Neutrino Interaction Physics

Lecture 1: Introduction of neutrino interactions

- 1. Overview
- 2. Neutrino lepton scattering
- 3. Neutrino quark scattering (DIS)
- 4. Neutrino nucleus reactions

Lecture 2: Neutrino interactions for long baseline oscillation experiments

- 1. Overview
- 2. CCQE interaction
- 3. Baryonic resonances
- 4. Shallow inelastic scattering (SIS)

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Formaggio and Zeller, Rev.Mod.Phys.,84 (2012) 1307

1. From eV to EeV: Neutrino cross sections across energy scales



1. From eV to EeV: Neutrino cross sections across energy scales



1. Scattering measurements

Size of wave packet ~ momentum transfer (~energy) $\hbar c = 197 MeV \cdot fm \rightarrow 200 \text{ MeV} \sim 1 \text{ fm} \text{ (size of nucleon)}$





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Lecture 1: Introduction of neutrino interactions

- 1. Overview
- 2. Neutrino lepton scattering (Standard Model)
- 3. Neutrino quark scattering (v-q scattering)
- 4. Neutrino nucleus reactions (v-A scattering)

Lecture 2: Neutrino interactions for long baseline oscillation experiments (v-N scattering)

- 1. Overview
- 2. CCQE interaction
- 3. Baryonic resonances
- 4. Shallow inelastic scattering



2. Neutrino-electron scattering

Neutrino – electron differential cross section

T=recoil electron kinetic energy
$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[c_L^2 + c_R^2 \left(\frac{E-T}{E} \right)^2 - C_L C_R \frac{m_e T}{E^2} \right]$$

Neutrino – electron differential cross section with neutrino magnetic moment $(\mu_{\nu} < 3x10^{-11} \mu_{\rm B})$ $\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[c_L^2 + c_R^2 \left(\frac{E-T}{E}\right)^2 - C_L C_R \frac{m_e T}{E^2} \right] + \frac{\pi \alpha \mu_{\nu}^2}{m_e^2} \left(\frac{1}{T} - \frac{1}{E}\right)$

Lepton-only process (pure Standard Model) is often used to test new physics

	CL	C _R
v _e - e⁻	$\frac{1}{2}$ +sin ² θ_{w}	$sin^2 \theta_w$
v_e - e⁻	$sin^2 \theta_w$	$\frac{1}{2}$ +sin ² θ_{w}
ν _μ - e⁻	$-\frac{1}{2}+\sin^2\theta_w$	$sin^2 \theta_w$
$\overline{ u_{\mu}}$ - e-	$sin^2 \theta_w$	$-\frac{1}{2}+\sin^2\theta_w$



Lee, PhD thesis, Virginia Tech (2001)

2. v-l scattering 3. v-q scattering 4. v-A reaction

2. Time dependence of muon decay Michel parameter ρ





3. Neutrino-DIS cross section

Neutrino – single d-quark cross section

$$\frac{d\sigma}{dy}(\nu d \to \mu u) = \frac{G_F^2 x s}{\pi}$$

Neutrino – d-quark cross section

$$\frac{d\sigma}{dy}(\nu d \to \mu u) = \int_0^1 \frac{G_F^2 x s}{\pi} d(x) dx$$

Neutrino-nucleon DIS cross section

$$\frac{d\sigma}{dy}(\nu N \to \mu X) = \int_0^1 \frac{G_F^2 x s}{\pi} [(d(x) + s(x) \dots) + [\bar{u}(x) + \bar{c}(x) \dots](1 - y)^2] dx$$

Neutrino-nucleus DIS cross section with isoscalar assumption

$$\frac{d\sigma}{dy}(vA \to \mu X) = A \int_0^1 \frac{G_F^2 xs}{\pi} [Q(x) + \bar{Q}(x)(1-y)^2] dx$$
$$u^p(x) + u^n(x) = d^n(x) + d^p(x) = u(x) + d(x) \equiv Q(x)$$
$$\bar{u}^p(x) + \bar{u}^n(x) = \bar{u}^n(x) + \bar{u}^p(x) = \bar{u}(x) + \bar{d}(x) \equiv \bar{Q}(x)$$



IceCube, PRD104(2021)022002

2. v-l scattering3. v-q scattering4. v-A reaction

3. Astrophysical high-energy neutrino measurement

Data and MC agree up to \sim PeV. \rightarrow We more or less understand neutrino interactions up to \sim PeV.







2. v-l scattering 3. v-q scattering 4. v-A reaction

3. Neutrino DIS saturation









Dziewonski, Anderson (PREM), Phys. Earth Planet.Inter.25,(1981)297 Donini, Palomares-Ruiz, Salvado, Nature Physics 15(2019)37

3. Earth tomography

Earth absorption for Earth density measurement

- PREM (Preliminary reference Earth model)
- Standard earth density model used by T2K, NOvA, etc
- Earth density profile is extracted by assuming flux and cross section
- Measure Earth moment of inertia and Earth mass by neutrinos







2. v-l scattering

3. v-q scattering 4. v-A reaction

3. Glashow resonance



A 5.9 PeV event in IceCube







Akindele (Neutrieno2020), <u>https://zenodo.org/record/3959532</u> SONGS, Journal of Applied Physics, 105(6), 064902 (2009)

4. Reactor neutrino

Low energy electron anti-neutrinos

- High-precision spectrum prediction
- Monitoring fission reactor









2. v-l scattering



GALLEX, PLB490(2000)16;SAGE, J.Expt.Theor.Phys.95(2002)181 Borexino, PRL 108(2012)051302

4. Solar neutrino

Gallium experiment

 $v_e + {^{71}Ga} \rightarrow e^- + {^{71}Ge}$

- Sensitive to pp-neutrino (0.42 MeV), 90% of total solar neutrino flux.

- Both experiments observed deficit, but higher than Homestake result

GALLEX N2 + GeCl4 GaCI, + HCI (54 m3, 110 t)



COHERENT, Science10.1126/science.aao0990 (2017).

4. Neutrino-Nucleus coherent scattering



v-l scattering
 v-q scattering
 v-A reaction

Conclusion

Neutrinos interact by weak force

v-I scattering : test of weak theory Neutrino-electron scattering Muon decay

v-q scattering : test of weak theory, test of quark model DIS cross sections Di-muon production Paschos-Wolfenstein ratio Astrophysical neutrinos

v-A scattering :

Reactor neutrino experiments Neutrino nuclear capture by CI and Ga, important for solar neutrinos Neutrino coherent scattering, important for supernova (2017)

v-N scattering : important reactions for long baseline neutrino oscillation experiment (T2K, NOvA, DUNE, Hyper-Kamiokande)

1. From eV to EeV: Neutrino cross sections across energy scales



Formaggio and Zeller, Rev.Mod.Phys.84(2012)1307

1. Next generation neutrino oscillation experiments

Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE



1. Next generation neutrino oscillation experiments

Accelerator-based neutrino oscillation experiments

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1. Next generation neutrino oscillation experiments

Accelerator-based neutrino oscillation experiments

- Present to Future: T2K, NOvA, Hyper-Kamiokande, DUNE...

Most of data are from muon neutrino beam

- create by π -DIF, K-DIF (pion and kaon decay-in-flight)
- $\Phi(\nu_{\mu}) > \Phi(\bar{\nu}_{\mu})$: more π^+ and K⁺ than π^- and K⁻ (for low energy)
- $\mu\text{-}\text{decay}$ can make electro-neutrinos but they are background
- δ_{CP} study need electro-neutrino and antineutrino cross-sections (v_e appearance)

Nuclear physics sucks

- Simple extrapolation may be broken due to nuclear physics
- We are not good at nuclear physics because we are not nuclear physicists
- Nuclear physics = non-perturbative QCD (many models, no theory)
- Particle physics is developed by avoiding nuclear physics...



 ${}_{k}P_{\mu\to e}(L/E) = \sin^{2}2\theta\sin^{2}\left(1.27\Delta m^{2}(eV^{2})\frac{L(km)}{E(GeV^{2})}\right)$

Benhar, Day, Sick, Rev. Mod. Phys. 80(2008) 189 Nakamura et a;, Rep. Prog. Phys. 80(2017) 056301

1. Particle Physics vs. Nuclear Physics



Particle physics (neutrino physics) Interactions are classified in Q^2 (4momentum transfer) and v (energy transfer) or W^2 (invariant mass)

katc

Nuclear physics

Interactions are classified in q (3-momnetum transfer) and ω (energy transfer)





1. Neutrino cross-section formula

Cross-section

- product of Leptonic and Hadronic tensor

$$d\sigma \sim L^{\mu\nu}W_{\mu\nu}$$



Hadronic tensor → nuclear physics (hard)





1. Neutrino cross-section formula

Cross-section

- product of Leptonic and Hadronic tensor

$$d\sigma \sim L^{\mu\nu}W_{\mu\nu}$$

Leptonic tensor → the Standard Model (easy)

Hadronic tensor → nuclear physics (hard)

All complication of neutrino cross-section is how to model the hadronic tensor part





2. Charged Current Quasi-Elastic scattering (CCQE)

The simplest and the most abundant interaction around ~1 GeV.

$$v_{\mu} + n \rightarrow p + \mu^{-} \quad (v_{\mu} + X \rightarrow X' + \mu^{-})$$

 $d\sigma \sim L_{\mu\nu}T^{\mu\nu}$ $L_{\mu\nu} \sim J_{\mu}J_{\nu}$: Lepton tensor $W_{\mu\nu} = \int f(\vec{k}, \vec{q}, \omega)T_{\mu\nu}dE$: hadronic tensor $f(\vec{k}, \vec{q}, \omega)$: nucleon phase space $T_{\mu\nu} = T_{\mu\nu}(F_1, F_2, F_A, F_P)$: form factors

Form factors can be parameterized with dipole form

$$F(Q^2) = \frac{g}{\left(1 + \frac{Q^2}{M^2}\right)^2}$$





Quasi Elastic

W⁺

p

2. Form factors





cosθ

2. Charged Current Quasi-Elastic scattering (CCQE)

The simplest and the most abundant interaction around ~1 GeV.

$$v_{\mu} + n \rightarrow p + \mu^{-} \quad (v_{\mu} + X \rightarrow X' + \mu^{-})$$

Neutrino energy is reconstructed from the observed lepton kinematics "QE assumption"

n

X

D

- 1. assuming neutron at rest
- 2. assuming interaction is CCQE

Neutrinos hit nucleons inside of nucleus, and the energy reconstruction is possible only with QE assumption

v-beam









2. Nucleon correlations

2-particle 2-hole (2p2h) effect

- Mimic CCQE interaction, significant change cross section (both shape and normalization)
- The biggest topic in nuxsec community (T2K, NOvA, MINERvA, MicroBooNE)

An explanation of this puzzle







Martini et al, PRC80(2009)065501 NOvA, EPJC80,1119(2020)

2. Nucleon correlations

2-particle 2-hole (2p2h) effect

- Mimic CCQE interaction, significant change cross section (both shape and normalization)
- The biggest topic in nuxsec community (T2K, NOvA, MINERvA, MicroBooNE)
- 2p2h models in generators don't describe data well?
- High resolution detector (LArTPC, emulsion, etc) can find what is going on?





Smith and Moniz, NPB43(1972)605 Ashkenazi (Neutrino 2020), https://zenodo.org/record/3959538

2. Fermi motion

Fermi motion

- Measured energy is smeared from the true energy if you assume nucleon at rest
- High resolution detector can measure all outgoing hadrons
 - \rightarrow initial nucleon momentum can be reconstructed (no Fermi motion smearing)





Cherenkov detectors: Assuming QE interaction Using lepton only $2M\epsilon + 2ME_l - m_l^2$

$$E_{QE} = \frac{2MC + 2ML_l - m_l}{2(M - E_l + |k_l| \cos \theta_l)}$$



Quasi Elastic

w+

р

Tracking detectors: Calorimetric sum Using All detected particles

 $E_{\rm cal} = E_l + E_p^{\rm kin} + \epsilon$ ^[1p0 π]



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MiniBooNE, PRD81(2010)092005 2. Pauli blocking

Smith and Moniz, NPB43(1972)605

Pauli blocking

- Low momentum transfer reaction is forbidden.
- data show more suppression than what Pauli blocking can \rightarrow RPA(?)
- In the global Fermi gas model, Pauli blocking looks unphysical





Smith and Moniz, NPB43(1972)605 Bodek and Cai, EPJC79(2019)293

2. Nuclear Shell structure and binding energy

Binding energy ~ unobserved energy

- Energy to cost to release 1 nucleon, not constant
- Separation energy + excitation energy + recoil energy
 - Separation energy: energy to release 1 nucleon from the shell (~15 MeV, depends)
 - Excitation energy: energy used to excite leftover target nucleus (~1 MeV)
 - Recoil energy: kinetic energy of recoil target nucleus (~2-3 MeV)





Quasi Elastic

 W^+



Neutrino energy is reconstructed from the observed lepton kinematics

- "QE assumption"
- 1. assuming neutron at rest
- 2. assuming interaction is CCQE

Typical neutrino oscillation detector

- Big and dense, to maximize interaction rate
- Coarsely instrumented, to minimize cost (not great detector to measure hadrons)



Signal

ν

3. non-QE background (resonance pion production)

non-QE background \rightarrow shift spectrum



Typical neutrino oscillation detector

- Big and dense, to maximize interaction rate
- Coarsely instrumented, to minimize cost

(not great detector to measure hadrons)



RESonance

 W^+

3. non-QE background (resonance pion production) non-QE background \rightarrow shift spectrum



Typical neutrino oscillation detector

- Big and dense, to maximize interaction rate
- Coarsely instrumented, to minimize cost

(not great detector to measure hadrons)



RESonance

3. non-QE background (resonance pion production)

non-QE background \rightarrow shift spectrum





RESonance

 W^+

RESonance Coloma et al, PRL111(2013)221802 Mosel et al, PRL112(2014)151802 3. non-QE background (resonance pion production) W^+ Λ^{++} DUNE true vs. reconstructed Ev spectrum Pion production for v_{μ} 111111 __{∂CP}=+π/2 disappearance search 0.02 0π - Source of mis-reconstruction of 0.015 neutrino energy Event distribution/A (10⁻³⁸ cm²/GeV) pion absorption 0.01 μ 0.005 Ζ $\delta_{CP} = -\pi/2$ Ν Ν 0 0.02 $0\pi + 1p + Xn$ Neutral pion production in v_e appearance search 0.015 - Source of misID of electron 0.01 $NC\pi^{o}$ + asymmetric decay 0.005 πο Ζ 2 3 5 6 Ν Ν E, (GeV)



Understanding of neutrino baryonic resonance meson production is important for oscillation experiments

3. Final state interaction

Cascade model

- Elastic scattering: Nucleon elastic scattering, pion elastic scattering
- Inelastic scattering: Nucleon inelastic scattering, pion inelastic scattering
- Charge exchange: Nucleon charge exchange, pion charge exchange
- Absorption: Nucleon absorption, pion absorption





RESonance

3. Neutrino Baryonic resonance data

Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation





MiniBooNE π° momentum vs simulation





3. Neutrino Baryonic resonance data

RESonance



Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation





MiniBooNE π° momentum vs simulation



3. Neutrino Baryonic resonance data

RESonance



Final state interaction

- Cascade model as a standard of the community
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KING'S College LONDON

3. Neutrino Baryonic resonance data

v_l p Λ^+

RESonance

Final state interaction

- Cascade model as a standard of the community
- Advanced models are not available for event-by-event simulation





All neutrino baryonic resonance processes have ~30% errors

Nakamura et al,Rep.Prog.Phys.80(2017)056301

4. Shallow Inelastic Scattering (SIS)







4. Higher baryonic resonances

Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low Q², low W DIS)
- Nuclear dependent DIS

DCC model

- Total amplitude is conserved
- Channels are coupled (πN , $\pi \pi N$, etc)
- 2 pion productions ~10% at 2 GeV









Bodek and Yang, AIP.Conf.Proc.670(2003)110, Nucl.Phys.B(Proc.Suppl.)139(2005)11

4. Quark-Hadron duality

Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low Q², low W DIS)
- Nuclear dependent DIS

GRV98 LO PDF + Bodek-Yang correction

- GRV98 for low Q² DIS
- Bodek-Yang correction for QH-duality
- 20 years old, out-of-dated

- not sure how to implement systematic errors

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Nachtmann $\xi = \frac{2x}{\left(1 + \sqrt{1 + \frac{4x^2M^2}{Q^2}}\right)}$



Proton F2 function GRV98-BY correction vs. data



HKN,PRC76(2007)065207, EPS,JHEP04(2009)065, FSSZ,PRD85(2012)074028 nCTEQ, PRD80(2009)094004

4. Nuclear dependent DIS



Cross section

- Higher resonances and hadron dynamics
- Quark-Hadron duality (low Q², low W DIS)
- Nuclear dependent DIS

Nuclear PDF

- Shadowing, EMC effect, Fermi motion
- Likely due to nucleon dynamics in nucleus
- Various models describe charged lepton data
- Neutrino data look very different





Conclusion

v-N scattering : important reactions for long baseline neutrino oscillation experiment (T2K, NOvA, DUNE, Hyper-Kamiokande, etc)

CCQE: charged-current quasi-elastic, around 1 GeV RES: baryonic resonance, around 2 GeV DIS: deep inelastic scattering, 3 GeV to higher

Nuclear physics sucks

- Fermi motion: nucleon motion smears kinematic reconstruction
- Pauli blocking: It limits low momentum transfer reaction
- Nuclear shell structure: separation energy (missing energy) for different nucleons
- Baryonic resonance: Often misidentified as CCQE
- Final state interaction: RES looks like CCQE, DIS looks like RES, etc.
- Nucleon correlation: Physics between v-N and v-A interaction
- Quark-Hadron duality: Physics between v-q and v-N interaction
- Nuclear dependent PDF: Physics between v-q and v-A interaction

Currently, ~30% error is acceptable for many processes

References (books)

Quarks and Leptons (Halzen and Martin)

- show many calculations
- solutions for all exercises

Weak interactions of Leptons and Quarks (Commins and Bucksbaum)

- show details of weak interaction calculations
- too many typos

Physics of Neutrinos (Fukugita and Yanagida)

- very intense
- from solar neutrinos to SUSY

Neutrino astrophysics (Bahcall)

- good book to read

Foundation of Nuclear and Particle Physics (2017)

- Authors: Donnelly, Formaggio, Holstein, Milner, Surrow
- one and only one textbook on this subject

- buy if your PhD thesis topic is about neutrino cross section in T2K, NOvA, SBN, etc





References (papers)

"From eV to EeV: Neutrino cross sections across energy scales"

- Authors: Formaggio and Zeller (MicroBooNE spokesperson)
- Rev.Mod.Phys.84(2012)1307, https://arxiv.org/abs/1305.7513
- very good summary of neutrino cross sections

"Neutrino-Nucleus Cross Sections for Oscillation Experiments"

- Authors: Katori (me) and Martini (Martini model)
- J.Phys. G45 (2018) no.1, 013001, https://arxiv.org/abs/1611.07770
- A review both theoretical and experimental views

"NuSTEC White Paper: Status and challenges of neutrino-nucleus scattering"

- NuSTEC (Neutrino Scattering Theory-Experiment Collaboration)
- Prog.Part.Nucl.Phys. 100 (2018) 1-68, https://arxiv.org/abs/1706.03621
- Cover all open issues in the community

"NuSTEC News"

- http://nustec.fnal.gov/
- subscribe mailing list, "like" facebook page, use #nuxsec





Backup



3. Di-muon production



NuTeV, PRL88(2002)091802

3. Paschos-Wolfenstein ratio and NuTeV anomaly

