxsec community (T2K, NOvA, MINERvA, MicroBooNE)

An explanation of this puzzle

Inclusion of the multinucleon emission channel (np-nh)



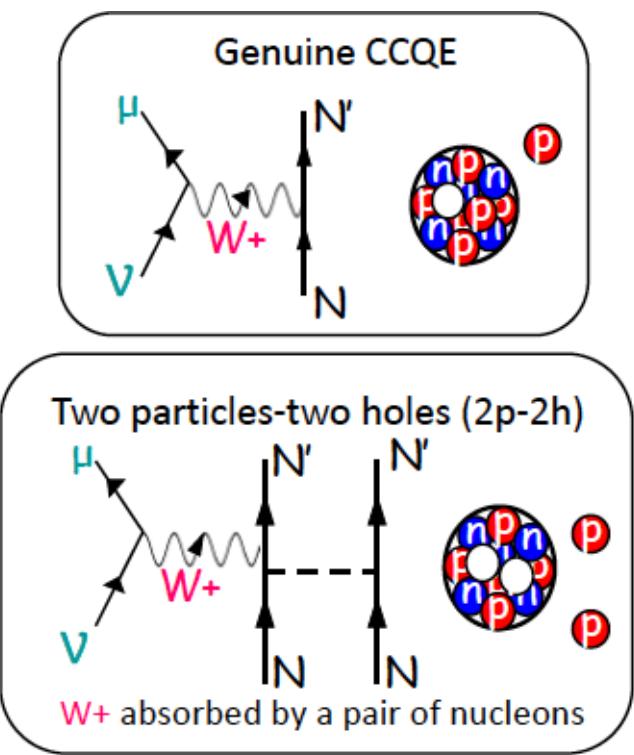
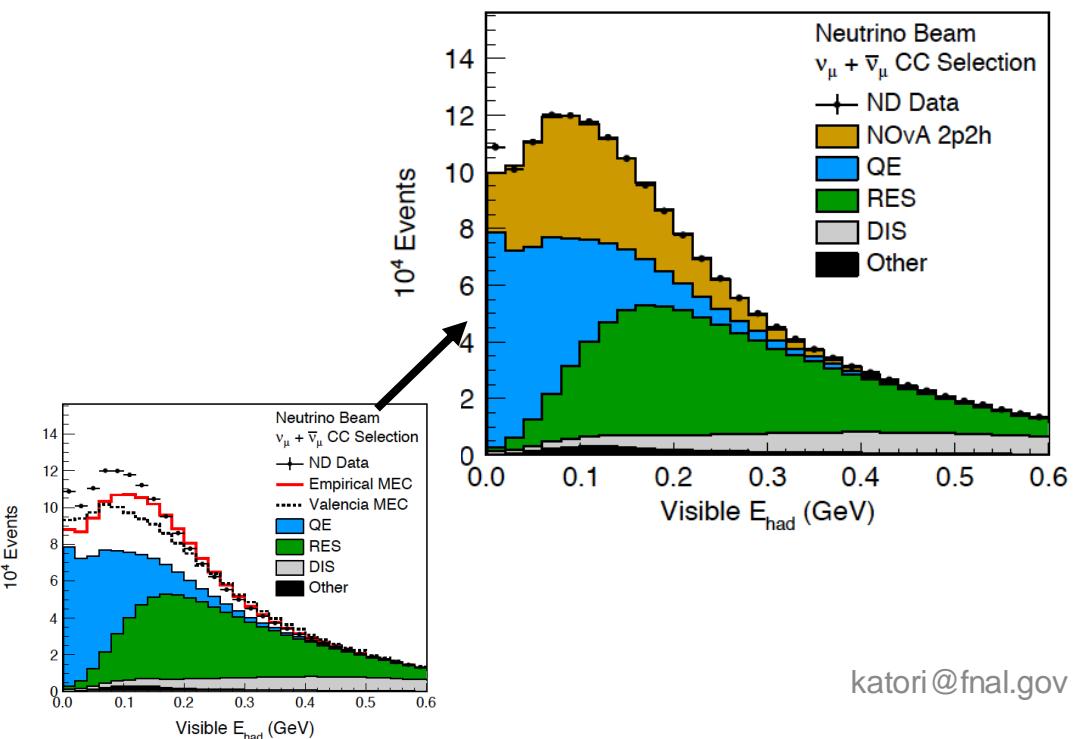


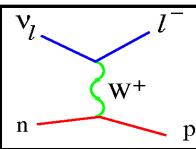
## 2. Nucleon correlations

### 2-particle 2-hole (2p2h) effect

- Mimic CCQE interaction, significant change cross section (both shape and normalization)
- The biggest topic in nuxsec community (T2K, NOvA, MINERvA, MicroBooNE)
- 2p2h models in generators don't describe data well?
- High resolution detector (LArTPC, emulsion, etc) can find what is going on?

NOvA near detector data-MC comparison after fit

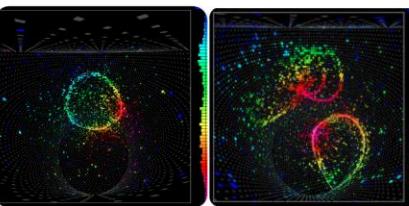
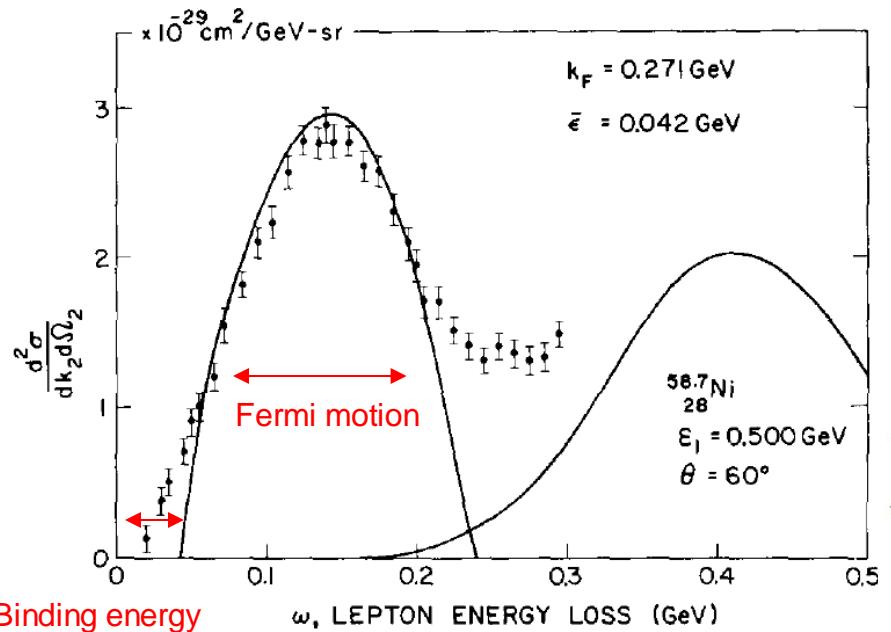




## 2. Fermi motion

### Fermi motion

- Measured energy is smeared from the true energy if you assume nucleon at rest
- High resolution detector can measure all outgoing hadrons  
→ initial nucleon momentum can be reconstructed (no Fermi motion smearing)



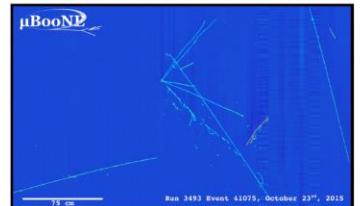
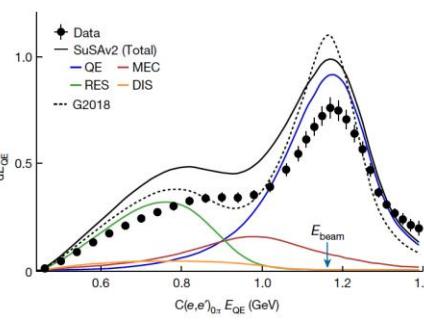
Cherenkov detectors:



Assuming QE interaction

Using lepton only

$$E_{QE} = \frac{2M\epsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l| \cos \theta_l)}$$



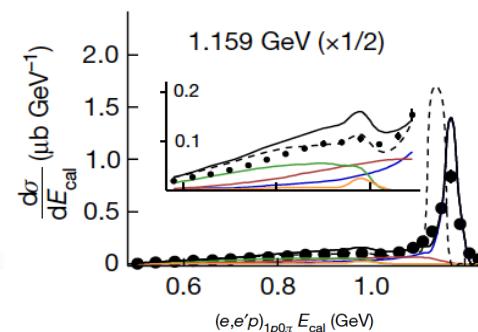
Tracking detectors:

Calorimetric sum

Using All detected particles

$$E_{cal} = E_l + E_p^{\text{kin}} + \epsilon$$

[1p0π]

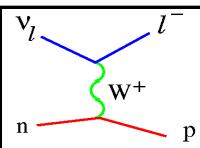


QE formula (HyperK)

katori@fnal.gov

Calorimetric (DUNE)

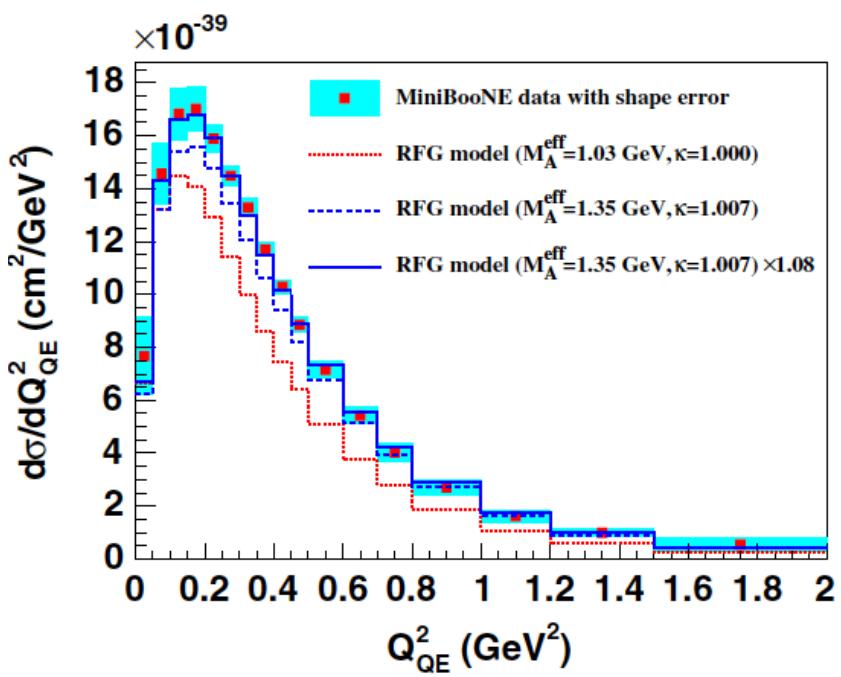
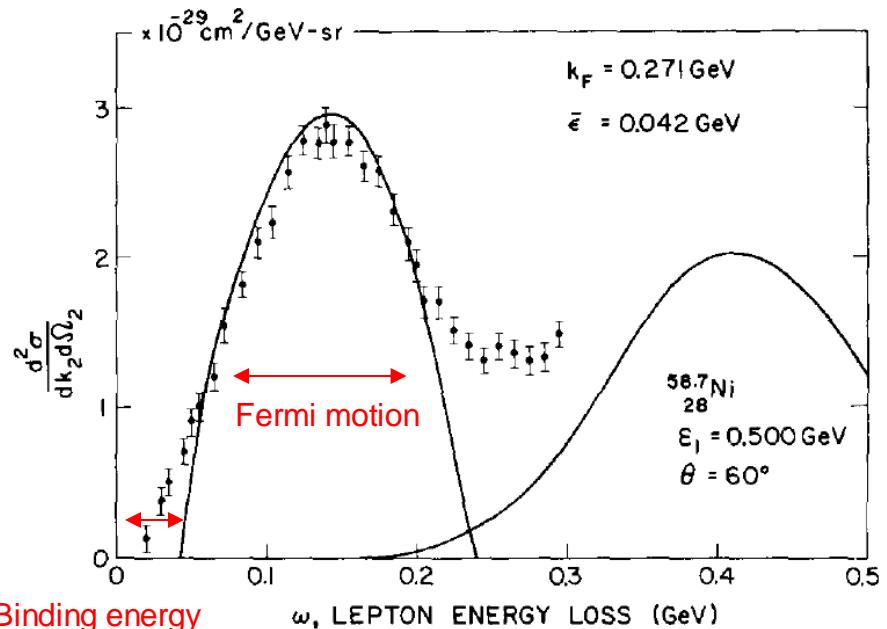
5b

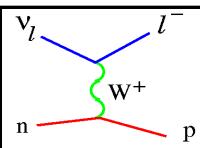


## 2. Pauli blocking

### Pauli blocking

- Low momentum transfer reaction is forbidden.
- data show more suppression than what Pauli blocking can → RPA(?)
- In the global Fermi gas model, Pauli blocking looks unphysical

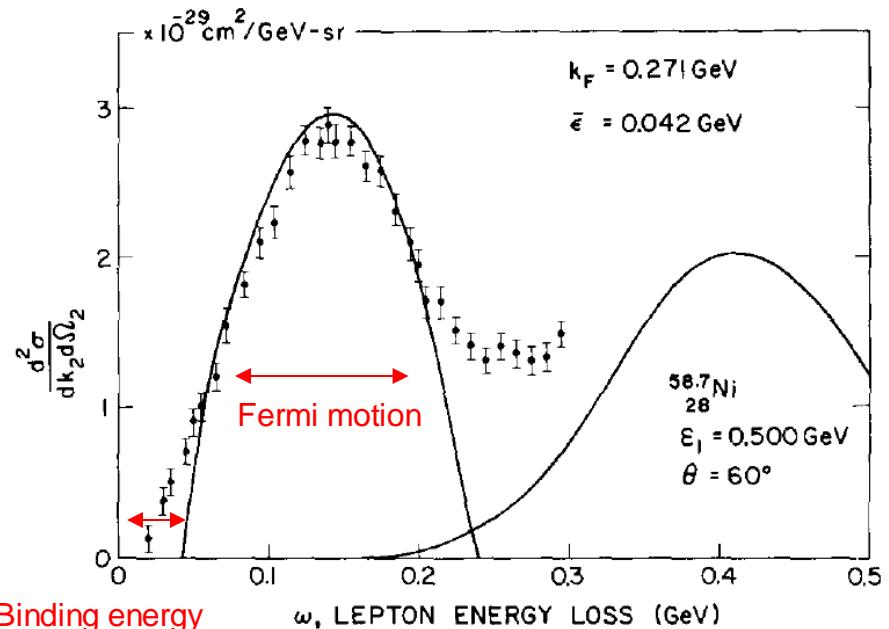




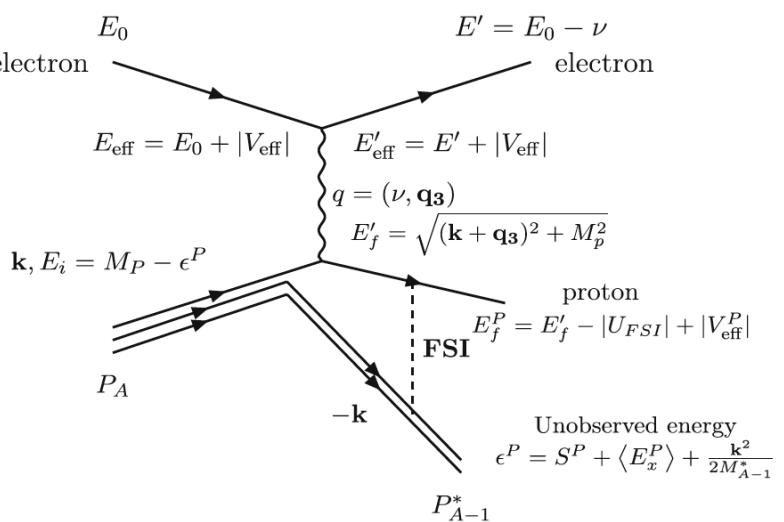
## 2. Nuclear Shell structure and binding energy

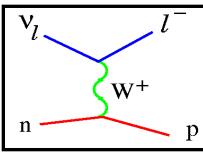
Binding energy ~ unobserved energy

- Energy to cost to release 1 nucleon, not constant
- Separation energy + excitation energy + recoil energy
  - Separation energy: energy to release 1 nucleon from the shell (~15 MeV, depends)
  - Excitation energy: energy used to excite leftover target nucleus (~1 MeV)
  - Recoil energy: kinetic energy of recoil target nucleus (~2-3 MeV)



Electron scattering on proton

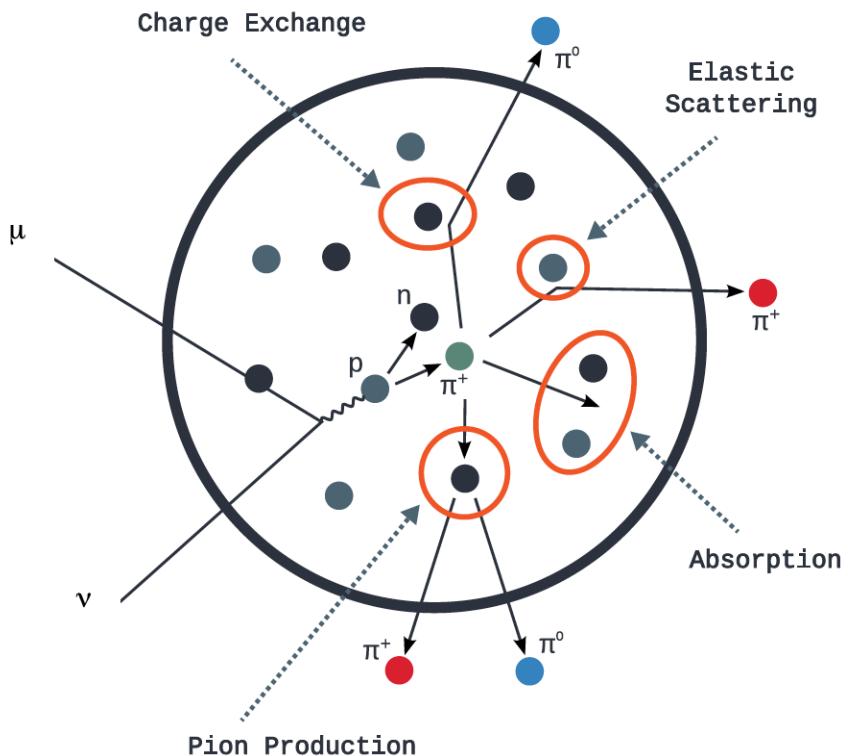


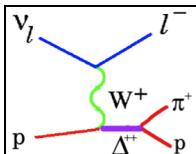


## 2. Final state interaction

### Cascade model

- Elastic scattering: Nucleon elastic scattering, pion elastic scattering
- Inelastic scattering: Nucleon inelastic scattering, pion inelastic scattering
- Charge exchange: Nucleon charge exchange, pion charge exchange
- Absorption: Nucleon absorption, pion absorption

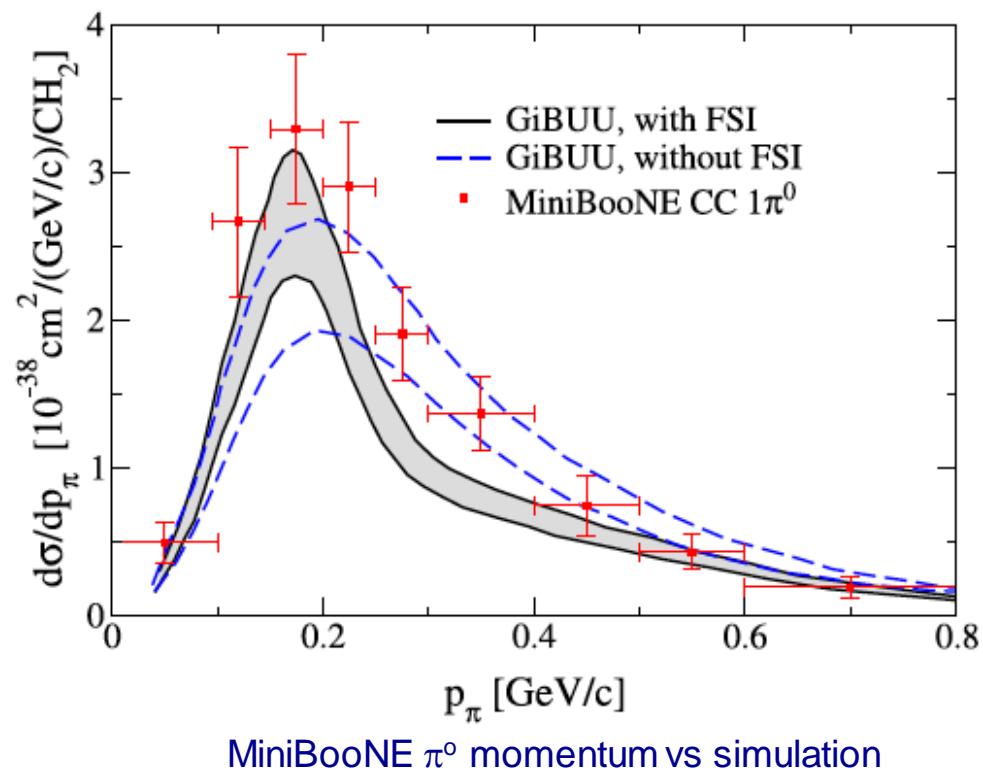
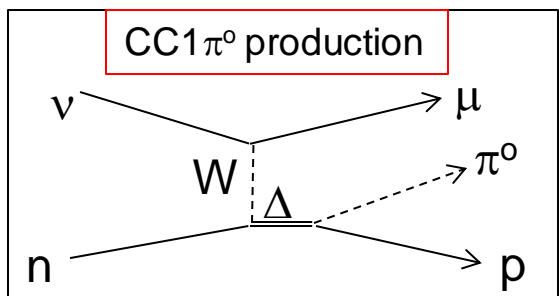


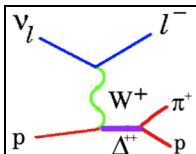


### 3. Neutrino Baryonic resonance data

#### Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation

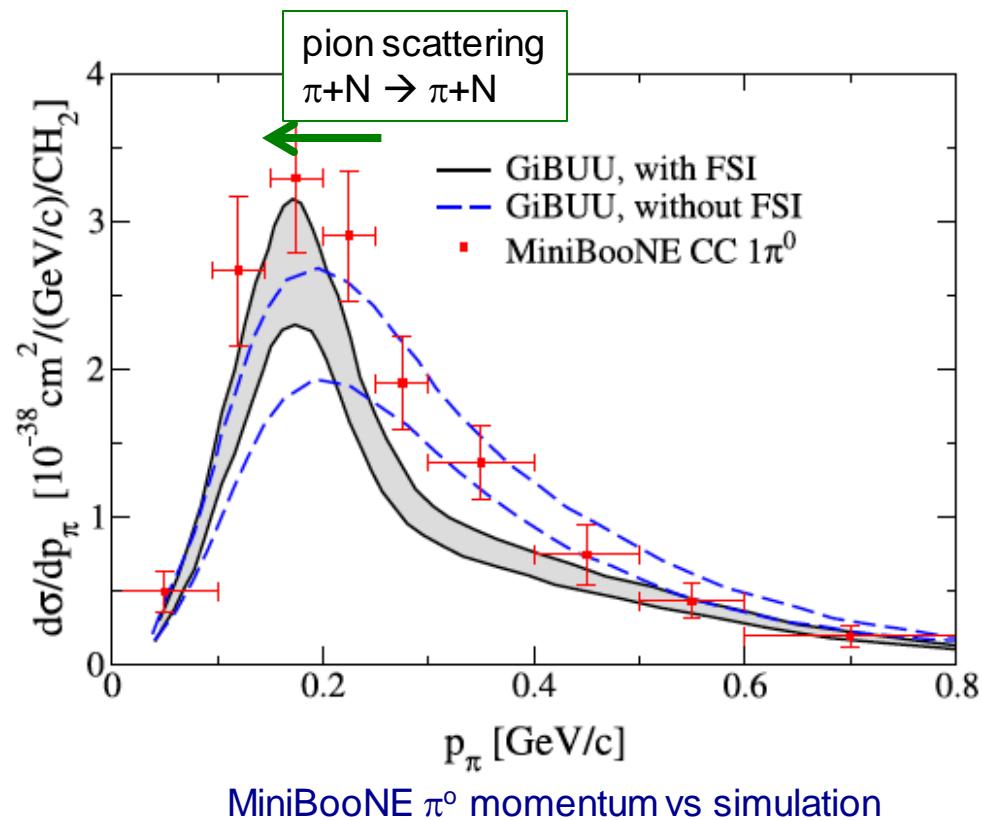
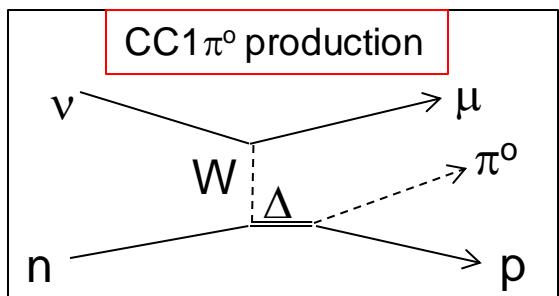


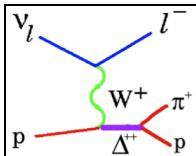


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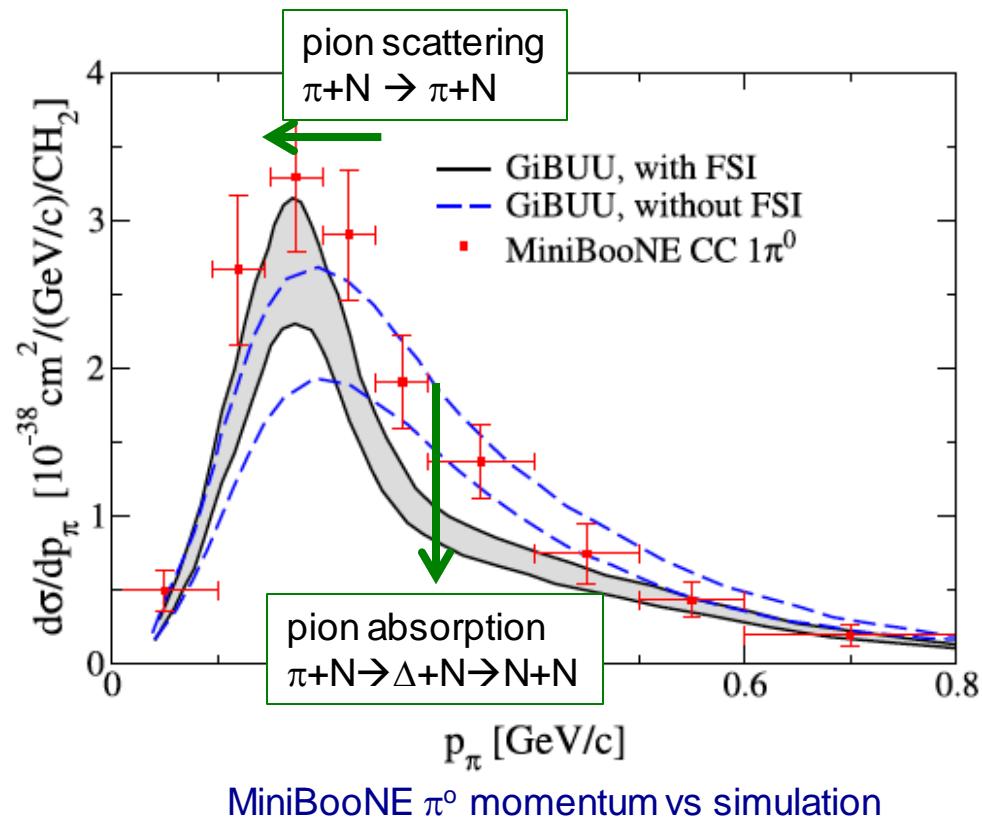
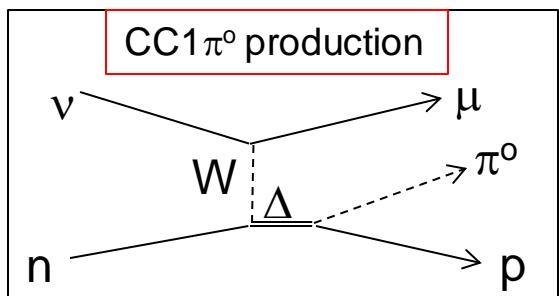




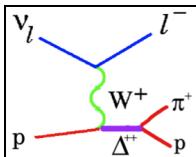
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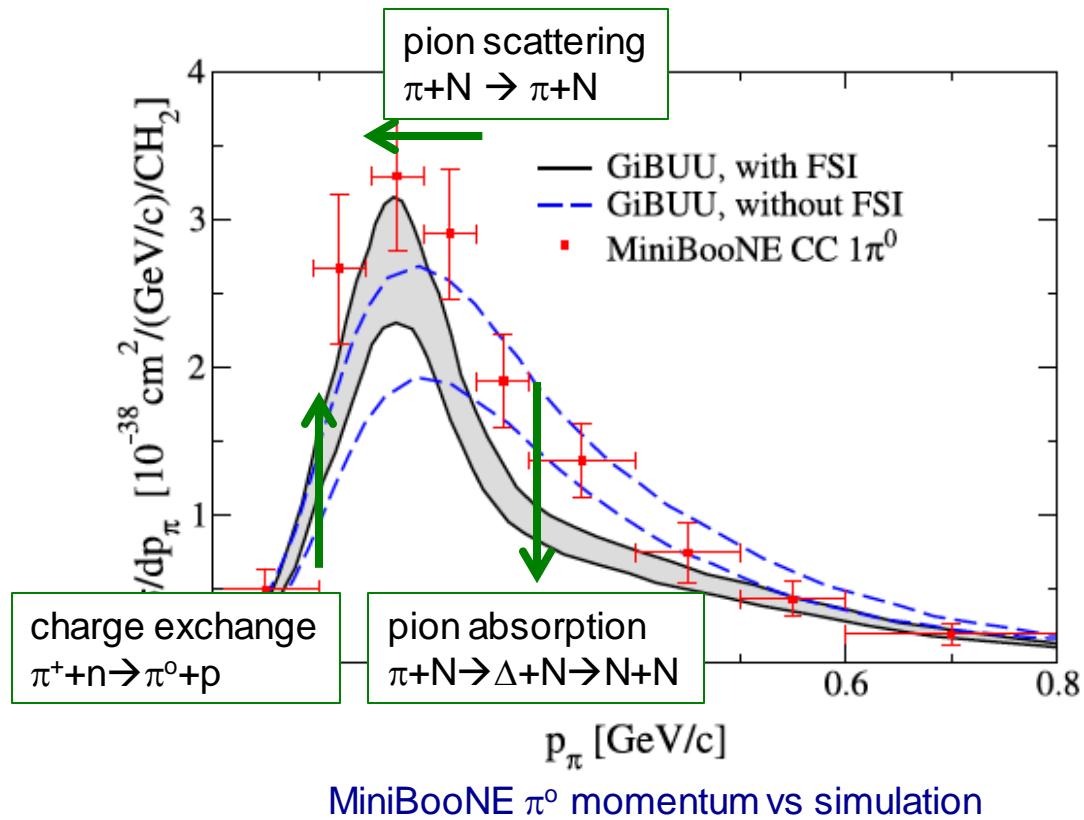
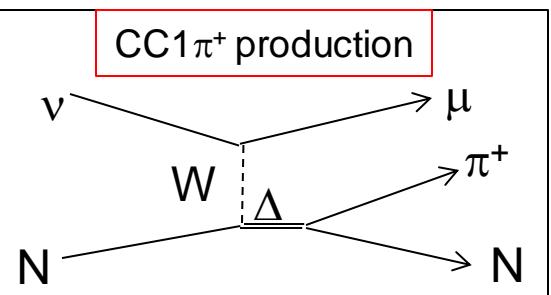
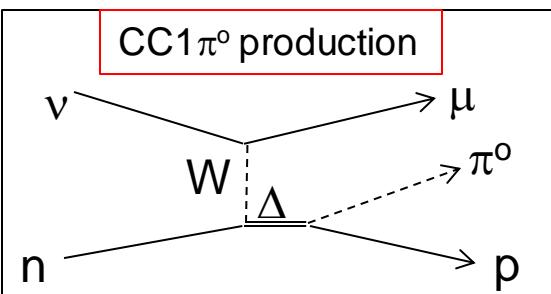
MiniBooNE  $\pi^0$  momentum vs simulation



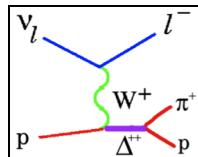
### 3. Neutrino Baryonic resonance data

#### Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation



All neutrino baryonic resonance processes have ~30% errors



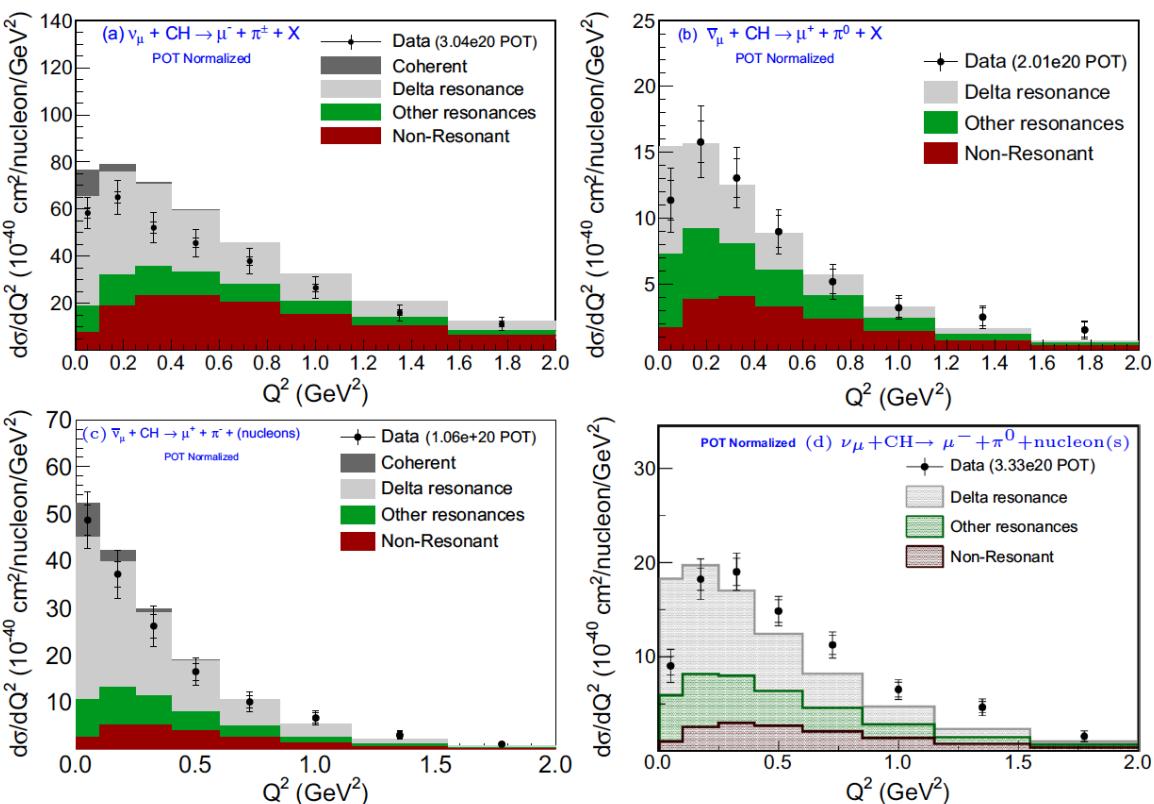
### 3. pion production global fit

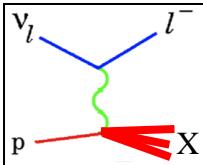
#### MINERvA pion data

- It is extremely difficult to tune pion and/or FSI parameters to fit all pion data
- $\nu_\mu CC\pi^\pm$ , low Q2 suppression, over-predicted
- $\nu_\mu CC\pi^0$ , strong low Q2 suppression
- $\bar{\nu}_\mu CC\pi^-$ , no low Q2 suppression
- $\bar{\nu}_\mu CC\pi^0$ , low Q2 suppression, under-predicted

The study relies of available knobs in the simulation

It looks the simulation doesn't have good knobs to tune or missing



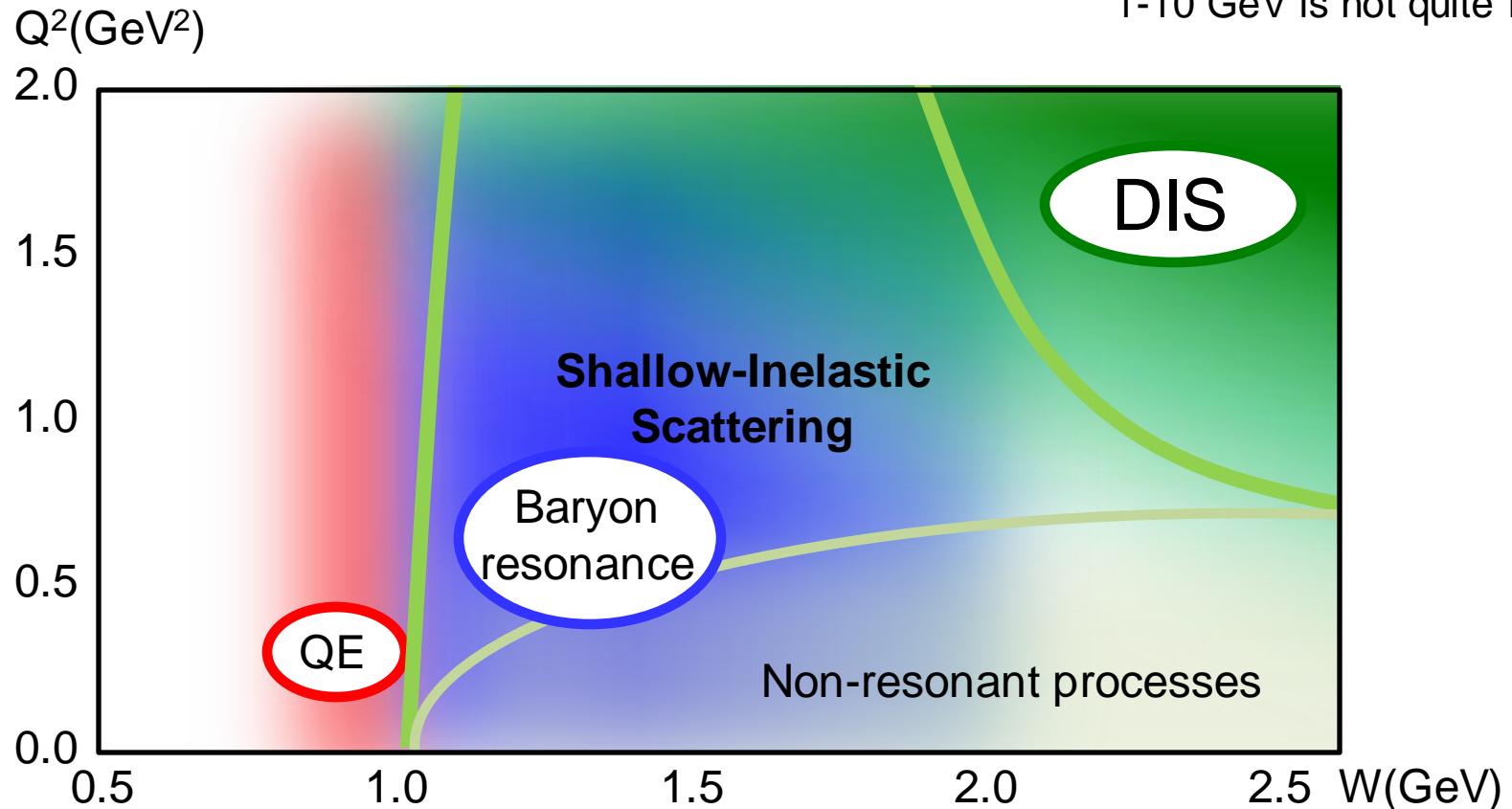


## 4. Shallow- and Deep-Inelastic Scattering (SIS and DIS)

### Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low  $Q^2$ , low  $W$  DIS)
- Nuclear dependent DIS

Neutrino experiment around 1-10 GeV is not quite DIS yet



## 4. Higher baryonic resonances

### Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low  $Q^2$ , low  $W$  DIS)
- Nuclear dependent DIS

### DCC model

- Total amplitude is conserved
- Channels are coupled ( $\pi N$ ,  $\pi\pi N$ , etc)
- 2 pion productions  $\sim 10\%$  at 2 GeV

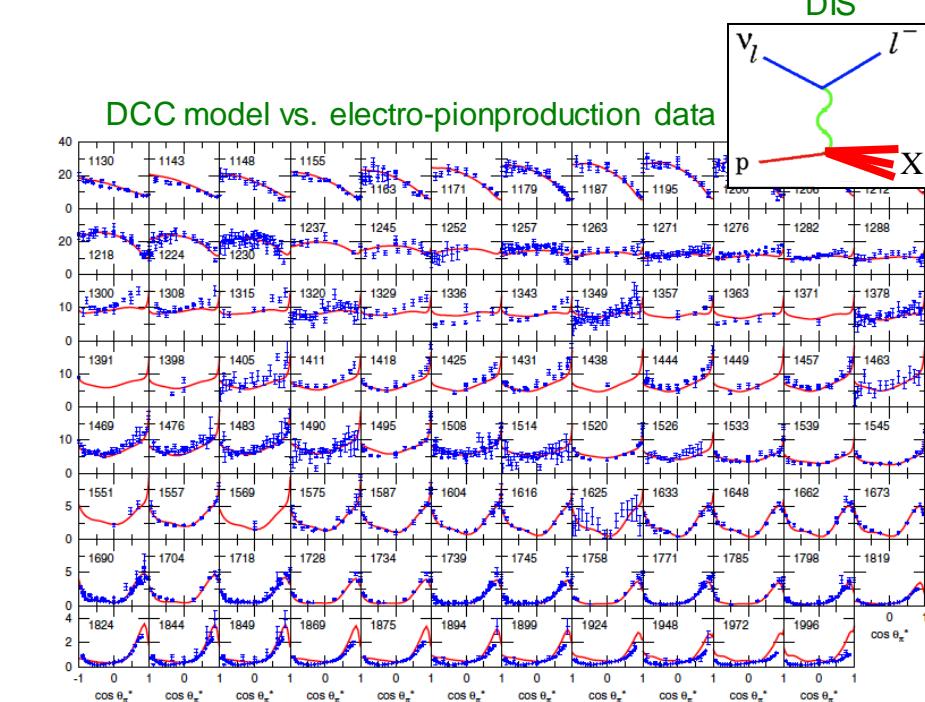
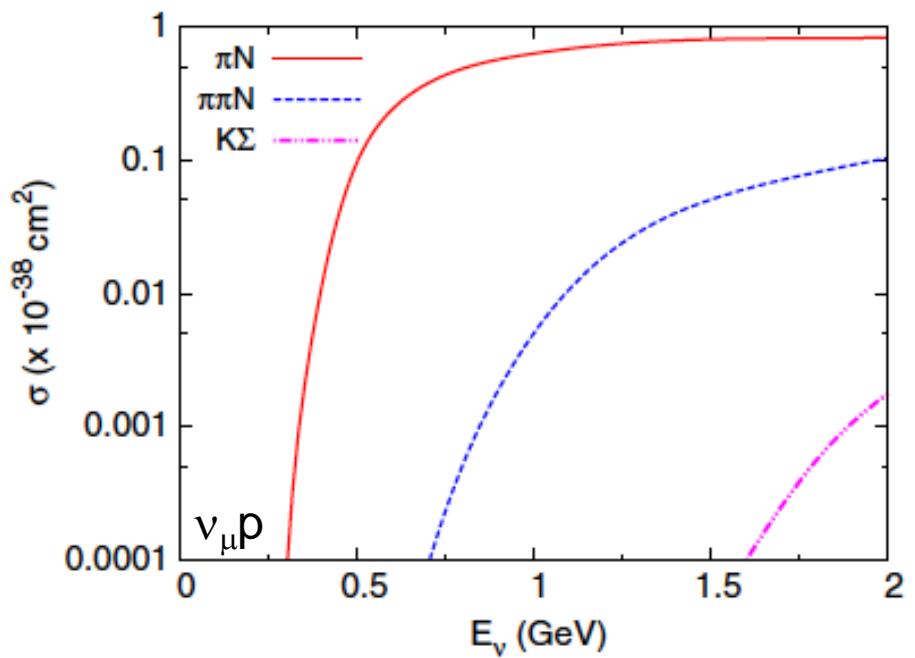
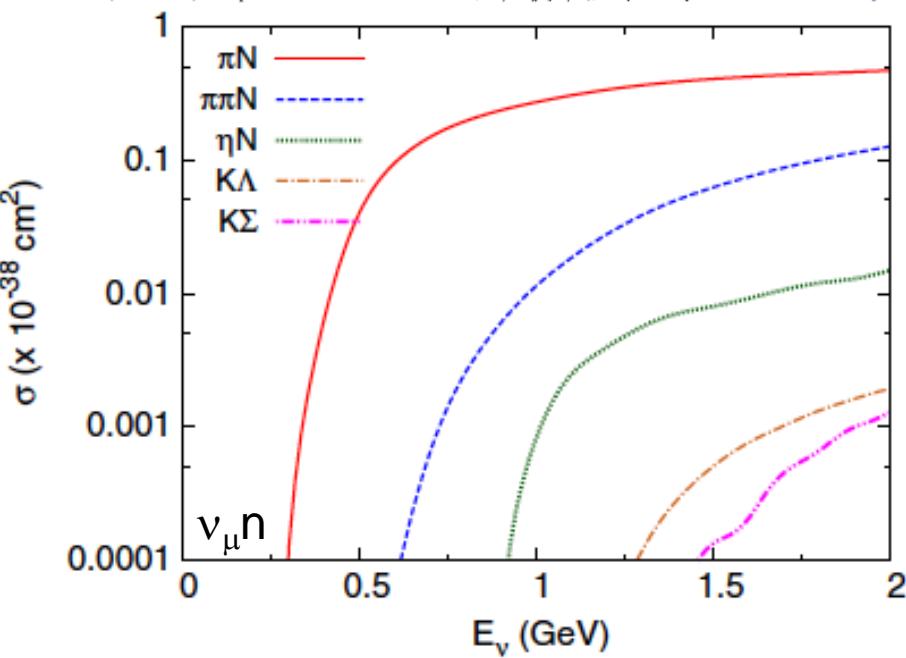


FIG. 8 (color online). Unpolarized differential cross sections,  $d\sigma/d\Omega_\pi^*$  ( $\mu\text{b}/\text{sr}$ ), for  $\gamma n \rightarrow \pi^- p$ . The data are from Refs. [55–78].



## 4. Quark-Hadron duality

### Cross section

- Higher resonances and hadron dynamics
- **Quark-Hadron duality (low  $Q^2$ , low  $W$  DIS)**
- Nuclear dependent DIS

### GRV98 LO PDF + Bodek-Yang correction

- GRV98 for low  $Q^2$  DIS
- Bodek-Yang correction for QH-duality
- 20 years old, out-of-dated
- not sure how to implement systematic errors

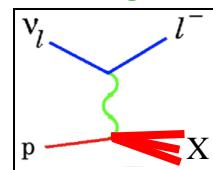
$$\xi \rightarrow \xi_\omega = \frac{2x \left( 1 + \frac{M_f^2 + B}{Q^2} \right)}{\left( 1 + \sqrt{1 + \frac{4x^2 M^2}{Q^2}} \right) + \frac{2Ax}{Q^2}}$$

$$K_{valence}(Q^2) = [1 - G_D^2(Q^2)] \cdot \left( \frac{Q^2 + C_{v2}}{Q^2 + C_{v1}} \right)$$

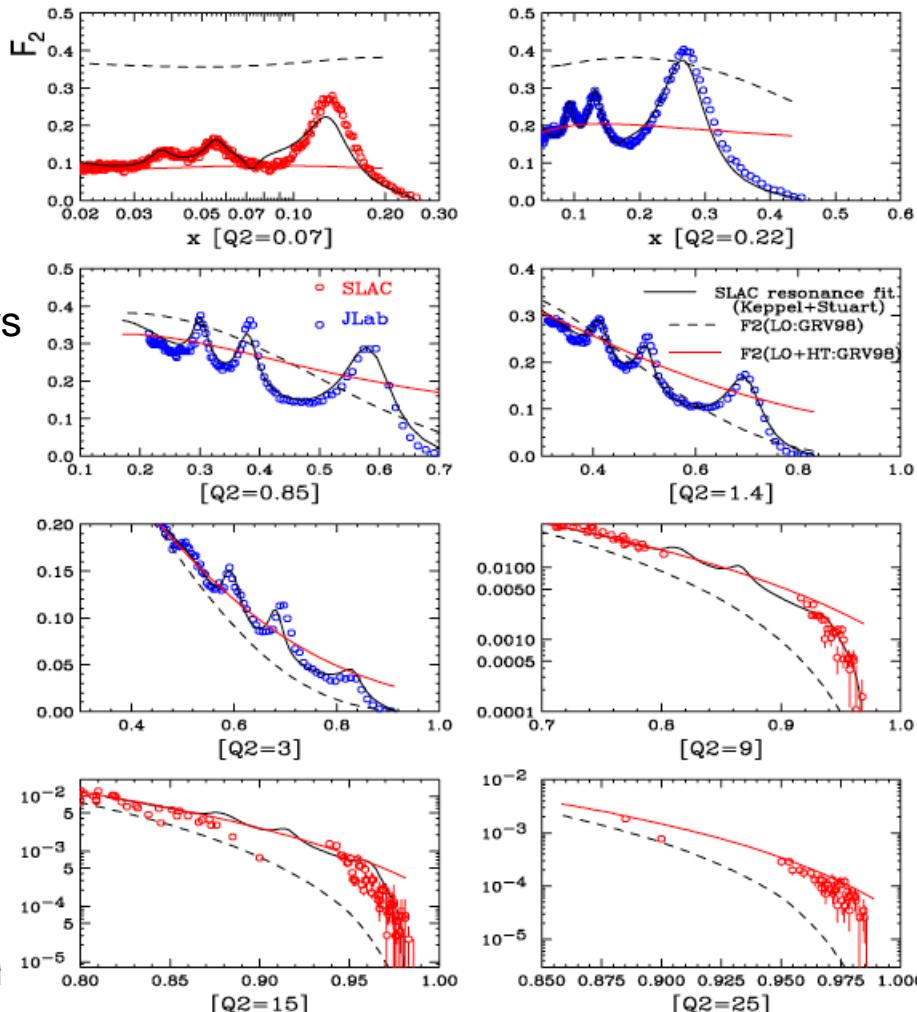
$$K_{sea}(Q^2) = \frac{Q^2}{Q^2 + C_{s1}}$$

Nachtmann variable

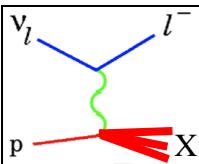
$$\xi = \frac{2x}{\left( 1 + \sqrt{1 + \frac{4x^2 M^2}{Q^2}} \right)}$$



Proton F2 function GRV98-BY correction vs. data



## 4. Nuclear dependent DIS

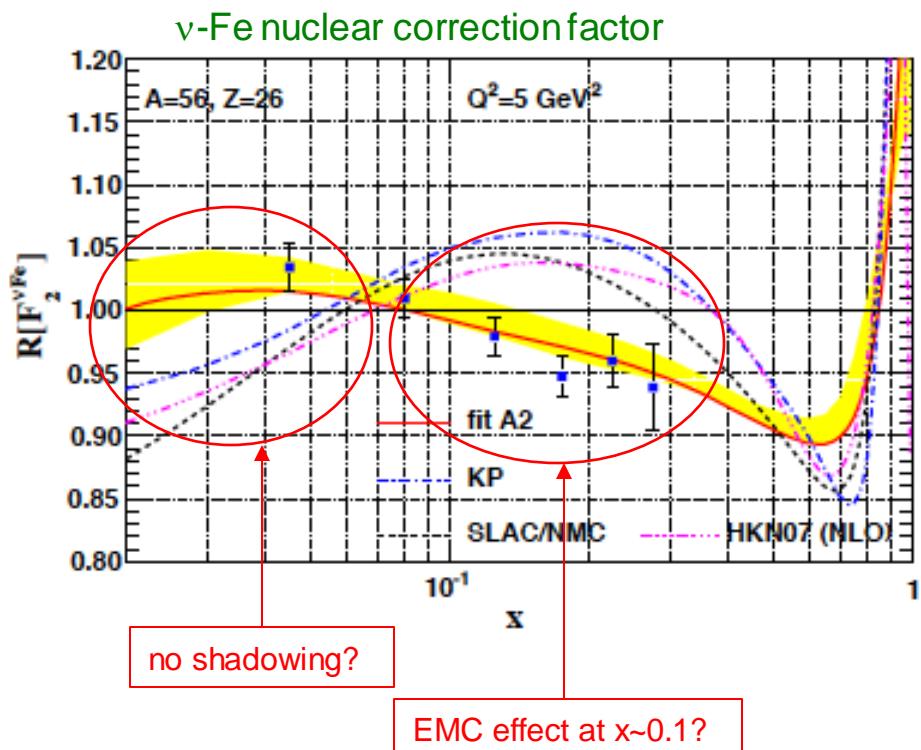
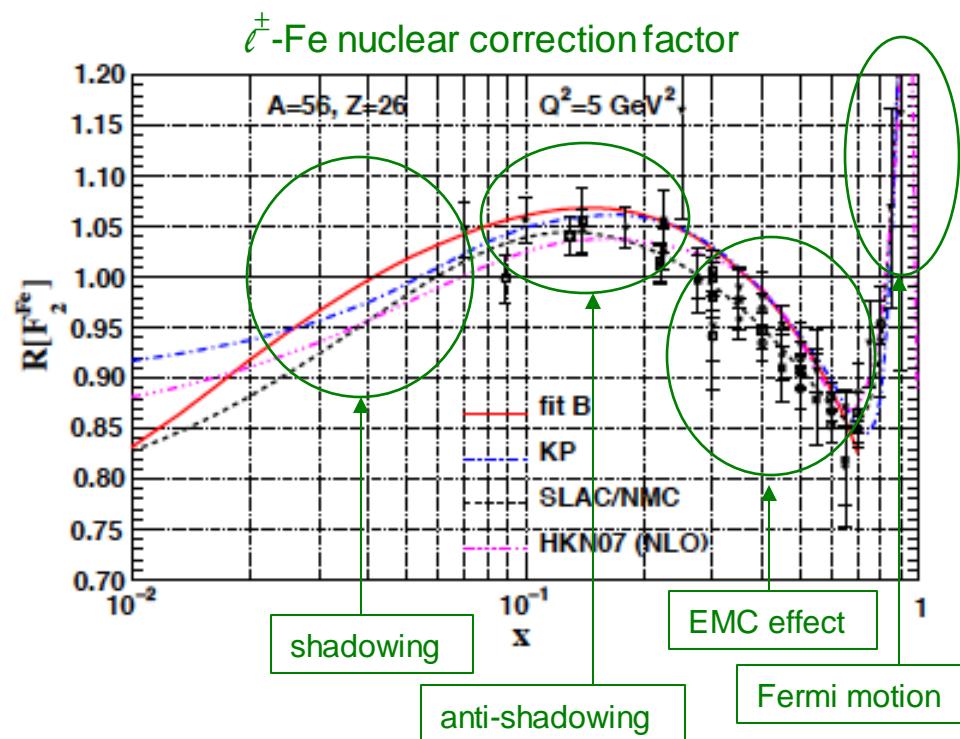


### Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low  $Q^2$ , low  $W$  DIS)
- Nuclear dependent DIS

### Nuclear PDF

- Shadowing, EMC effect, Fermi motion
- Likely due to nucleon dynamics in nucleus
- Various models describe charged lepton data
- Neutrino data look very different



# Conclusion

$\nu$ -N scattering : important reactions for long baseline neutrino oscillation experiment  
(T2K, NOvA, DUNE, Hyper-Kamiokande, etc)

CCQE: charged-current quasi-elastic, around 1 GeV

RES: baryonic resonance, around 2 GeV

DIS: deep inelastic scattering, 3 GeV to higher

Nuclear physics sucks

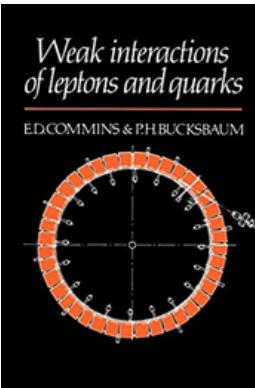
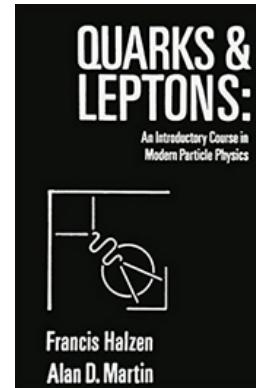
- Fermi motion: nucleon motion smears kinematic reconstruction
- Pauli blocking: It limits low momentum transfer reaction
- Nuclear shell structure: separation energy (missing energy) for different nucleons
- Final state interaction: RES looks like CCQE, DIS looks like RES, etc
- Nucleon correlation: Physics between  $\nu$ -N and  $\nu$ -A interaction
- Quark-Hadron duality: Physics between  $\nu$ -q and  $\nu$ -N interaction
- Nuclear dependent PDF: Physics between  $\nu$ -q and  $\nu$ -A interaction

Currently, ~30% error is acceptable for many processes

# References (books)

Quarks and Leptons (Halzen and Martin)

- show many calculations
- solutions for all exercises

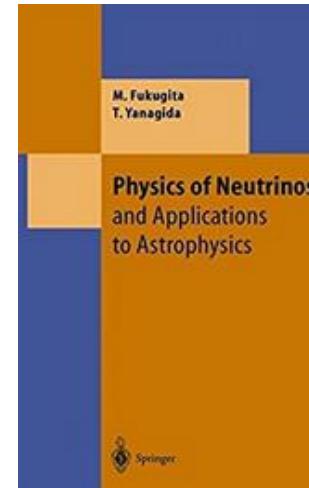


Weak interactions of Leptons and Quarks (Commins and Bucksbaum)

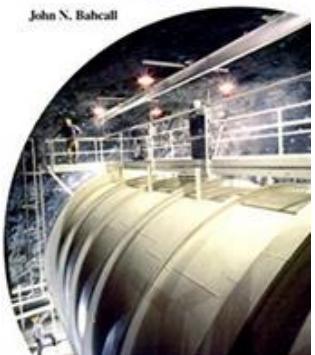
- show details of weak interaction calculations
- too many typos

Physics of Neutrinos (Fukugita and Yanagida)

- very intense
- from solar neutrinos to SUSY



Neutrino Astrophysics

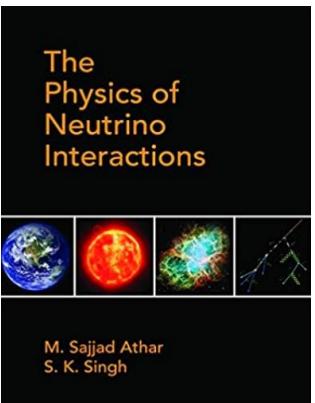
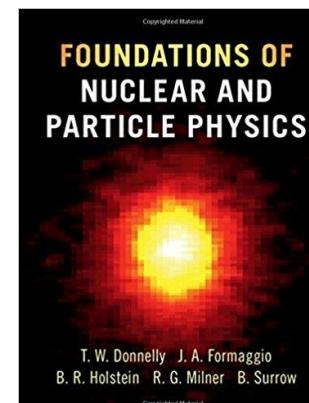


Neutrino astrophysics (Bahcall)

- good book to read

Foundation of Nuclear and Particle Physics (2017)

- Authors: Donnelly, Formaggio, Holstein, Milner, Surrow
- buy if your PhD thesis topic is about neutrino cross section measurements in T2K, NOvA, SBN, etc



The Physics of Neutrino interactions (2020)

- Authors: Sajjad Athar, Singh
- The newest book in this kind (970 pages!)

# References (papers)

“From eV to EeV: Neutrino cross sections across energy scales”

- Authors: Formaggio and Zeller (MicroBooNE spokesperson)
- Rev.Mod.Phys.84(2012)1307, <https://arxiv.org/abs/1305.7513>
- very good summary of neutrino cross sections

“Neutrino-Nucleus Cross Sections for Oscillation Experiments”

- Authors: Katori (me) and Martini (Martini model)
- J.Phys. G45 (2018) no.1, 013001, <https://arxiv.org/abs/1611.07770>
- A review both theoretical and experimental views

“NuSTEC White Paper: Status and challenges of neutrino–nucleus scattering”

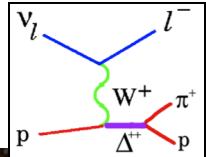
- NuSTEC (Neutrino Scattering Theory-Experiment Collaboration)
- Prog.Part.Nucl.Phys. 100 (2018) 1-68, <https://arxiv.org/abs/1706.03621>
- Cover all open issues in the community

“NuSTEC News”

- <http://nustec.fnal.gov/>
- subscribe mailing list, “like” facebook page, use #nuxsec

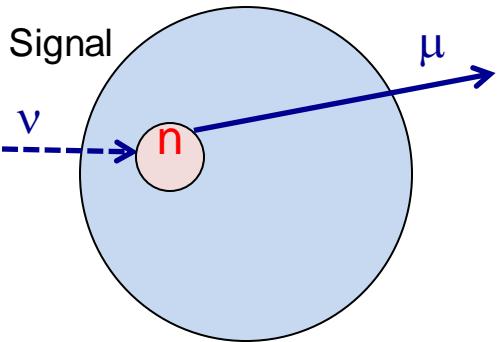
The screenshot shows the NuSTEC website homepage. At the top, there's a navigation bar with links for Home, Contact, Photo Book, Fermilab at Work, Jobs, We are 50, About, Science, Newsroom, Come visit us, and Resources for. Below the navigation is a large banner featuring a presentation slide with two plots showing neutrino scattering cross sections. To the right of the banner, the text "NuSTEC" is displayed. On the left side, there's a sidebar with links for Home, NuSTEC school, NuSTEC News, NuSTEC conference series, Workshops, conferences, schools, Database, and NuSTEC News. It also includes social media icons for Facebook, Twitter, and YouTube. On the right side, there are two smaller boxes: one for "NUINT 2017" (25-30 JUNE 2017, THE FIELDS INSTITUTE, UNIVERSITY OF TORONTO) and another for "NuSTEC School 2017" (7-15 November, 2017, Fermilab, USA). The footer contains the NuSTEC logo.

# Backup



### 3. non-QE background (resonance pion production)

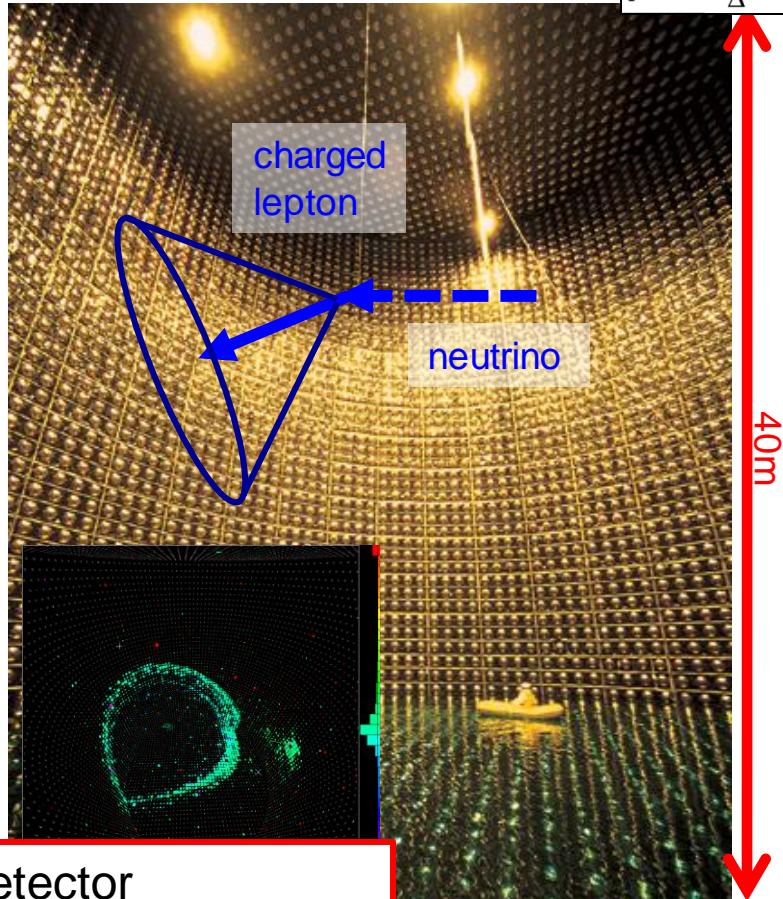
non-QE background → shift spectrum



Neutrino energy is reconstructed from the observed lepton kinematics

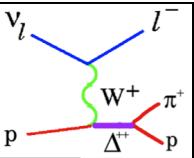
“QE assumption”

1. assuming neutron at rest
2. assuming interaction is CCQE



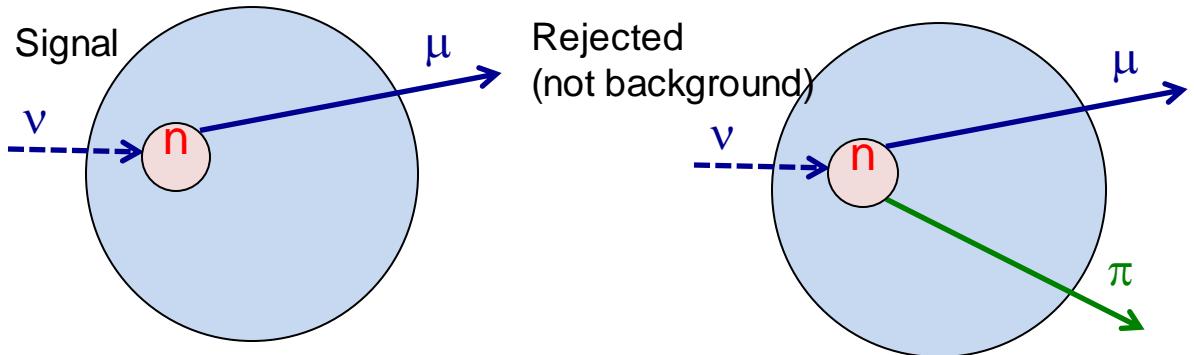
Typical neutrino oscillation detector

- Big and dense, to maximize interaction rate
- Coarsely instrumented, to minimize cost  
(not great detector to measure hadrons)



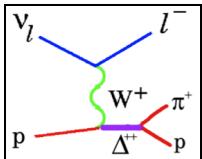
### 3. non-QE background (resonance pion production)

non-QE background → shift spectrum



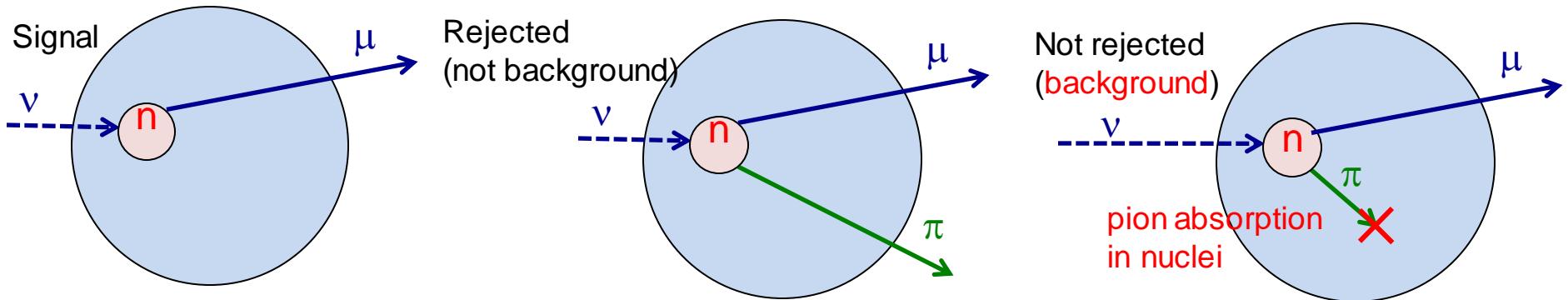
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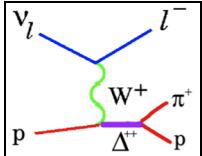
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non-QE background → shift spectrum



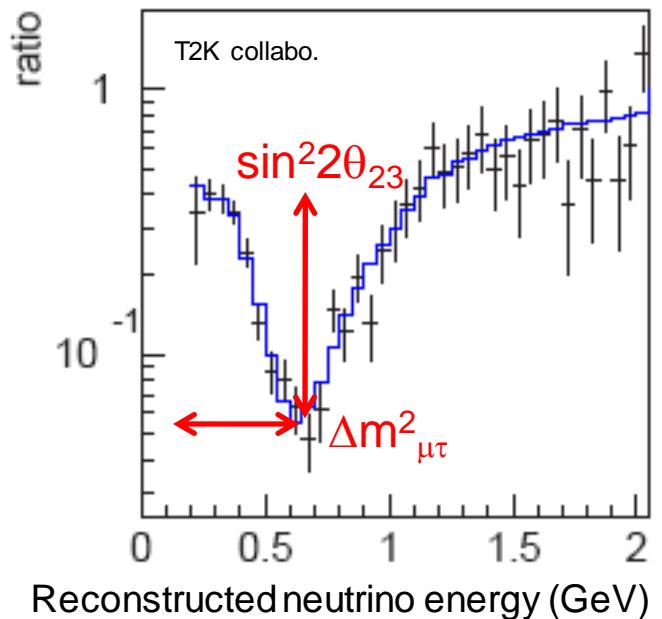
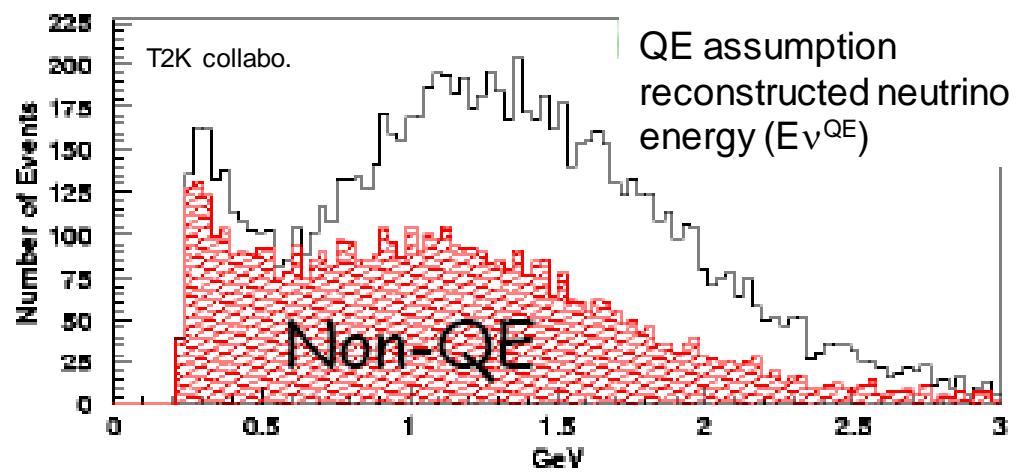
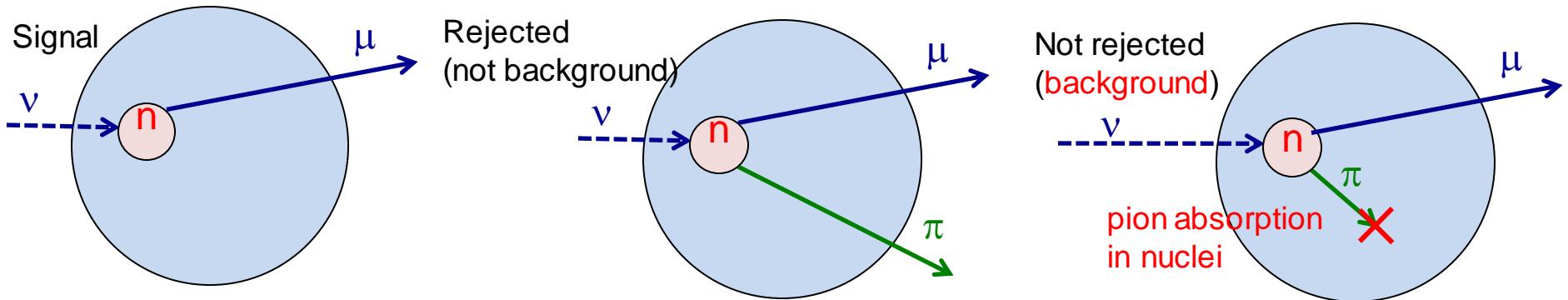
Typical neutrino oscillation detector

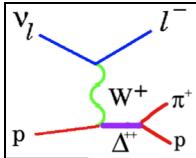
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### 3. non-QE background (resonance pion production)

non-QE background → shift spectrum

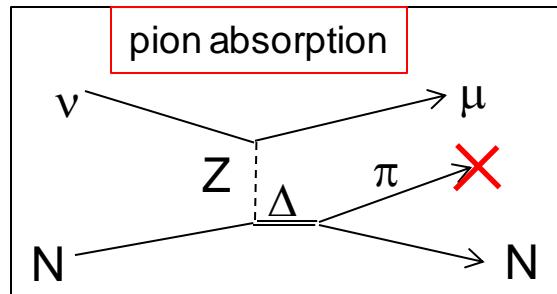




### 3. non-QE background (resonance pion production)

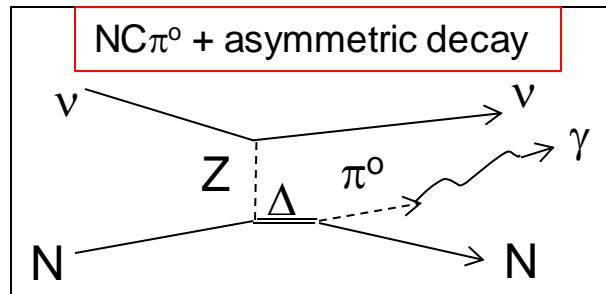
Pion production for  $\nu_\mu$  disappearance search

- Source of mis-reconstruction of neutrino energy

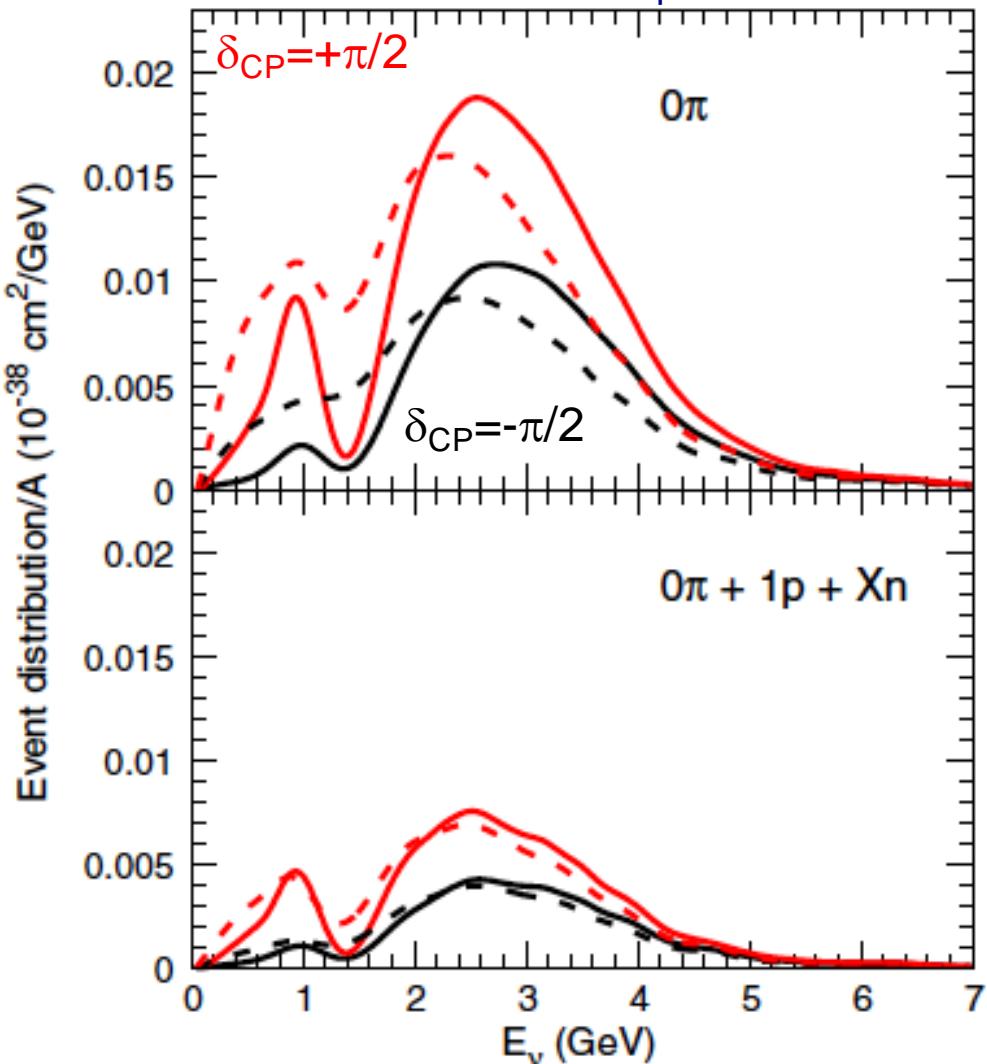


Neutral pion production in  $\nu_e$  appearance search

- Source of misID of electron



DUNE true vs. reconstructed  $E\nu$  spectrum



Understanding of neutrino baryonic resonance meson production is important for oscillation experiments