Neutrino Interaction Physics

Lecture 1: Introduction of neutrino interactions

- 1. Overview
- 2. Neutrino lepton scattering
- 3. Neutrino quark scattering (DIS)
- 4. Neutrino nucleus reactions

Lecture 2: Neutrino interactions for long baseline oscillation experiments

- 1. Overview
- 2. CCQE interaction
- 3. Baryonic resonances
- 4. Shallow inelastic scattering (SIS)

Teppei Katori King's College London Nov. 1, 2022

Subscribe "NuSTEC-News" <u>nustec.fnal.gov</u> like "NuSTEC-News" on Facebook page use hashtag #nuxsec



Formaggio and Zeller, Rev.Mod.Phys.,84 (2012) 1307

1. From eV to EeV: Neutrino cross sections across energy scales



1. From eV to EeV: Neutrino cross sections across energy scales



1. Scattering measurements

Size of wave packet ~ momentum transfer (~energy) $\hbar c = 197 MeV \cdot fm \rightarrow 200 \text{ MeV} \sim 1 \text{ fm} \text{ (size of nucleon)}$





1. Scattering measurements



1. Scattering measurements

Size of wave packet ~ momentum transfer (~energy) $\hbar c = 197 MeV \cdot fm \rightarrow 200 \text{ MeV} \sim 1 \text{ fm} \text{ (size of nucleon)}$

Lecture 1: Introduction of neutrino interactions

- 1. Overview
- 2. Neutrino lepton scattering (Standard Model)
- 3. Neutrino quark scattering (v-q scattering)
- 4. Neutrino nucleus reactions (v-A scattering)

Lecture 2: Neutrino interactions for long baseline oscillation experiments (v-N scattering)

- 1. Overview
- 2. CCQE interaction
- 3. Baryonic resonances
- 4. Shallow inelastic scattering



Alexander 2016 J.Phys.:Conf. Ser. 718(2016)062076

2. Neutrino-electron scattering

Neutrino – electron differential cross section

$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[c_L^2 + c_R^2 \left(\frac{E-T}{E} \right)^2 - C_L C_R \frac{m_e T}{E^2} \right]$$

T=recoil electron kinetic energy E=neutrino energy

	CL	C _R
ν _e - e⁻	$\frac{1}{2}$ +sin ² θ_{w}	$sin^2 \theta_w$
$\overline{ u_e}$ - e-	$sin^2\theta_w$	$\frac{1}{2}$ +sin ² θ_{w}
ν _μ - e ⁻	$-\frac{1}{2}+\sin^2\theta_w$	$sin^2\theta_w$
$\overline{ u_{\mu}}$ - e-	$sin^2\theta_w$	$-\frac{1}{2}$ +sin ² θ_w



2. MINERvA neutrino flux tuning

Neutrino – electron differential cross section

$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[c_L^2 + c_R^2 \left(\frac{E-T}{E}\right)^2 - C_L C_R \frac{m_e T}{E^2} \right]$$

T=recoil electron kinetic energy E=neutrino energy

$$#events = \left(\int flux \otimes cross \ section \otimes efficiency \otimes target \ number\right) \times exposure$$

By assuming detector efficiency and cross-section are known, you can measure neutrino flux





2. Neutrino magnetic moment

Neutrino – electron differential cross section

$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[c_L^2 + c_R^2 \left(\frac{E - T}{E} \right)^2 - C_L C_R \frac{m_e T}{E^2} \right]$$

T=recoil electron kinetic energy E=neutrino energy

Neutrino – electron differential cross section with neutrino magnetic moment

$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[c_L^2 + c_R^2 \left(\frac{E-T}{E}\right)^2 - C_L C_R \frac{m_e T}{E^2} \right] + \frac{\pi \alpha \mu_\nu^2}{m_e^2} \left(\frac{1}{T} - \frac{1}{E}\right)$$

large neutrino magnetic moment (BSM)

Lepton-only process (pure Standard Model) is often used to test new physics

SM



3. Neutrino-DIS cross section

Neutrino - single d-quark cross section

$$\frac{d\sigma}{dy}(\nu d \to \mu u) = \frac{G_F^2 x s}{\pi}$$

Neutrino – d-quark cross section

$$\frac{d\sigma}{dy}(\nu d \to \mu u) = \int_0^1 \frac{G_F^2 x s}{\pi} d(x) dx$$

Neutrino-nucleon DIS cross section

$$\frac{d\sigma}{dy}(\nu N \to \mu X) = \int_0^1 \frac{G_F^2 x s}{\pi} [(d(x) + s(x) \dots) + [\bar{u}(x) + \bar{c}(x) \dots](1 - y)^2] dx$$

Neutrino-nucleus DIS cross section with isoscalar assumption

$$\frac{d\sigma}{dy}(vA \to \mu X) = A \int_0^1 \frac{G_F^2 x s}{\pi} [Q(x) + \bar{Q}(x)(1-y)^2] dx$$
$$u^p(x) + u^n(x) = d^n(x) + d^p(x) = u(x) + d(x) \equiv Q(x)$$
$$\bar{u}^p(x) + \bar{u}^n(x) = \bar{u}^n(x) + \bar{u}^p(x) = \bar{u}(x) + \bar{d}(x) \equiv \bar{Q}(x)$$



3. Di-muon production



NuTeV, PRL88(2002)091802

3. Paschos-Wolfenstein ratio and NuTeV anomaly



IceCube, PRD104(2021)022002

3. Astrophysical high-energy neutrino measurement

Data and MC agree up to \sim PeV. \rightarrow We more or less understand neutrino interactions up to \sim PeV.







3. Neutrino DIS saturation









katori@fnal.gov

Dziewonski, Anderson (PREM), Phys. Earth Planet.Inter.25,(1981)297 Donini, Palomares-Ruiz, Salvado, Nature Physics 15(2019)37

3. Earth tomography

Earth absorption for Earth density measurement

- PREM (Preliminary reference Earth model)
- Standard earth density model used by T2K, NOvA, etc
- Earth density profile is extracted by assuming flux and cross section
- Measure Earth moment of inertia and Earth mass by neutrinos







3. Glashow resonance



A 5.9 PeV event in IceCube







3. Collider neutrino

FASERnu

- Emulsion detector (high-resolution)
- neutrinos from ATLAS collision point

p-p collision at IP

of ATLAS <

10 cm

- neutrino excess from pilot run
- ~10,000 neutrino events from LHC run3

forward jets

emplead hundered





beam collision axis

katori@fna

Akindele (Neutrieno2020), <u>https://zenodo.org/record/3959532</u> SONGS, Journal of Applied Physics, 105(6), 064902 (2009)

4. Reactor neutrino

Low energy electron anti-neutrinos

- High-precision spectrum prediction
- Monitoring fission reactor











4. Solar neutrino



GALLEX, PLB490(2000)16;SAGE, J.Expt.Theor.Phys.95(2002)181 Borexino, PRL 108(2012)051302

4. Solar neutrino

Gallium experiment

 v_e + ⁷¹Ga \rightarrow e⁻ + ⁷¹Ge

- Sensitive to pp-neutrino (0.42 MeV), 90% of total solar neutrino flux.

- Both experiments observed deficit, but higher than Homestake result





COHERENT, Science10.1126/science.aao0990 (2017), PRL126(2021)012002; 129(2022)081801

4. Neutrino-Nucleus coherent scattering

Cs



Ge

Neutron number

Cross section (10⁻⁴⁰ cm²)

Na



Conclusion

v-I scattering : well-known, test of weak theory
 Neutrino-electron scattering for neutrino flux measurement
 Anti-electron neutrino scattering for neutrino magnetic moment search (BSM)

v-q scattering : test of weak theory, test of quark model

DIS cross sections Di-muon production Paschos-Wolfenstein ratio Astrophysical neutrinos collider neutrinos

v-A scattering :

Reactor neutrino experiments Neutrino nuclear capture by CI and Ga, important for solar neutrinos Neutrino coherent scattering, important for supernova (2017)

v-N scattering : important reactions for long baseline neutrino oscillation experiment (T2K, NOvA, DUNE, Hyper-Kamiokande)

katori@fnal.go

1. From eV to EeV: Neutrino cross sections across energy scales



1. NuInt22 in Seoul (Oct. 24-29, 2022)

Neutrino interaction physics community https://nuint22.org/





The 13th International Workshop on Neutrino-Nucleus Interactions in the Few GeV Regions

October 24 to 29, 2022 (OFFLINE)

Hoam Faculty House Seoul National University Seoul, Korea





Formaggio and Zeller, Rev.Mod.Phys.84(2012)1307

1. Next generation neutrino oscillation experiments

Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE



1. Next generation neutrino oscillation experiments

Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE...



1. Next generation neutrino oscillation experiments

Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE...

Most of data are from muon neutrino beam

- create by π -DIF, K-DIF (pion and kaon decay-in-flight)
- $\Phi(\nu_{\mu}) > \Phi(\bar{\nu}_{\mu})$: more π^+ and K⁺ than π^- and K⁻ (for low energy accelerators)
- μ -decay can make electro-neutrinos but they are background
- δ_{CP} study need electro-neutrino and antineutrino cross-sections (v_e appearance)

Nuclear physics sucks

- Simple extrapolation may be broken due to nuclear physics
- We are not good at nuclear physics because we are not nuclear physicists
- Nuclear physics = non-perturbative QCD (many models, no theory)
- Particle physics is developed by avoiding nuclear physics...



 ${}_{k}P_{\mu\to e}(L/E) = \sin^{2}2\theta\sin^{2}\left(1.27\Delta m^{2}(eV^{2})\frac{L(km)}{E(GeV^{2})}\right)$

Benhar, Day, Sick, Rev. Mod. Phys. 80(2008) 189 Nakamura et a;, Rep. Prog. Phys. 80(2017) 056301

1. Particle Physics vs. Nuclear Physics



Particle physics (neutrino physics) Interactions are classified in Q^2 (4momentum transfer) and v (energy transfer) or W^2 (invariant mass)

katc

Nuclear physics

Interactions are classified in q (3-momnetum transfer) and ω (energy transfer)





1. Neutrino cross-section formula

Cross-section

- product of Leptonic and Hadronic tensor

$$d\sigma \sim L^{\mu\nu}W_{\mu\nu}$$



Hadronic tensor \rightarrow nuclear physics (hard)





1. Neutrino cross-section formula

Cross-section

- product of Leptonic and Hadronic tensor

$$d\sigma \sim L^{\mu\nu}W_{\mu\nu}$$

Leptonic tensor → the Standard Model (easy)

Hadronic tensor → nuclear physics (hard)

All complication of neutrino cross-section is how to model the hadronic tensor part





2. Charged Current Quasi-Elastic scattering (CCQE)

The simplest and the most abundant interaction around ~1 GeV.

$$v_{\mu} + n \rightarrow p + \mu^{-} \quad (v_{\mu} + X \rightarrow X' + \mu^{-})$$

 $d\sigma \sim L_{\mu\nu}T^{\mu\nu}$ $L_{\mu\nu} \sim J_{\mu}J_{\nu}$: Lepton tensor $W_{\mu\nu} = \int f(\vec{k}, \vec{q}, \omega)T_{\mu\nu}dE$: hadronic tensor $f(\vec{k}, \vec{q}, \omega)$: nucleon phase space $T_{\mu\nu} = T_{\mu\nu}(F_1, F_2, F_A, F_P)$: form factors

Form factors can be parameterized with dipole form

$$F(Q^2) = \frac{g}{\left(1 + \frac{Q^2}{M^2}\right)^2}$$





Quasi Elastic

2. Form factors







cosθ

2. Charged Current Quasi-Elastic scattering (CCQE)

The simplest and the most abundant interaction around ~1 GeV.

$$v_{\mu} + n \rightarrow p + \mu^{-} \quad (v_{\mu} + X \rightarrow X' + \mu^{-})$$

Neutrino energy is reconstructed from the observed lepton kinematics "QE assumption"

n

X

D

- 1. assuming neutron at rest
- 2. assuming interaction is CCQE

Neutrinos hit nucleons inside of nucleus, and the energy reconstruction is possible only with QE assumption

v-beam







Quasi Elastic

 $E_{\nu}^{QE} = \frac{ME_{\nu} - 0.5m_{\mu}^2}{M - E_{\mu} + p_{\mu}cos\theta}$

2. Nucleon correlations

2-particle 2-hole (2p2h) effect

- Mimic CCQE interaction, significant change cross section (both shape and normalization)
- The biggest topic in nuxsec community (T2K, NOvA, MINERvA, MicroBooNE)

An explanation of this puzzle







Martini et al, PRC80(2009)065501 NOvA, EPJC80,1119(2020)

2. Nucleon correlations

2-particle 2-hole (2p2h) effect

- Mimic CCQE interaction, significant change cross section (both shape and normalization)
- The biggest topic in nuxsec community (T2K, NOvA, MINERvA, MicroBooNE)
- 2p2h models in generators don't describe data well?
- High resolution detector (LArTPC, emulsion, etc) can find what is going on?





Smith and Moniz, NPB43(1972)605 Khachatryan et al., Nature 599(2021)565

2. Fermi motion

Quasi Elastic v_l u^+ v_r $v_$

Fermi motion

- Measured energy is smeared from the true energy if you assume nucleon at rest
- High resolution detector can measure all outgoing hadrons
 - \rightarrow initial nucleon momentum can be reconstructed (no Fermi motion smearing)



katori@fnal.gov

Pauli blocking

- Low momentum transfer reaction is forbidden.
- data show more suppression than what Pauli blocking can \rightarrow RPA(?)
- In the global Fermi gas model, Pauli blocking looks unphysical



Smith and Moniz, NPB43(1972)605 MiniBooNE, PRD81(2010)092005 **2. Pauli blocking**



Smith and Moniz, NPB43(1972)605 Bodek and Cai, EPJC79(2019)293

2. Nuclear Shell structure and binding energy

Binding energy ~ unobserved energy

- Energy to cost to release 1 nucleon, not constant
- Separation energy + excitation energy + recoil energy
 - Separation energy: energy to release 1 nucleon from the shell (~15 MeV, depends)
 - Excitation energy: energy used to excite leftover target nucleus (~1 MeV)
 - Recoil energy: kinetic energy of recoil target nucleus (~2-3 MeV)







Quasi Elastic

 W^+

2. Final state interaction

Cascade model

- Elastic scattering: Nucleon elastic scattering, pion elastic scattering
- Inelastic scattering: Nucleon inelastic scattering, pion inelastic scattering
- Charge exchange: Nucleon charge exchange, pion charge exchange
- Absorption: Nucleon absorption, pion absorption





3. Neutrino Baryonic resonance data

Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation





MiniBooNE π° momentum vs simulation



3. Neutrino Baryonic resonance data

RESonance

 W^+



- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation





MiniBooNE π° momentum vs simulation



3. Neutrino Baryonic resonance data

RESonance



Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation







3. Neutrino Baryonic resonance data

v_l____

RESonance

 W^+

Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation





All neutrino baryonic resonance processes have ~30% errors

3. pion production global fit

MINERvA pion data



- $\nu_{\mu}CC\pi^{\pm}$, low Q2 suppression, over-predicted
- $\nu_{\mu}CC\pi^{0}$, strong low Q2 suppression
- $\bar{\nu}_{\mu}CC\pi^{-}$, no low Q2 suppression
- $\bar{\nu}_{\mu}CC\pi^{0}$, low Q2 suppression, under-predicted

The study relies of available knobs in the simulation

It looks the simulation doesn't have good knobs to tune or missing





4. Shallow- and Deep-Inelastic Scattering (SIS and DIS)

Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low Q², low W DIS)
- Nuclear dependent DIS







Neutrino experiment around 1-10 GeV is not quite DIS ye

4. Higher baryonic resonances

Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low Q², low W DIS)
- Nuclear dependent DIS

DCC model

- Total amplitude is conserved
- Channels are coupled (πN , $\pi \pi N$, etc)
- 2 pion productions ~10% at 2 GeV







2

Bodek and Yang, AIP.Conf.Proc.670(2003)110, Nucl.Phys.B(Proc.Suppl.)139(2005)11

4. Quark-Hadron duality

Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low Q², low W DIS)
- Nuclear dependent DIS

GRV98 LO PDF + Bodek-Yang correction

- GRV98 for low Q² DIS
- Bodek-Yang correction for QH-duality
- 20 years old, out-of-dated

- not sure how to implement systematic errors

katori@





Nachtmann $\xi = \frac{2x}{\left(1 + \sqrt{1 + \frac{4x^2M^2}{Q^2}}\right)}$



Proton F2 function GRV98-BY correction vs. data



HKN,PRC76(2007)065207, EPS,JHEP04(2009)065, FSSZ,PRD85(2012)074028 nCTEQ, PRD80(2009)094004

4. Nuclear dependent DIS



Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low Q², low W DIS)
- Nuclear dependent DIS

Nuclear PDF

- Shadowing, EMC effect, Fermi motion
- Likely due to nucleon dynamics in nucleus
- Various models describe charged lepton data
- Neutrino data look very different





Conclusion

v-N scattering : important reactions for long baseline neutrino oscillation experiment (T2K, NOvA, DUNE, Hyper-Kamiokande, etc)

CCQE: charged-current quasi-elastic, around 1 GeV RES: baryonic resonance, around 2 GeV DIS: deep inelastic scattering, 3 GeV to higher

Nuclear physics sucks

- Fermi motion: nucleon motion smears kinematic reconstruction
- Pauli blocking: It limits low momentum transfer reaction
- Nuclear shell structure: separation energy (missing energy) for different nucleons
- Final state interaction: RES looks like CCQE, DIS looks like RES, etc
- Nucleon correlation: Physics between v-N and v-A interaction
- Quark-Hadron duality: Physics between v-q and v-N interaction
- Nuclear dependent PDF: Physics between v-q and v-A interaction

Currently, ~30% error is acceptable for many processes

References (books)

Quarks and Leptons (Halzen and Martin)

- show many calculations
- solutions for all exercises

Weak interactions of Leptons and Quarks (Commins and Bucksbaum)

- show details of weak interaction calculations
- too many typos

Physics of Neutrinos (Fukugita and Yanagida)

- very intense

- from solar neutrinos to SUSY

Neutrino astrophysics (Bahcall)

- good book to read

Foundation of Nuclear and Particle Physics (2017) - Authors: Donnelly, Formaggio, Holstein, Milner, Surrow - buy if your PhD thesis topic is about neutrino cross section measurements in T2K, NOvA, SBN, etc

The Physics of Neutrino interactions (2020)

- Authors: Sajjad Athar, Singh
- The newest book in this kind (970 pages!)





References (papers)

"From eV to EeV: Neutrino cross sections across energy scales"

- Authors: Formaggio and Zeller (MicroBooNE spokesperson)
- Rev.Mod.Phys.84(2012)1307, https://arxiv.org/abs/1305.7513
- very good summary of neutrino cross sections

"Neutrino-Nucleus Cross Sections for Oscillation Experiments"

- Authors: Katori (me) and Martini (Martini model)
- J.Phys. G45 (2018) no.1, 013001, https://arxiv.org/abs/1611.07770
- A review both theoretical and experimental views

"NuSTEC White Paper: Status and challenges of neutrino-nucleus scattering"

- NuSTEC (Neutrino Scattering Theory-Experiment Collaboration)
- Prog.Part.Nucl.Phys. 100 (2018) 1-68, https://arxiv.org/abs/1706.03621
- Cover all open issues in the community

"NuSTEC News"

- http://nustec.fnal.gov/
- subscribe mailing list, "like" facebook page, use #nuxsec





Backup





Neutrino energy is reconstructed from the observed lepton kinematics "QE assumption"

- 1. assuming neutron at rest
- 2. assuming interaction is CCQE

40m



ν

- Big and dense, to maximize interaction rate

- Coarsely instrumented, to minimize cost

(not great detector to measure hadrons)

Typical neutrino oscillation detector

3. non-QE background (resonance pion production)

non-QE background \rightarrow shift spectrum



Typical neutrino oscillation detector

- Big and dense, to maximize interaction rate
- Coarsely instrumented, to minimize cost

(not great detector to measure hadrons)



RESonance

w+

3. non-QE background (resonance pion production)

non-QE background \rightarrow shift spectrum



Typical neutrino oscillation detector

- Big and dense, to maximize interaction rate
- Coarsely instrumented, to minimize cost

(not great detector to measure hadrons)



RESonance

3. non-QE background (resonance pion production)

non-QE background \rightarrow shift spectrum





RESonance

 W^+

RESonance Coloma et al, PRL111(2013)221802 Mosel et al, PRL112(2014)151802 3. non-QE background (resonance pion production) W^+ Λ^{++} DUNE true vs. reconstructed Ev spectrum Pion production for v_{μ} $\partial_{CP} = +\pi/2$ disappearance search 0.02 0π - Source of mis-reconstruction of 0.015 neutrino energy Event distribution/A (10⁻³⁸ cm²/GeV) pion absorption 0.01 μ 0.005 Ζ $\delta_{CP} = -\pi/2$ Ν Ν 0 0.02 Neutral pion production in v_e $0\pi + 1p + Xn$ appearance search 0.015 - Source of misID of electron 0.01 $NC\pi^{o}$ + asymmetric decay 0.005 πο Ζ 2 3 5 6 Ν Ν E, (GeV)



Understanding of neutrino baryonic resonance meson production is important for oscillation experiments