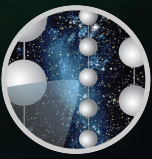


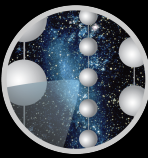
# Search for Quantum Gravity Using Astrophysical Neutrino Flavour



IceCube, ArXiv:2111.04654

Teppei Katori for the IceCube collaboration  
King's College London  
Snowmass21 Neutrino BSM Physics workshop,  
PITT PACC, Pittsburgh, Feb. 11, 2022

22/02/11



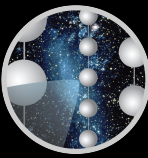
# High-energy astrophysical neutrino flavour

High-energy particles ( $>60$  TeV) propagating a long distance ( $>100$  Mpc)  
- Neutrinos can probe new physics in the universe



astrophysical  
neutrino





# High-energy astrophysical neutrino flavour

High-energy particles ( $>60$  TeV) propagating a long distance ( $>100$  Mpc)  
- Neutrinos can probe new physics in the universe

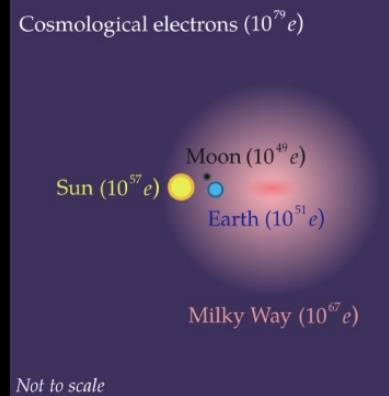
## Quantum foam

Ellis, Mavromatos, Nanopoulos  
PLB293(1992)37



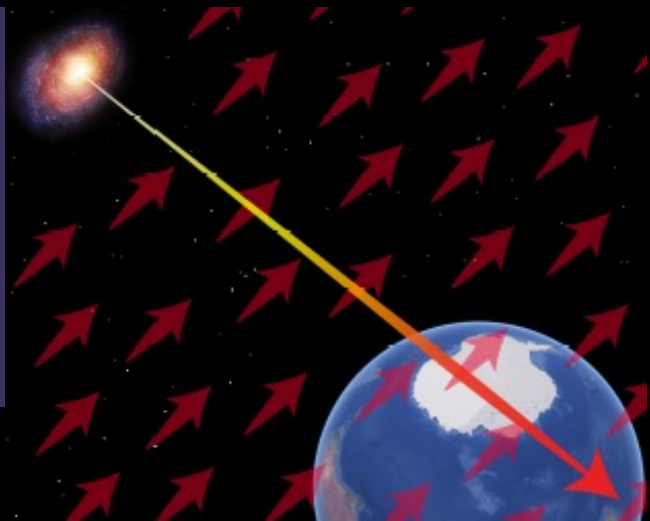
## new long-range force

Bustamante, Agarwalla  
PRL122(2019)061103



## Lorentz violating field

Kostelecký Mewes, PRD69(2004)016005

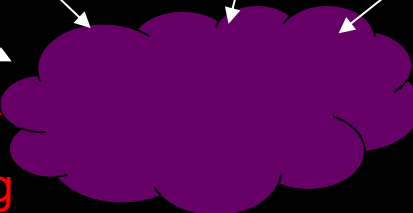


Klop, Ando  
PRD97(2018)063006

neutrino-dark energy  
coupling  
etc...



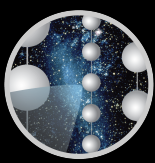
neutrino mixing



New physics

astrophysical  
neutrino





# Flavor new physics search with effective operators

Standard Model Extension (SME) is an effective field theory to look for Lorentz violation

$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu\psi + \bar{\psi}\gamma^\mu c_{\mu\nu}\partial^\nu\psi \dots$$

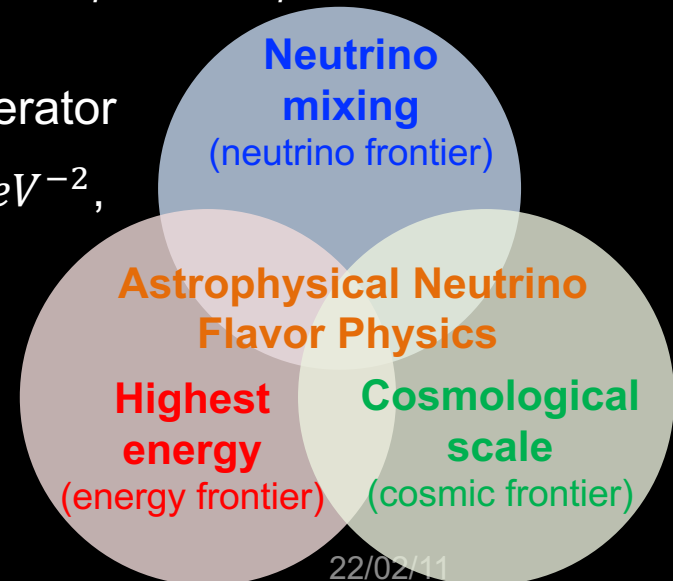
Standard Model     New physics

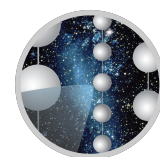
Effective Hamiltonian can be written from here

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} \dots$$

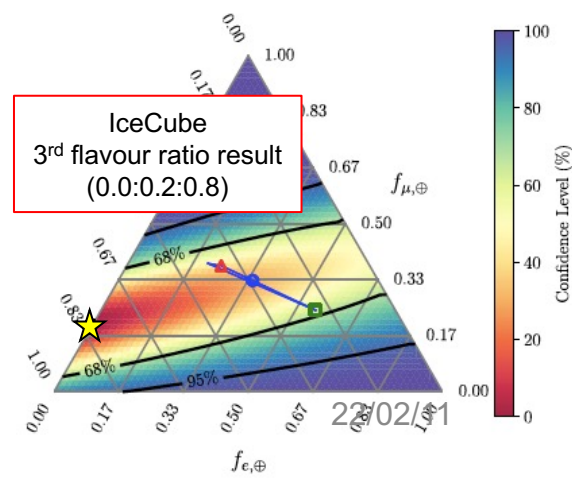
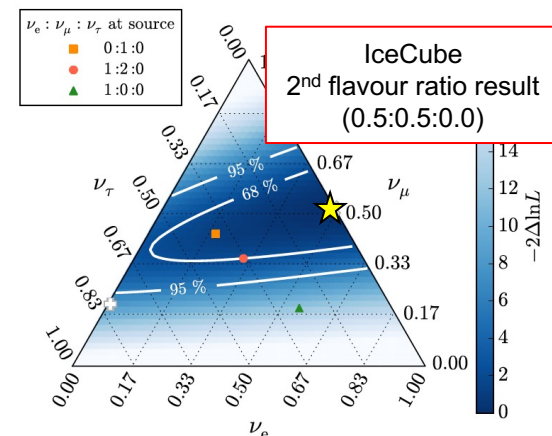
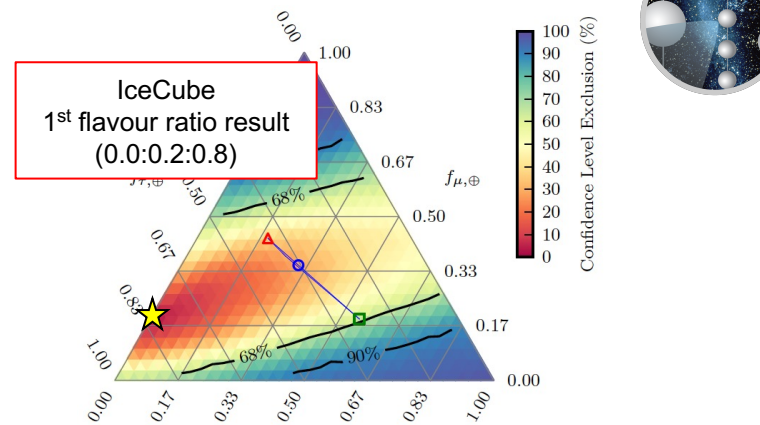
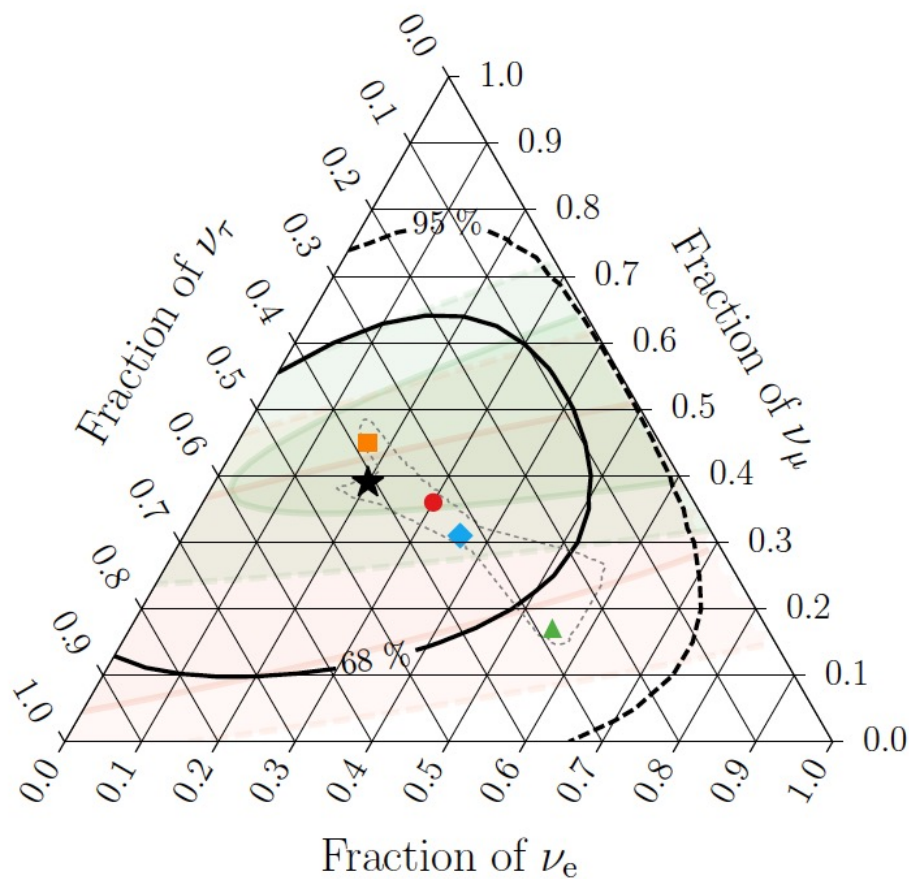
Standard Model     New physics (renormalizable)     higher dimension operator (non-renormalizable)

Astrophysical neutrino flavour sensitivity of dim-6 operator goes beyond the natural scale  $c^{(6)} \sim \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$ , first time in any known scientific system





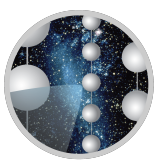
# HESE 7.5-yr flavor ratio (2018)



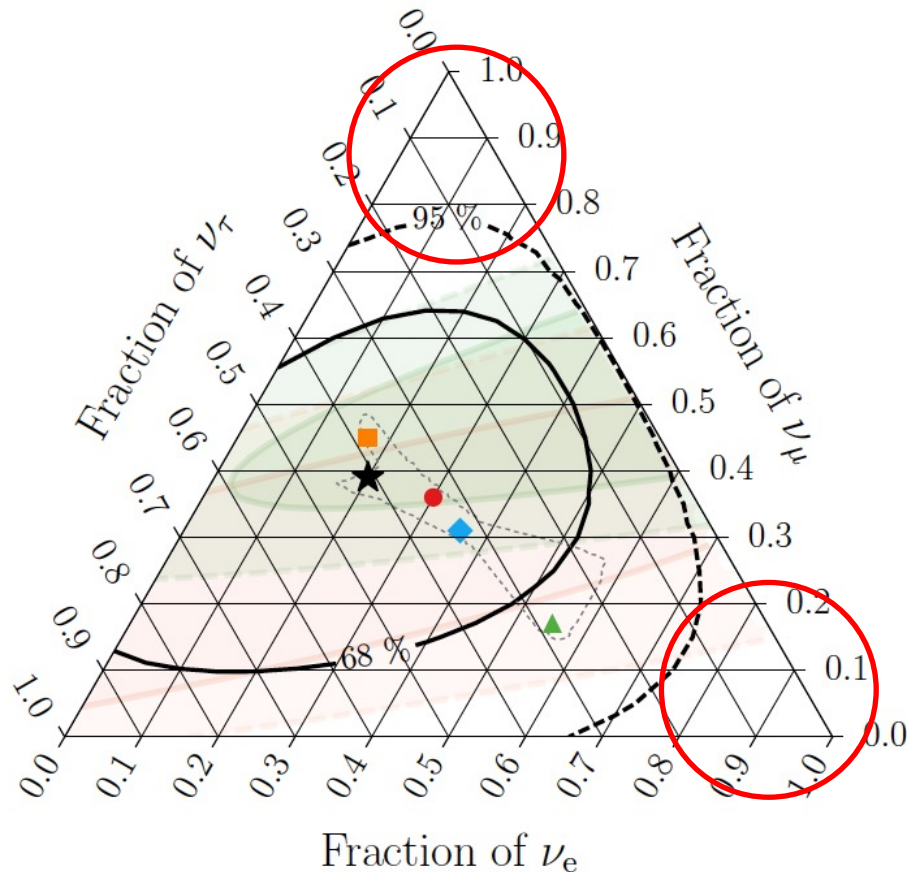
- HESE with ternary topology ID
- ★ Best fit: 0.20 : 0.39 : 0.42
- Global Fit (IceCube, APJ 2015)
- Inelasticity (IceCube, PRD 2019)
- ⋯⋯⋯  $3\nu$ -mixing  $3\sigma$  allowed region

$\nu_e : \nu_\mu : \nu_\tau$  at source → on Earth:

- 0:1:0 → 0.17 : 0.45 : 0.37
- 1:2:0 → 0.30 : 0.36 : 0.34
- ▲ 1:0:0 → 0.55 : 0.17 : 0.28
- ◆ 1:1:0 → 0.36 : 0.31 : 0.33



# HESE 7.5-yr flavor ratio (2018)



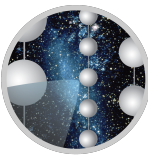
New HESE analysis included more comprehensive systematic errors

Likelihood includes tau PID, new flavour ratio result has some power to distinguish  $\nu_e$  and  $\nu_\tau$

Almost all flavour ratio is allowed from data, except regions near 2 corners

We can test scenarios which predict flavour ratio in those regions

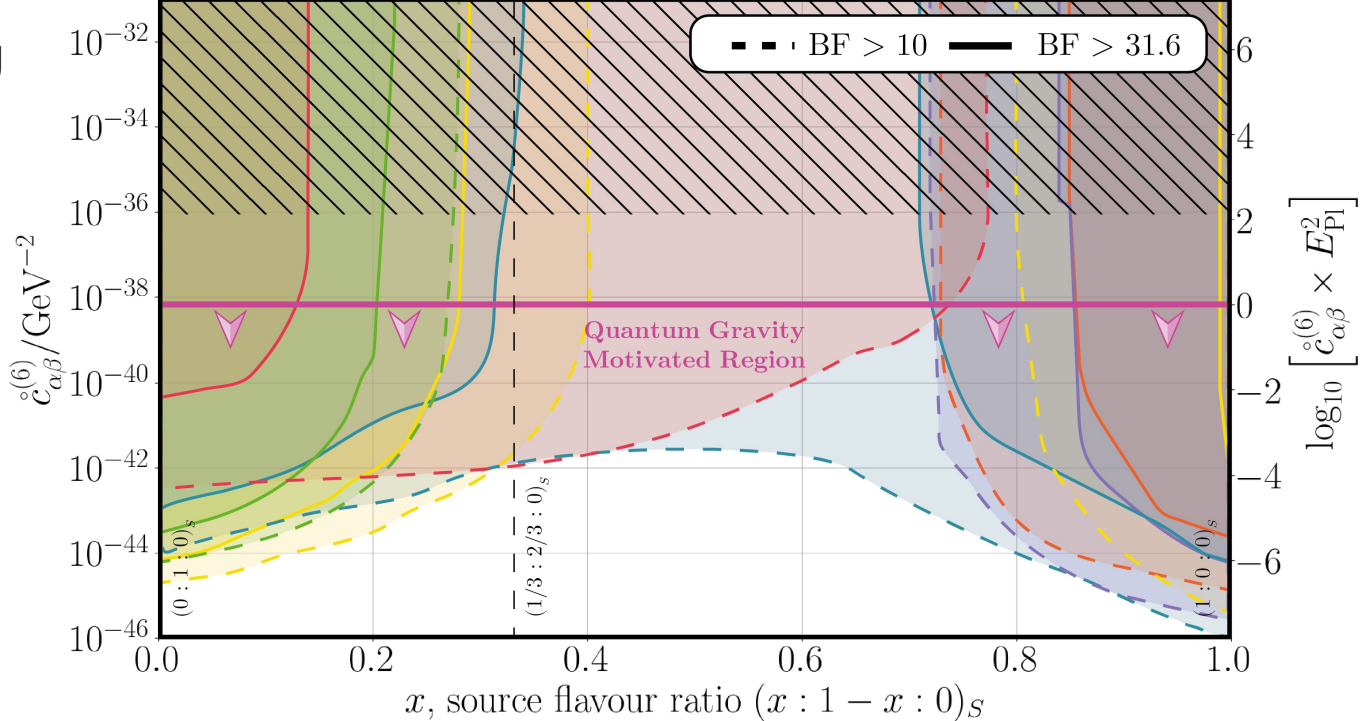
|   |   |  |
|---|---|--|
| — | HESE with ternary topology ID           | $\nu_e : \nu_\mu : \nu_\tau$ at source $\rightarrow$ on Earth: |
| ★ | Best fit: 0.20 : 0.39 : 0.42            | ■ 0:1:0 $\rightarrow$ 0.17 : 0.45 : 0.37                       |
| ■ | Global Fit (IceCube, APJ 2015)          | ● 1:2:0 $\rightarrow$ 0.30 : 0.36 : 0.34                       |
| ■ | Inelasticity (IceCube, PRD 2019)        | ▲ 1:0:0 $\rightarrow$ 0.55 : 0.17 : 0.28                       |
| ⋯ | $3\nu$ -mixing $3\sigma$ allowed region | ◆ 1:1:0 $\rightarrow$ 0.36 : 0.31 : 0.33                       |



# Search for Quantum Gravity Using Astrophysical Neutrino Flavour

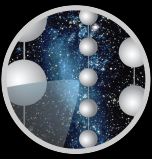
Strong limits for many parameters depending on assumed initial flavour ratio

- $a_{\alpha\beta}^{(3)} \sim 10^{-27} \text{ GeV}$
- $c_{\alpha\beta}^{(4)} \sim 10^{-33}$
- $a_{\alpha\beta}^{(5)} \sim 10^{-39} \text{ GeV}^{-1}$
- $c_{\alpha\beta}^{(6)} \sim 10^{-45} \text{ GeV}^{-2}$
- $a_{\alpha\beta}^{(7)} \sim 10^{-49} \text{ GeV}^{-3}$
- $c_{\alpha\beta}^{(8)} \sim 10^{-55} \text{ GeV}^{-4}$



But not many limits for standard flavour ratio  $(\nu_e : \nu_\mu : \nu_\tau) = (1/3 : 2/3 : 0)$

| New Physics (N.P.)  |  | Key   |  |
|---|--|---|--|
| <span style="color: orange;">—</span> $\text{Re}(c_{ee}^{(6)})$   | <span style="color: purple;">—</span> $\text{Re}(c_{\mu\tau}^{(6)})$ | $\text{Re}(c_{\mu\tau}^{(6)})$ atm. limit (90%) | <span style="color: pink;">—</span> $\log_{10}(c_{\alpha\beta}^{(6)} \times E_{Pl}^2) = 0$ |
| <span style="color: red;">—</span> $\text{Re}(c_{e\mu}^{(6)})$    | <span style="color: yellow;">—</span> $\text{Re}(c_{\mu\mu}^{(6)})$  |   |  |
| <span style="color: green;">—</span> $\text{Re}(c_{e\tau}^{(6)})$ | <span style="color: blue;">—</span> $\text{Re}(c_{\tau\tau}^{(6)})$  |   |  |



# Search for Quantum Gravity Using Astrophysical Neutrino Flavour – Next step

Does quantum gravity-motivated physics exist? Do we have new structure in vacuum and space-time? Say YES!

## 1. Better particle ID (IceCube)

Next generation tau PID will improve the flavour ratio measurement

## 2. Combined analysis (IceCube)

Maximize statistical power, constrain systematics from different samples

## 3. Astrophysical neutrino production model constraints (astrophysics)

New constraints on flavour structure, power spectrum, normalization will improve this analysis

## 4. More precise oscillation parameter measurements (oscillation physics)

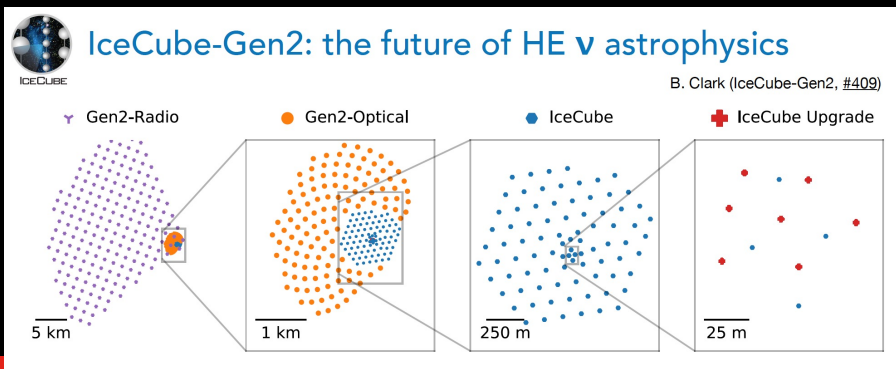
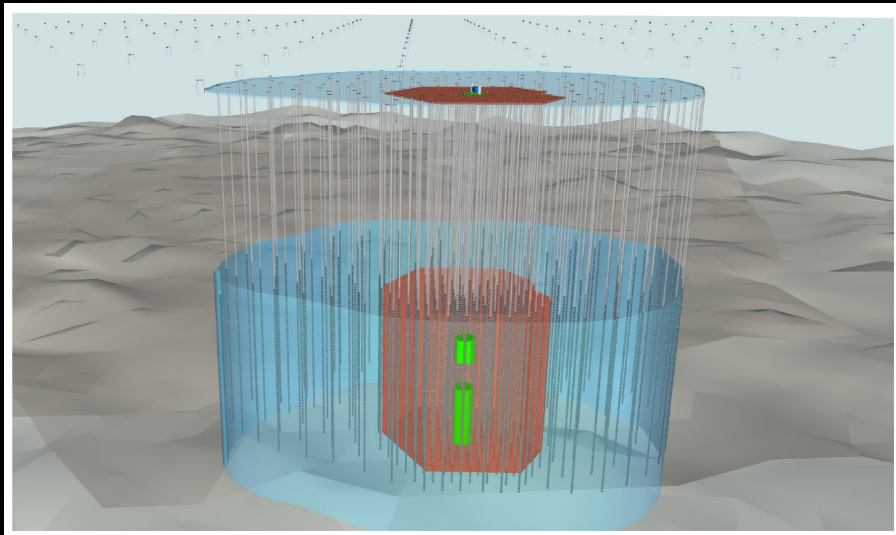
Smaller neutrino mass errors will improve this analysis

## 5. New experiments

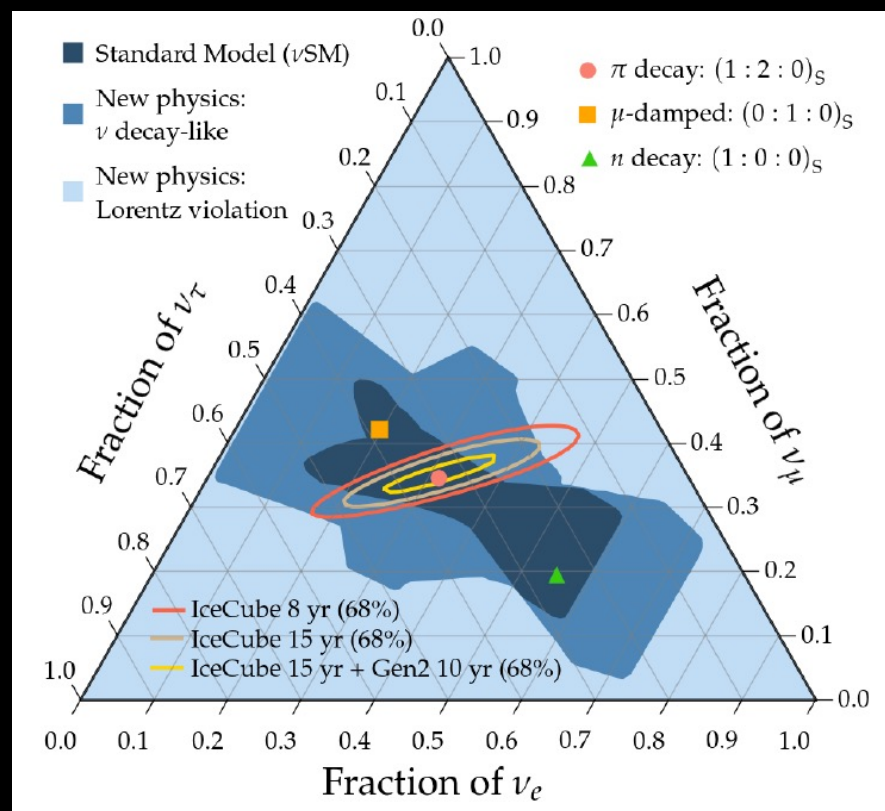




## IceCube-Gen2



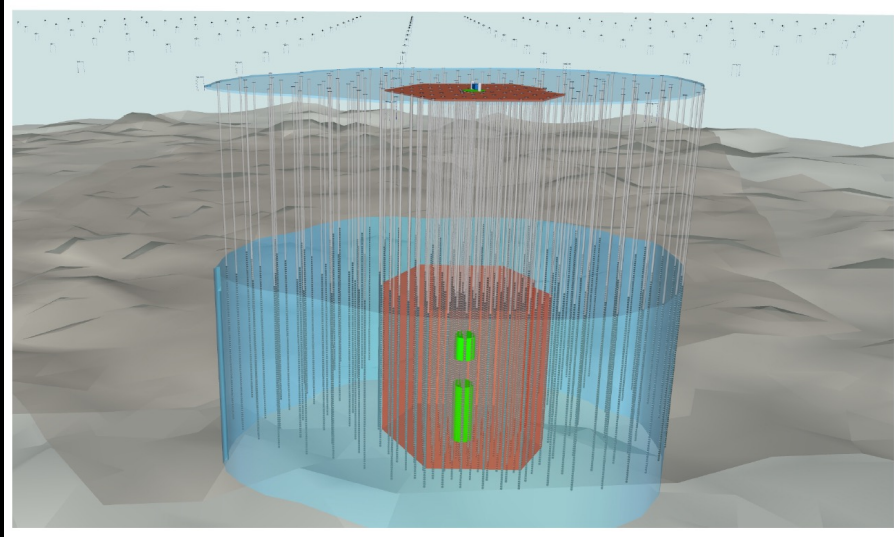
## IceCube-Gen2 flavour ratio sensitivity



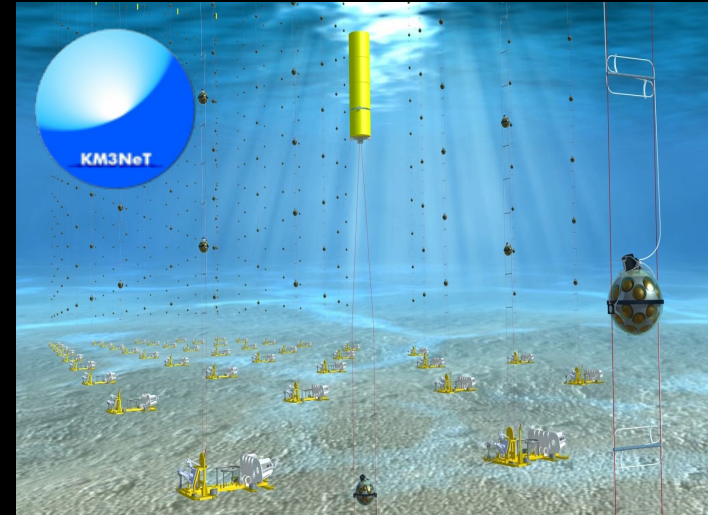


# Future HENTs (high-energy neutrino telescopes)

IceCube-Gen2

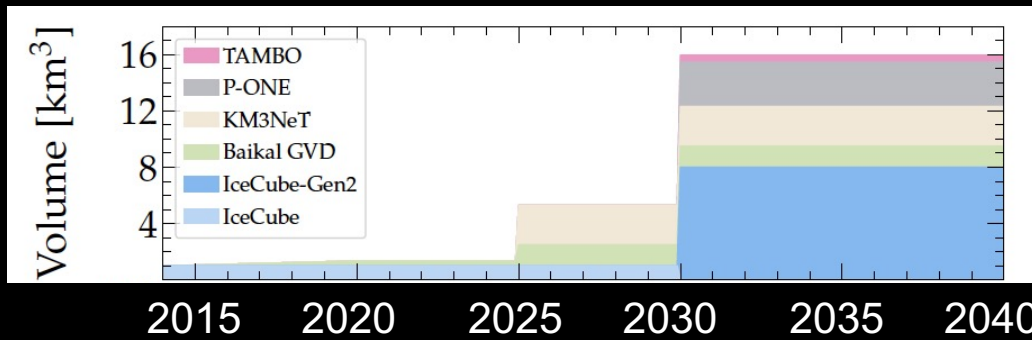
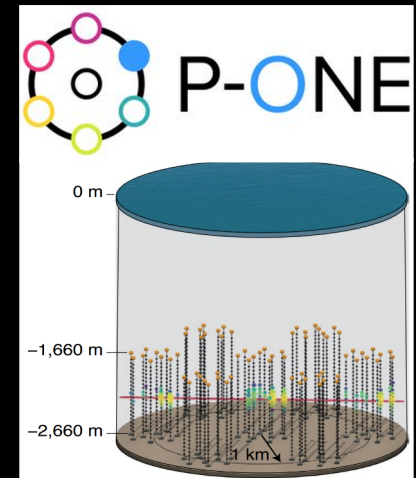


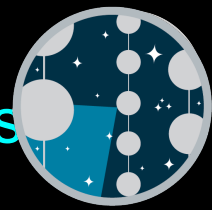
KM3NeT



GEN2

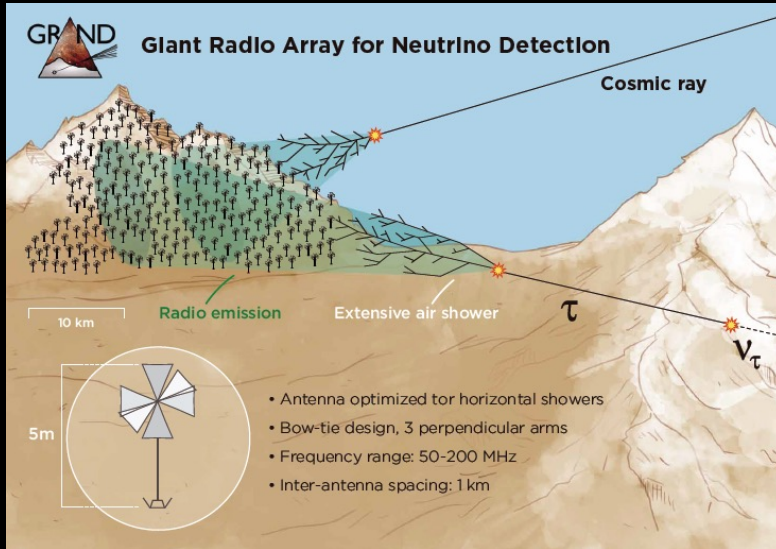
P-ONE



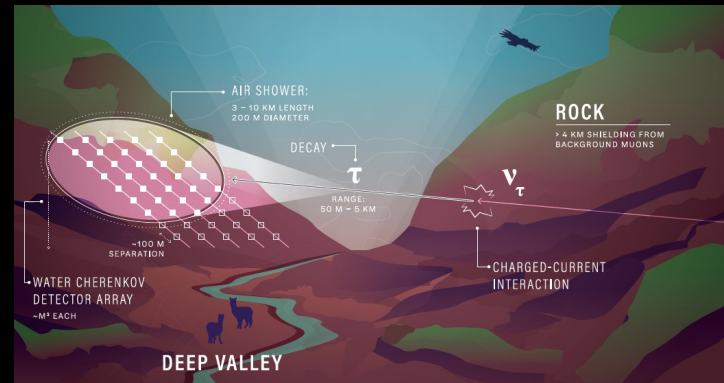


# Future EHENTs (extremely-high-energy neutrino telescopes)

## GRAND

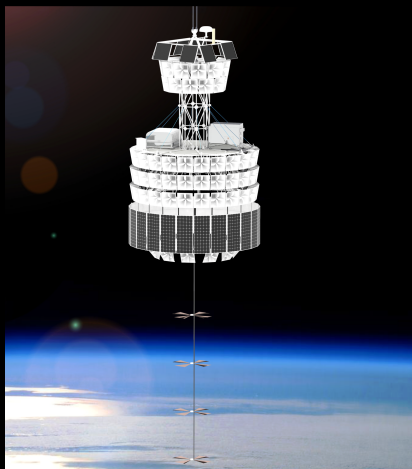


## TAMBO



## GEN2

## PUEO



| Energy Range          | Experiment           | Technology             | Detected Flavor                       | Ref.       |
|-----------------------|----------------------|------------------------|---------------------------------------|------------|
| < 10 <sup>3</sup> GeV | JUNO                 | Liquid scintillator    | All Flavors                           | [457]      |
| < 10 <sup>3</sup> GeV | DUNE                 | LRTPC                  | All Flavors                           | [366]      |
| < 10 <sup>3</sup> GeV | THEIA                | WbLS                   | All Flavors                           | [630]      |
| < 10 <sup>3</sup> GeV | WATCHMAN             | Gd-loaded Water C      | All Flavors                           | [631]      |
| < 10 <sup>3</sup> GeV | Super-Kamiokande     | Gd-loaded Water C      | All Flavors                           | [632]      |
| < 10 <sup>4</sup> GeV | Hyper-Kamiokande     | Water Cherenkov        | All Flavors                           | [459]      |
| < 10 <sup>5</sup> GeV | ANTARES              | Sea-Water Cherenkov    | ν <sub>μ</sub> , ν̄ <sub>μ</sub> (CC) | [633]      |
| < 10 <sup>6</sup> GeV | IceCube/IceCube-Gen2 | Ice Cherenkov          | All Flavors                           | [365, 415] |
| < 10 <sup>6</sup> GeV | KM3NeT               | Sea-Water Cherenkov    | All Flavors                           | [634]      |
| < 10 <sup>6</sup> GeV | Baikal-GVD           | Lake-Water Cherenkov   | All Flavors                           | [635]      |
| < 10 <sup>6</sup> GeV | P-ONE                | Sea-Water Cherenkov    | All Flavors                           | [636]      |
| 1 – 100 PeV           | TAMBO                | Earth-skimming WC      | ν <sub>τ</sub> , ν̄ <sub>τ</sub> (CC) | [637]      |
| > 1 PeV               | Trinity              | Earth-skimming Image   | ν <sub>τ</sub> , ν̄ <sub>τ</sub> (CC) | [638]      |
| > 10 PeV              | RET-N                | Radar echo             | All Flavors                           | [639]      |
| > 10 PeV              | IceCube-Gen2         | In-ice Radio           | All Flavors                           | [415]      |
| > 10 PeV              | ARIANNA-200          | On-ice Radio           | All Flavors                           | [640]      |
| > 20 PeV              | POEMMA               | Space Air-shower Image | ν <sub>τ</sub> , ν̄ <sub>τ</sub> (CC) | [641]      |
| > 100 PeV             | RNO-G                | In-ice Radio           | All Flavors                           | [642]      |
| > 100 PeV             | Auger/GCOS           | Earth-skimming WC      | ν <sub>τ</sub> , ν̄ <sub>τ</sub> (CC) | [643, 644] |
| > 100 PeV             | ANITA/PUEO           | Balloon Radio          | ν <sub>τ</sub> , ν̄ <sub>τ</sub> (CC) | [645, 646] |
| > 100 PeV             | Beacon               | Earth-skimming Radio   | ν <sub>τ</sub> , ν̄ <sub>τ</sub> (CC) | [647]      |
| > 100 PeV             | GRAND                | Earth-skimming Radio   | ν <sub>τ</sub> , ν̄ <sub>τ</sub> (CC) | [648]      |



ICECUBE  
GEN2

## Conclusion

Quantum gravity may create a new structure in vacuum.

Neutrino interferometry is a powerful technique to look for new physics.

Astrophysical neutrino mixing sensitivity reaches to naïve expectation of Planck scale physics.  
We need more statistics and better particle identification algorithm to find quantum gravity motivated physics.

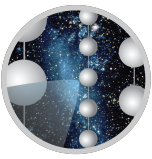
IceCube-Gen2 collaboration



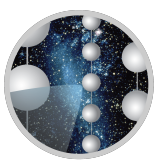
**Thank you for your attention!**

22/02/11

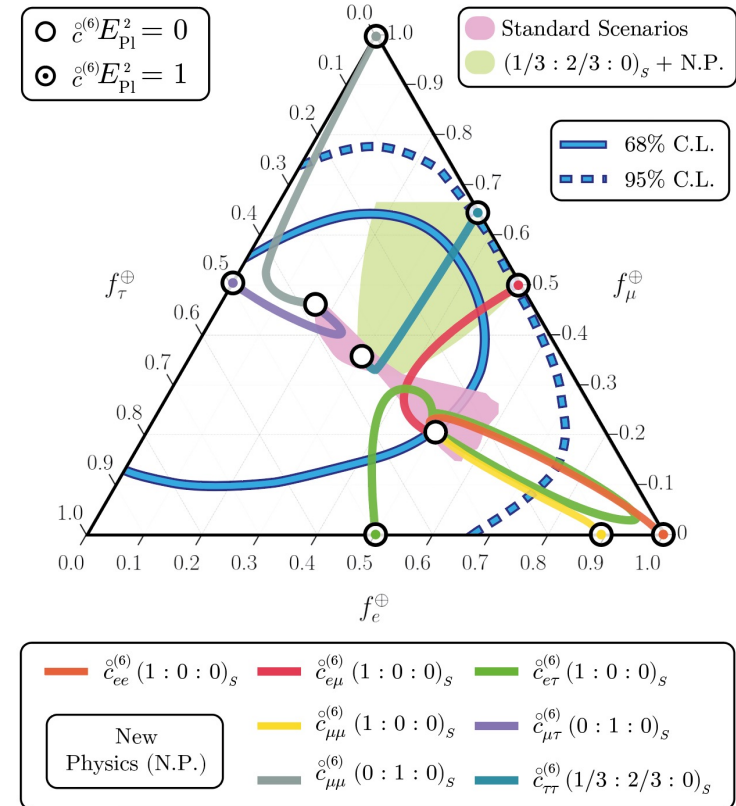
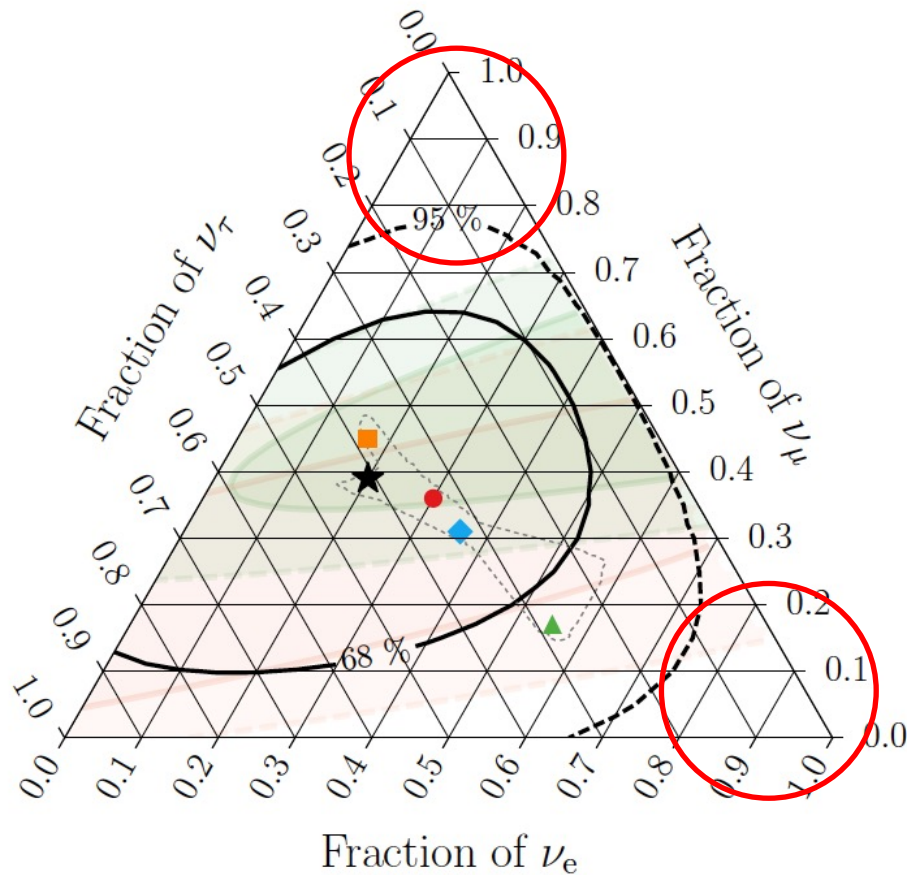




# Backup



# HESE 7.5-yr flavor ratio (2018)

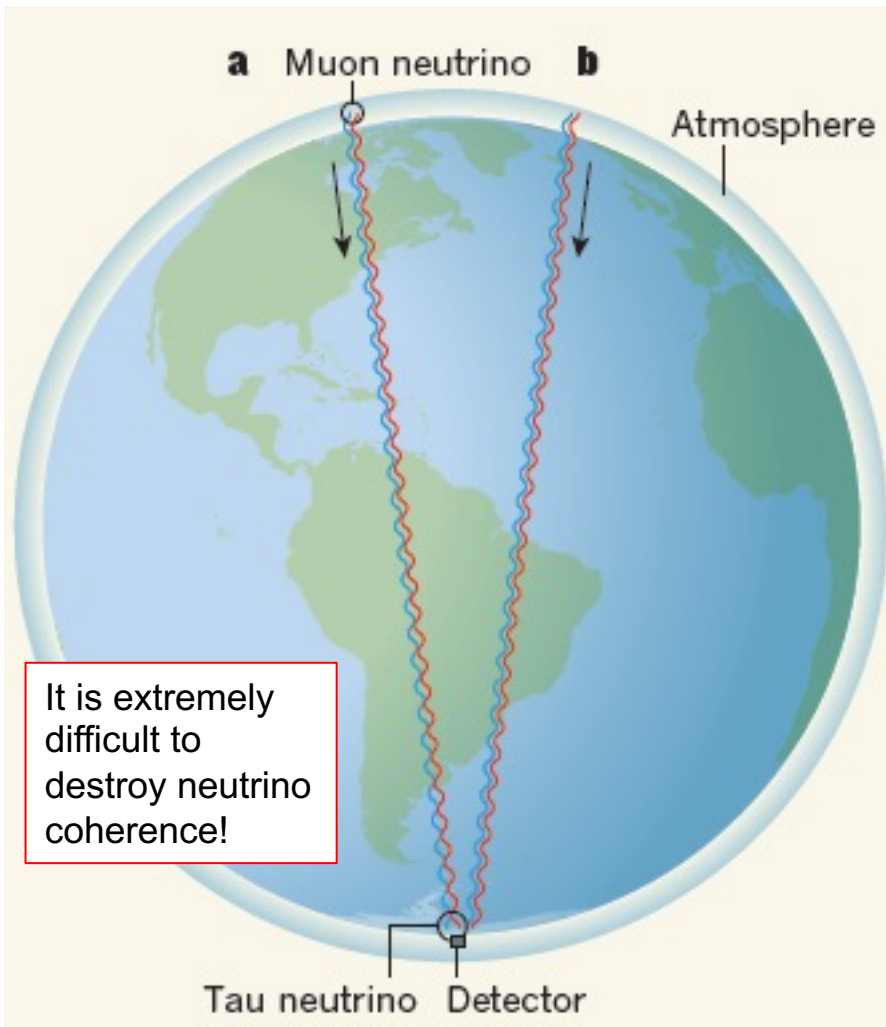


- HESE with ternary topology ID
- ★ Best fit: 0.20 : 0.39 : 0.42
- Global Fit (IceCube, APJ 2015)
- Inelasticity (IceCube, PRD 2019)
- ⋯⋯⋯ 3ν-mixing 3σ allowed region

- $\nu_e : \nu_\mu : \nu_\tau$  at source  $\rightarrow$  on Earth:
- 0:1:0  $\rightarrow$  0.17 : 0.45 : 0.37
  - 1:2:0  $\rightarrow$  0.30 : 0.36 : 0.34
  - ▲ 1:0:0  $\rightarrow$  0.55 : 0.17 : 0.28
  - ◆ 1:1:0  $\rightarrow$  0.36 : 0.31 : 0.33

We are mainly testing scenarios where we assume astrophysical neutrino productions are dominated by  $\nu_e$  or  $\nu_\mu$

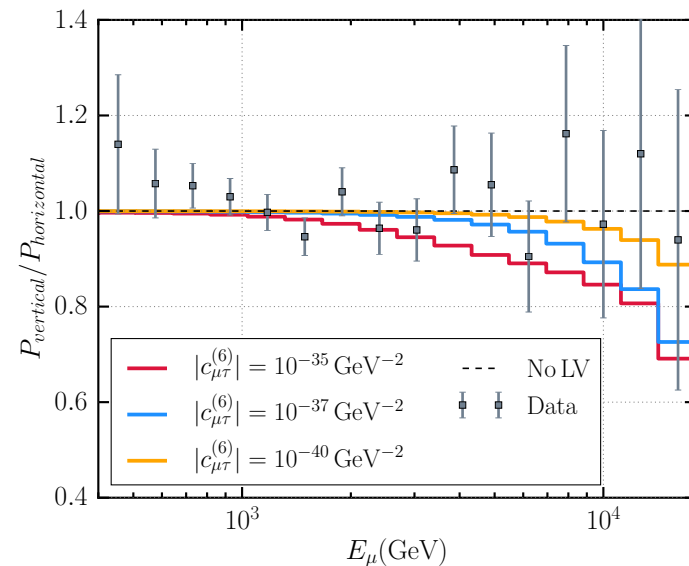
# Neutrino interferometry – Atmospheric neutrinos



Neutrino oscillation is a nature interferometer. Any extra interactions in the Lagrangian contribute the phase shift

The highest energy - 20 TeV  
The longest baseline - 12700km

If anomalous coupling with neutrinos in vacuum cause a phase shift in similar order, we can see it from **spectrum distortion of atmospheric neutrinos**



IceCube atmospheric neutrino limit,  $c^{(6)} < 10^{-36} GeV^{-2}$   
This is close to the target signal region,  $c^{(6)} \sim 10^{-38} GeV^{-2}$

# Neutrino interferometry – Atmospheric neutrinos

| dim.                 | method                            | type          | sector  | limits   | ref.      |
|----------------------|-----------------------------------|---------------|---|--|-----------|
| 3                    | CMB polarization                  | astrophysical | photon  | $\sim 10^{-43}$ GeV  | [6]       |
|                      | He-Xe comagnetometer              | tabletop      | neutron   | $\sim 10^{-34}$ GeV  | [10]      |
|                      | torsion pendulum                  | tabletop      | electron  | $\sim 10^{-31}$ GeV  | [12]      |
|                      | muon g-2                          | accelerator   | muon  | $\sim 10^{-24}$ GeV  | [13]      |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $ \text{Re}(\hat{a}_{\mu\tau}^{(3)}) ,  \text{Im}(\hat{a}_{\mu\tau}^{(3)})  < 2.9 \times 10^{-24}$ GeV (99% C.L.)<br>$< 2.0 \times 10^{-24}$ GeV (90% C.L.)                            | this work |
| 4                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-38}$  | [7]       |
|                      | Laser interferometer              | LIGO          | photon  | $\sim 10^{-22}$  | [8]       |
|                      | Sapphire cavity oscillator        | tabletop      | photon  | $\sim 10^{-18}$  | [5]       |
|                      | Ne-Rb-K comagnetometer            | tabletop      | neutron   | $\sim 10^{-29}$  | [11]      |
|                      | trapped $\text{Ca}^+$ ion         | tabletop      | electron  | $\sim 10^{-19}$  | [14]      |
| neutrino oscillation | atmospheric                       | neutrino      | $ \text{Re}(\hat{c}_{\mu\tau}^{(4)}) ,  \text{Im}(\hat{c}_{\mu\tau}^{(4)})  < 3.9 \times 10^{-28}$ (99% C.L.)<br>$< 2.7 \times 10^{-28}$ (90% C.L.) | this work  |           |
| 5                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-34}$ $\text{GeV}^{-1}$  | [7]       |
|                      | ultra-high-energy cosmic ray      | astrophysical | proton  | $\sim 10^{-22}$ to $10^{-18}$ $\text{GeV}^{-1}$  | [9]       |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{a}_{\mu\tau}^{(5)}) ,  \text{Im}(\hat{a}_{\mu\tau}^{(5)})  < 2.3 \times 10^{-32}$ $\text{GeV}^{-1}$ (99% C.L.)<br>$< 1.5 \times 10^{-32}$ $\text{GeV}^{-1}$ (90% C.L.) | this work |
| 6                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-31}$ $\text{GeV}^{-2}$  | [7]       |
|                      | ultra-high-energy cosmic ray      | astrophysical | proton  | $\sim 10^{-42}$ to $10^{-35}$ $\text{GeV}^{-2}$  | [9]       |
|                      | gravitational Cherenkov radiation | astrophysical | gravity   | $\sim 10^{-31}$ $\text{GeV}^{-2}$  | [15]      |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{c}_{\mu\tau}^{(6)}) ,  \text{Im}(\hat{c}_{\mu\tau}^{(6)})  < 1.5 \times 10^{-36}$ $\text{GeV}^{-2}$ (99% C.L.)<br>$< 9.1 \times 10^{-37}$ $\text{GeV}^{-2}$ (90% C.L.) | this work |
| 7                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-28}$ $\text{GeV}^{-3}$  | [7]       |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{a}_{\mu\tau}^{(7)}) ,  \text{Im}(\hat{a}_{\mu\tau}^{(7)})  < 8.3 \times 10^{-41}$ $\text{GeV}^{-3}$ (99% C.L.)<br>$< 3.6 \times 10^{-41}$ $\text{GeV}^{-3}$ (90% C.L.) | this work |
| 8                    | gravitational Cherenkov radiation | astrophysical | gravity   | $\sim 10^{-46}$ $\text{GeV}^{-4}$  | [15]      |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{c}_{\mu\tau}^{(8)}) ,  \text{Im}(\hat{c}_{\mu\tau}^{(8)})  < 5.2 \times 10^{-45}$ $\text{GeV}^{-4}$ (99% C.L.)<br>$< 1.4 \times 10^{-45}$ $\text{GeV}^{-4}$ (90% C.L.) | this work |

TABLE I: Comparison of attainable best limits of SME coefficients in various fields.

IceCube atmospheric neutrino limit,  $c^{(6)} < 10^{-36} \text{GeV}^{-2}$   
 This is close to the target signal region,  $c^{(6)} \sim 10^{-38} \text{GeV}^{-2}$



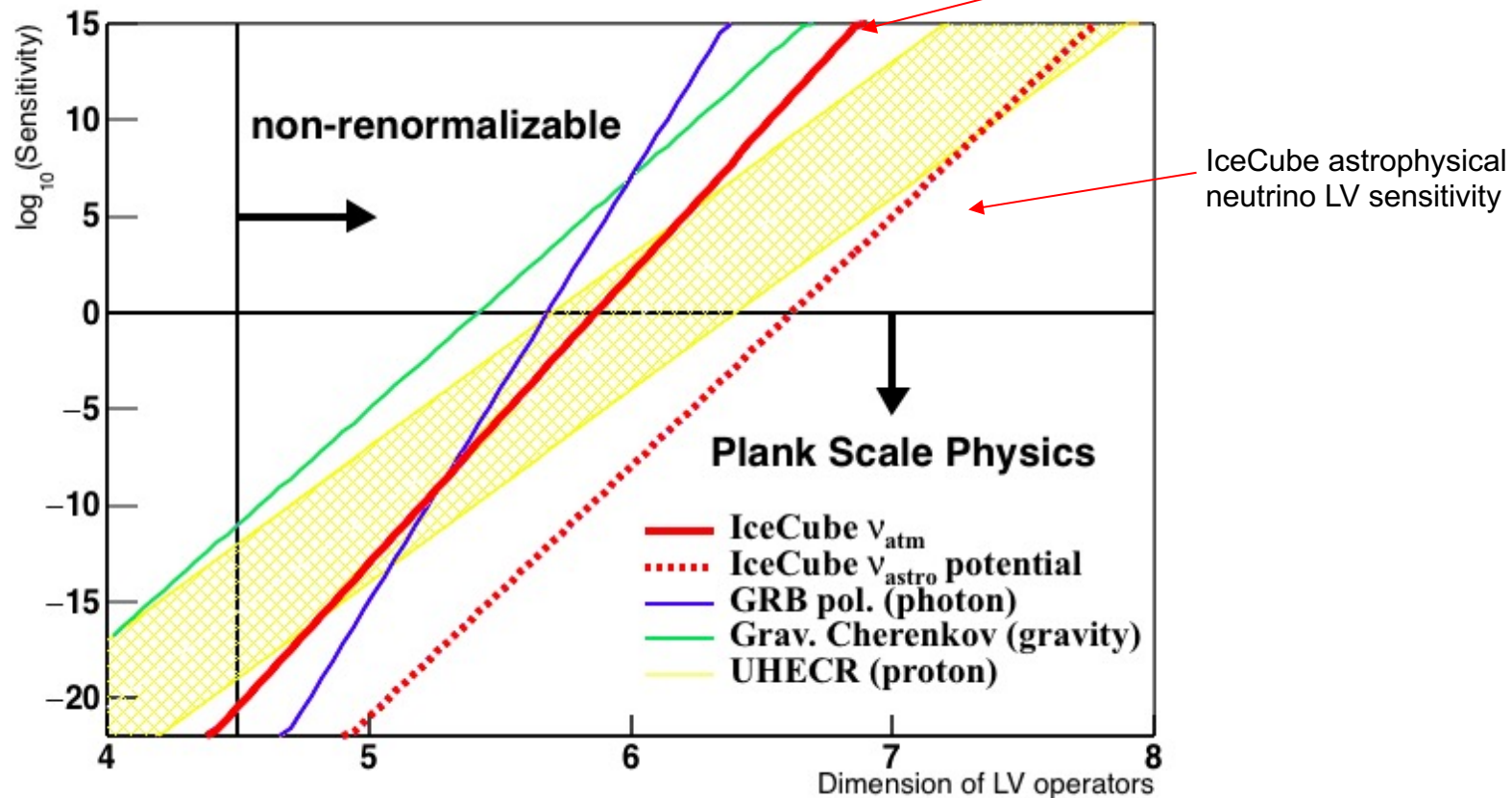
# Neutrino interferometry – Astrophysical neutrinos

Higher-dimension operators may be related to new physics

- Dimension-5 operator (unit:  $\text{GeV}^{-1}$ ), example: Majorana mass
- Dimension-6 operator (unit:  $\text{GeV}^{-2}$ ), example: Fermi constant ( $G_F$ )

IceCube atmospheric neutrino LV sensitivity  
Nature Physics 14(2018)961

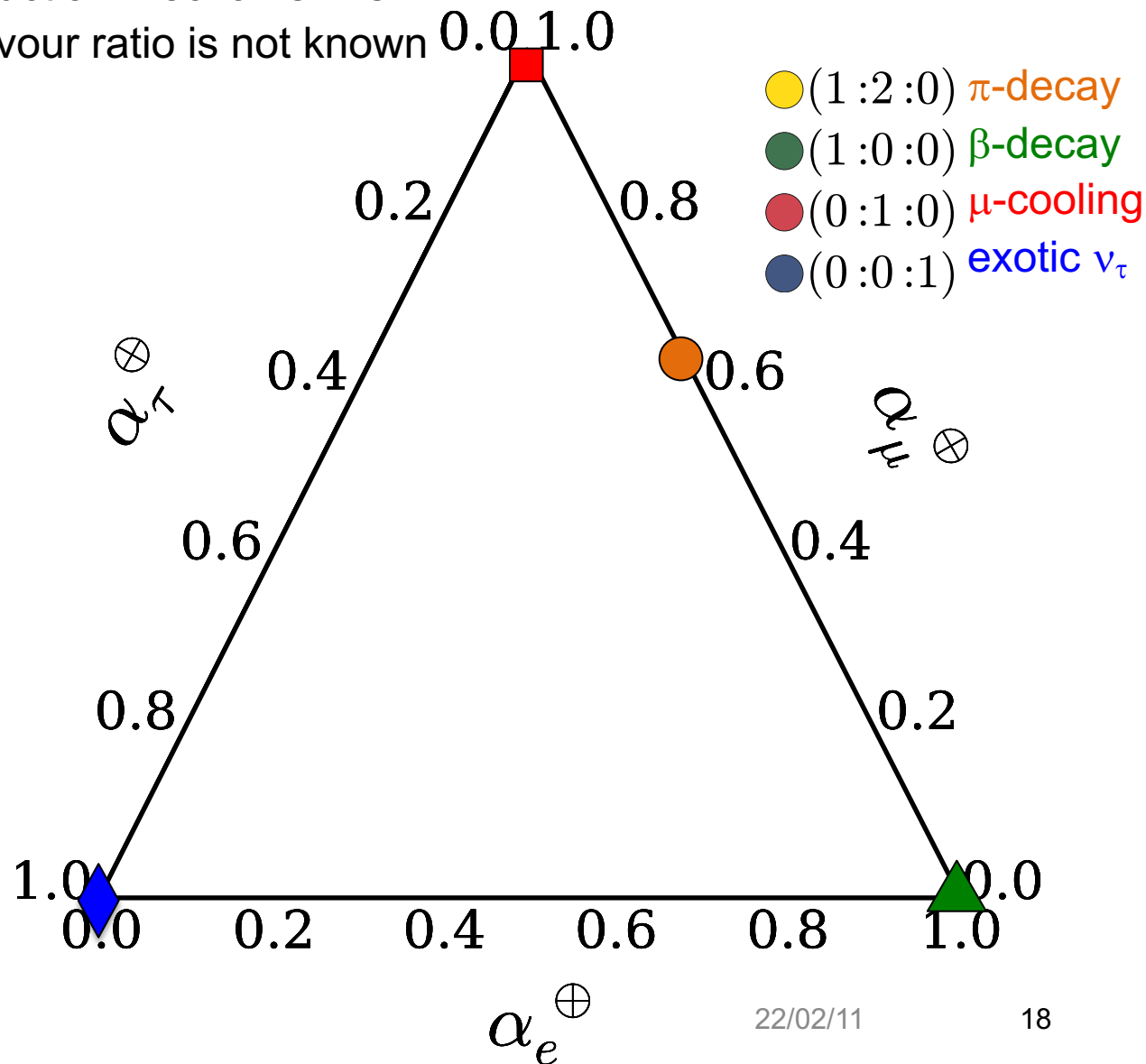
New physics limits and projected sensitivity



Astrophysical neutrino dim-6 LV operator search can reach quantum gravity motivated region ( $\sim 1/M_{\text{Planck}}^2 \sim 10^{-38} \text{ GeV}^{-2}$ )

### 3. Neutrino flavor ratio ( $\nu_e : \nu_\mu : \nu_\tau$ )

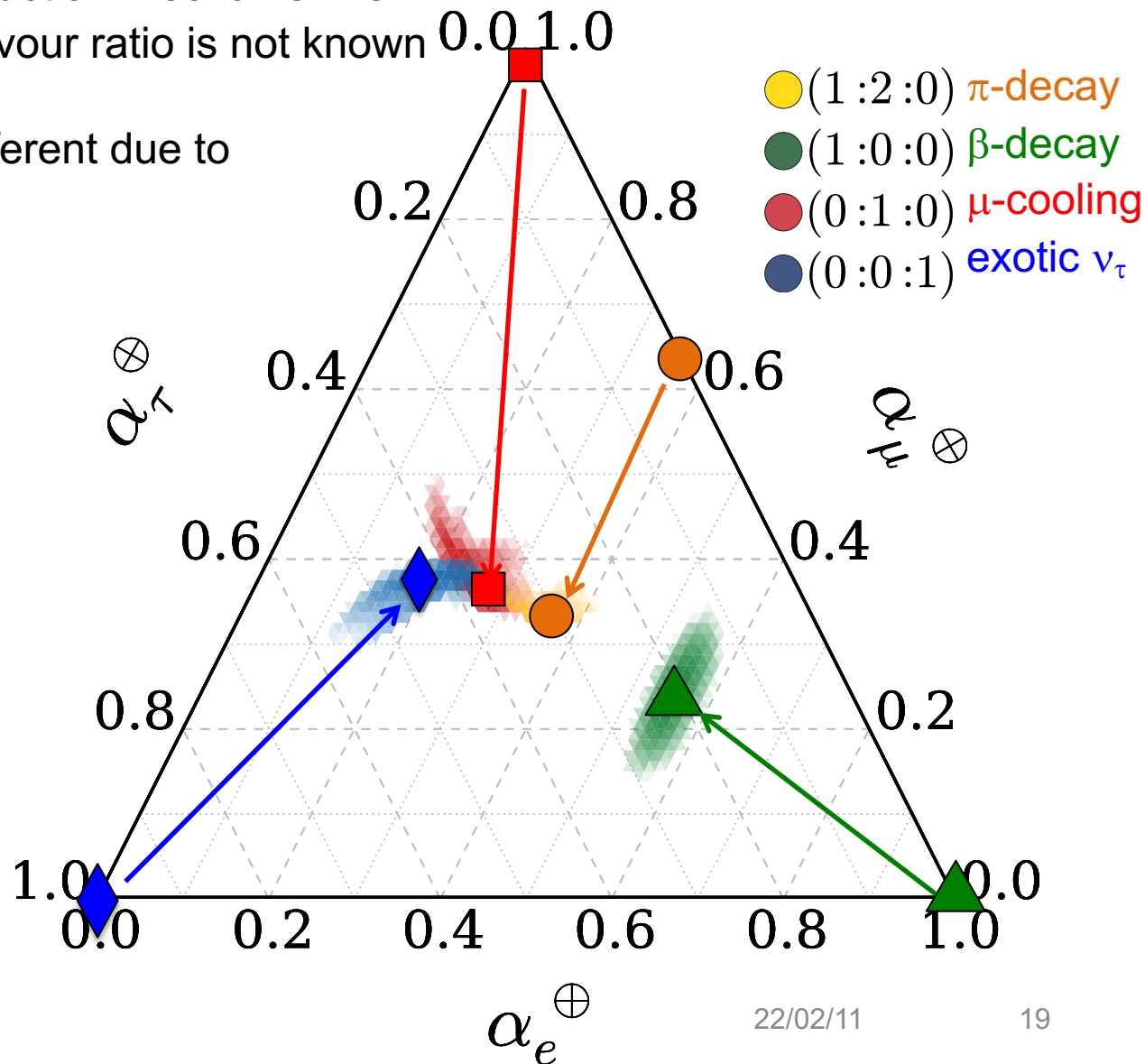
Astrophysical neutrino production mechanism is not known  $\rightarrow$  production flavour ratio is not known



### 3. Neutrino flavor ratio ( $\nu_e : \nu_\mu : \nu_\tau$ )

Astrophysical neutrino production mechanism is not known  $\rightarrow$  production flavour ratio is not known

Flavour ratio on Earth is different due to mixing by neutrino masses

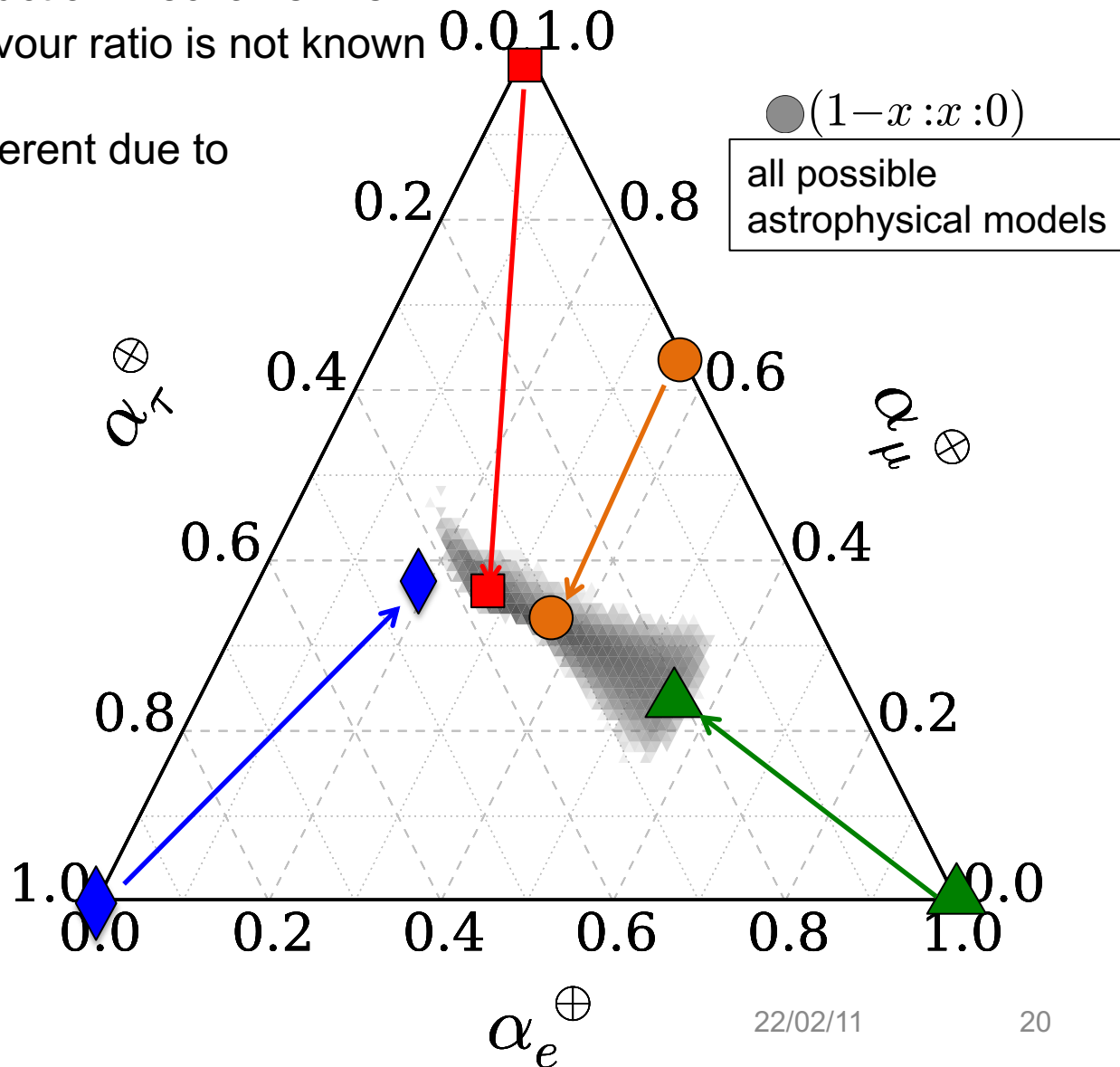


### 3. Neutrino flavor ratio ( $\nu_e : \nu_\mu : \nu_\tau$ )

Astrophysical neutrino production mechanism is not known  $\rightarrow$  production flavour ratio is not known

Flavour ratio on Earth is different due to mixing by neutrino masses

All possible flavour ratio is confined in a small space



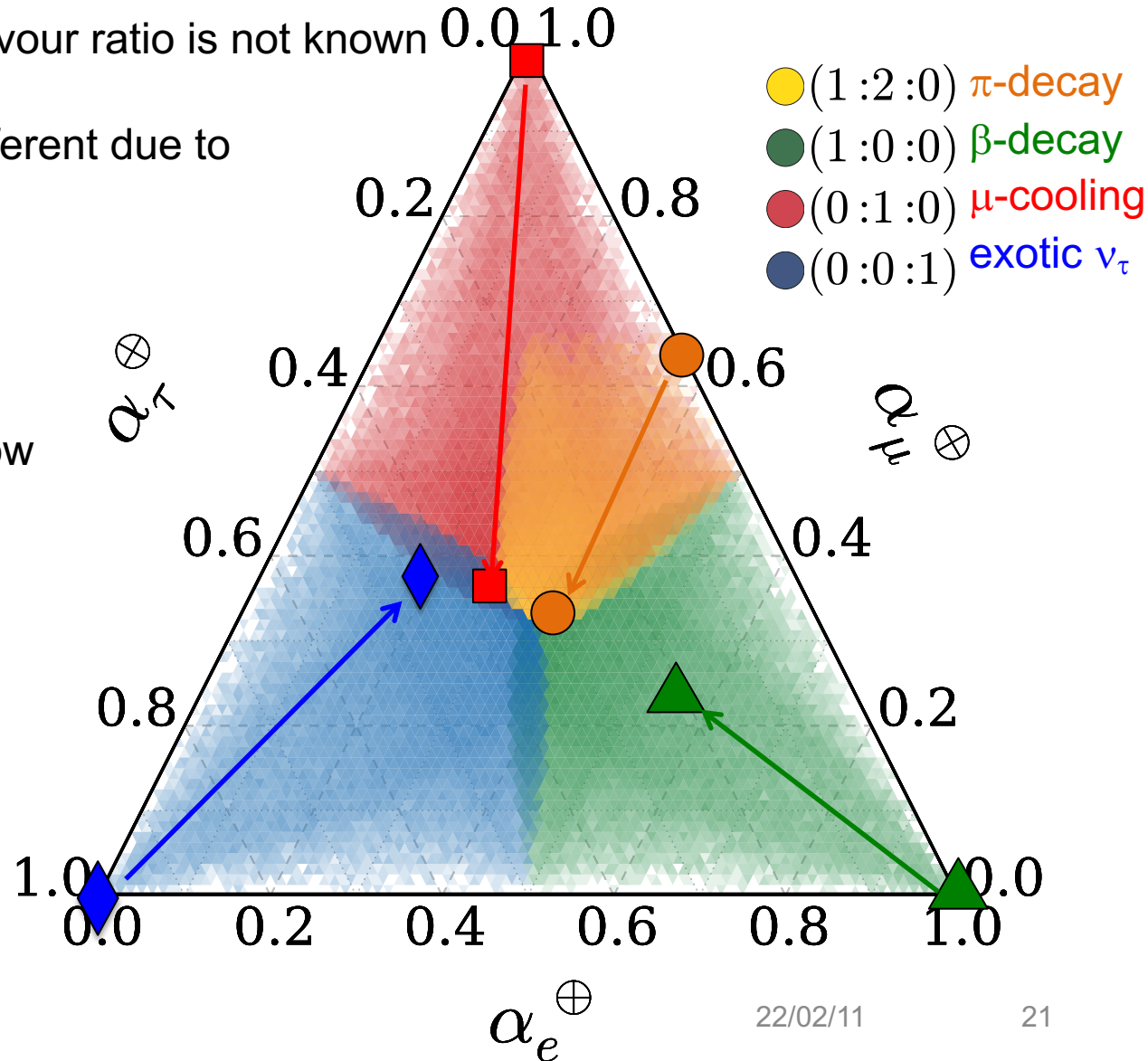
### 3. Neutrino flavor ratio ( $\nu_e : \nu_\mu : \nu_\tau$ )

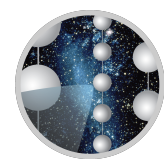
Astrophysical neutrino production mechanism is not known  $\rightarrow$  production flavour ratio is not known

Flavour ratio on Earth is different due to mixing by neutrino masses

All possible flavour ratio is confined in a small space

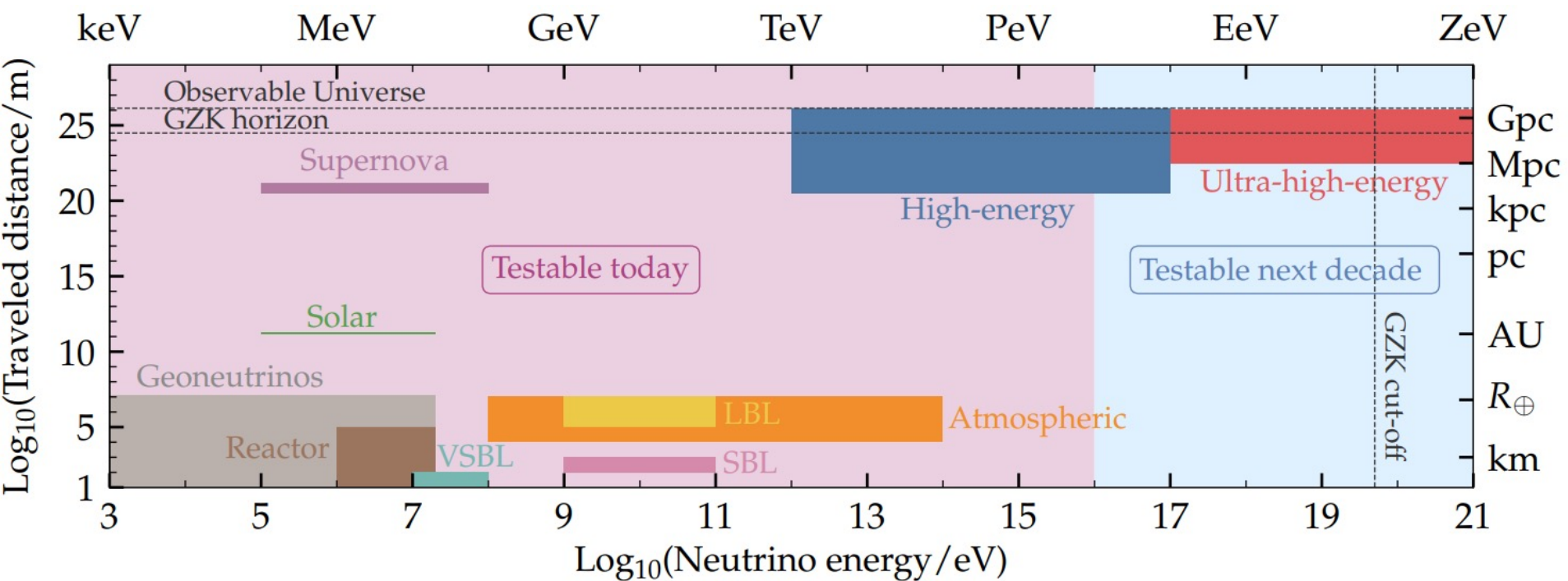
e.g.) New physics just below the limit can produce any flavour ratio

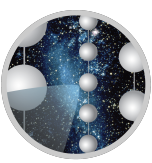




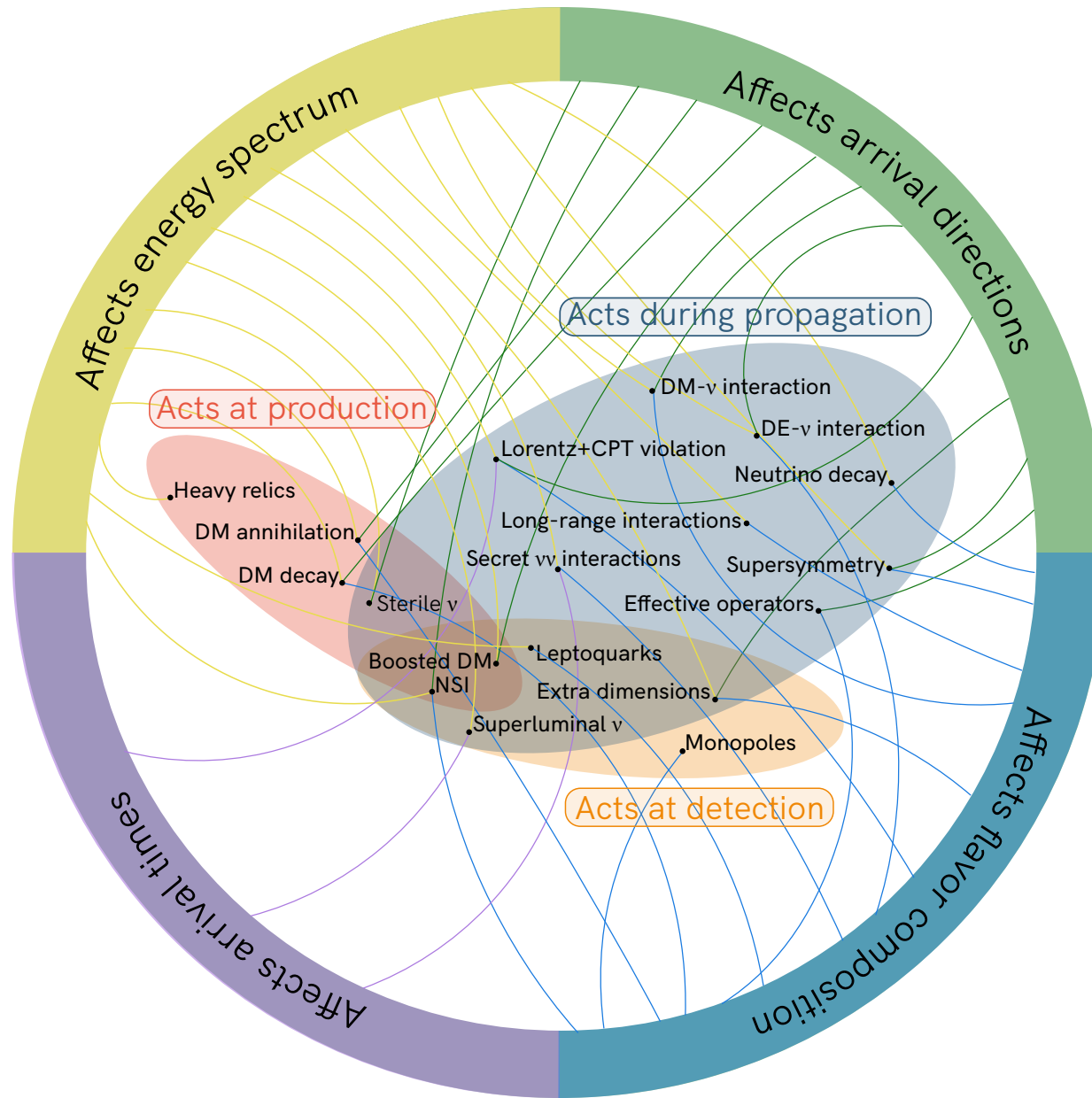
# Fundamental Physics with High-Energy Cosmic Neutrinos

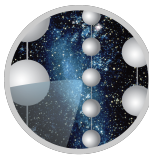
## Today and in the Future





# Fundamental Physics with High-Energy Cosmic Neutrinos Today and in the Future





# Flavor new physics search with effective operators

Neutrino oscillation formula is written with mixing matrix elements and eigenvalues

$$P_{\alpha \rightarrow \beta}(E, L) = 1 - 4 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin^2 \left( \frac{\lambda_i - \lambda_j}{2} L \right) + 2 \sum_{i>j} \text{Im}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin \left( (\lambda_i - \lambda_j) L \right)$$

However, astrophysical neutrinos propagate  $O(100\text{Mpc}) \rightarrow$  lost coherence

$$P_{\alpha \rightarrow \beta}(E, \infty) \sim 1 - 2 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) = \sum_i |V_{\alpha i}|^2 |V_{\beta i}|^2$$

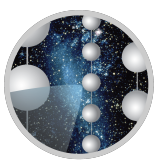
Astrophysical neutrino flux of flavour  $\alpha$  at production is  $\phi_{\alpha}^p(E) \sim \phi_{\alpha}^p \cdot E^{-\gamma}$ . Since it's low statistics, we consider energy-averaged flavour composition  $\beta$  on Earth

$$\bar{\phi}_{\beta}^{\oplus} = \frac{1}{\Delta E} \int_{\Delta E} \sum_{\alpha} P_{\alpha \rightarrow \beta}(E, \infty) \phi_{\alpha}^p(E) dE$$

We take the fraction of this for each flavour.

$$f_{\beta}^{\oplus} = \frac{\bar{\phi}_{\beta}^{\oplus}}{\sum_{e, \mu, \tau} \bar{\phi}_{\gamma}^{\oplus}}$$





# HESE 7.5-yr data flavor new physics search

Data, 2635 days HESE sample [IceCube,PRD104\(2021\)022002](#)

- 17 track events, 20  $\log(E)$  bins [60 TeV, 10 PeV], 10  $\cos\theta$  bins [-1.0, +1.0 ]
- 41 cascade events, 20  $\log(E)$  bins [60 TeV, 10 PeV], 10  $\cos\theta$  bins [-1.0, +1.0 ]
- 2 double cascades, 20  $\log(E)$  bins [60 TeV, 10 PeV], 10  $\log(L)$  bins [10m, 100m]

## Simulation

[Bhattacharya et al., JHEP06\(2015\)110](#)

- Foregrounds, conventional (Honda flux), prompt (BERSS model), muon (CORSIKA)
- Astrophysical neutrinos, simple power law
- Interaction, NLO PDF DIS (CSMS model) [Cooper-Sarkar et al., JHEP08\(2011\)042](#)

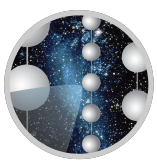
## Systematics (15 nuisance parameters)

- oscillation parameters (6)
- normalization of flux : conventional (40%), prompt (free), muon (50%), astrophysical (free)
- spectrum index : primary cosmic ray (5%) astrophysical neutrinos (free)
- Ice model : (20%)
- DOM efficiency : overall (10%), angular dependence (50%)

## Limits

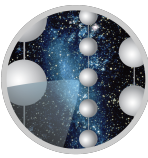
[Feroz et al., Mon. Not. Roy. Astron. Soc. 398,1601\(2009\)1601](#)

- Bayesian: MCMC with Multinest, Bayes factor with Jefferey' scale “strong” limit
- Frequentist: Wilks' theorem

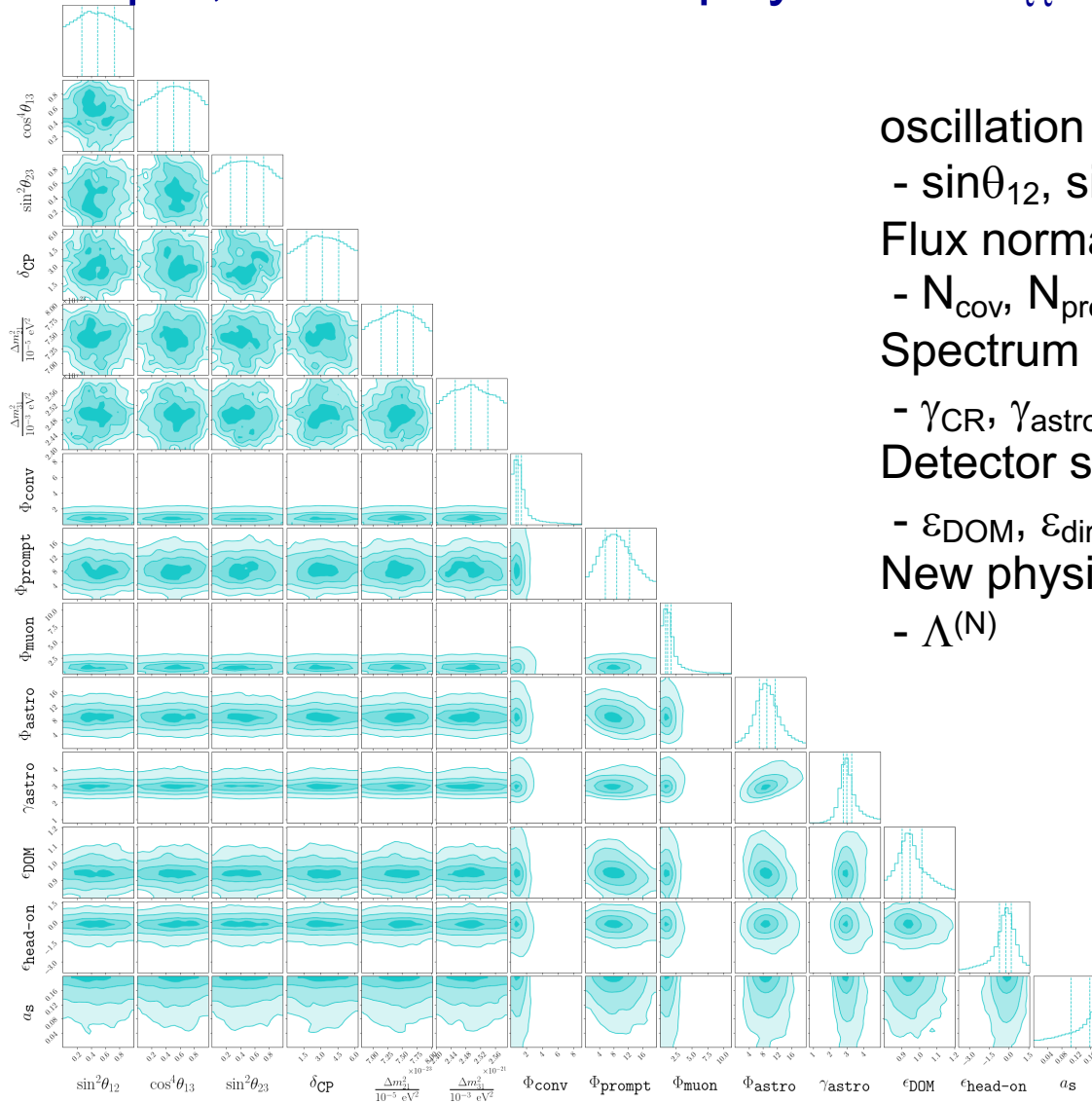


# HESE 7.5-yr data systematic errors

| Parameter                                | Prior (constraint) | Range               | Description                             |
|--|--------------------|---------------------|---|
| <b>Astrophysical neutrino flux:</b>      |                    |                     |   |
| $\Phi_{\text{astro}}$                    | -                  | $[0, \infty)$       | Normalization scale                     |
| $\gamma_{\text{astro}}$                  | -                  | $(-\infty, \infty)$ | Spectral index                          |
| <b>Atmospheric neutrino flux:</b>        |                    |                     |   |
| $\Phi_{\text{conv}}$                     | $1.0 \pm 0.4$      | $[0, \infty)$       | Conventional normalization scale        |
| $\Phi_{\text{prompt}}$                   | -                  | $[0, \infty)$       | Prompt normalization scale              |
| $R_{K/\pi}$                              | $1.0 \pm 0.1$      | $[0, \infty)$       | Kaon-Pion ratio correction              |
| $2\nu / (\nu + \bar{\nu})_{\text{atmo}}$ | $1.0 \pm 0.1$      | $[0, 2]$            | Neutrino-anti-neutrino ratio correction |
| <b>Cosmic-ray flux:</b>                  |                    |                     |   |
| $\Delta\gamma_{\text{CR}}$               | $0.0 \pm 0.05$     | $(-\infty, \infty)$ | Cosmic-ray spectral index modification  |
| $\Phi_{\mu}$                             | $1.0 \pm 0.5$      | $[0, \infty)$       | Muon normalization scale                |
| <b>Detector:</b>                         |                    |                     |   |
| $\epsilon_{\text{DOM}}$                  | $0.99 \pm 0.1$     | $[0.80, 1.25]$      | Absolute energy scale                   |
| $\epsilon_{\text{head-on}}$              | $0.0 \pm 0.5$      | $[-3.82, 2.18]$     | DOM angular response                    |
| $a_{\text{s}}$                           | $1.0 \pm 0.2$      | $[0.0, 2.0]$        | Ice anisotropy scale                    |



# Fit example, $10^{-44}$ GeV<sup>-2</sup> new physics in $c_{\tau\tau}^{(6)}$



oscillation parameters

-  $\sin\theta_{12}$ ,  $\sin\theta_{23}$ ,  $\sin\theta_{13}$ ,  $\Delta m_{12}$ ,  $\Delta m_{23}$ ,  $\delta$

Flux normalization

-  $N_{\text{cov}}$ ,  $N_{\text{prompt}}$ ,  $N_{\text{muon}}$ ,  $N_{\text{astro}}$

Spectrum index

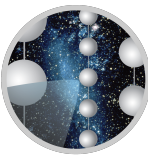
-  $\gamma_{\text{CR}}$ ,  $\gamma_{\text{astro}}$

Detector systematics

-  $\epsilon_{\text{DOM}}$ ,  $\epsilon_{\text{direction}}$ ,  $\alpha_{\text{anisotropy}}$

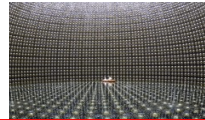
New physics scale

-  $\Lambda^{(N)}$



# Test of Lorentz violation with neutrinos

## Spectral distortion



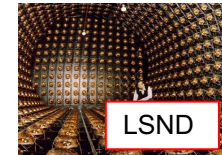
Super-Kamiokande

PRD91(2015)052003



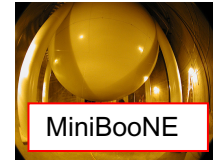
Daya Bay

PRD98(2018)092013



LSND

PRD72(2005)076004



MiniBooNE

PLB718(2013)1303



MINOS ND

PRL101(2008)151601



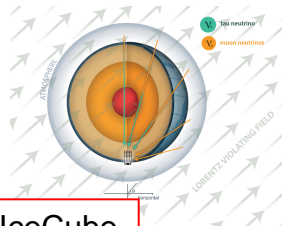
MINOS FD

PRL105(2010)151601



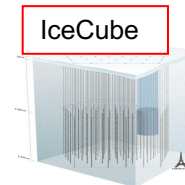
AMANDA

PRD79(2009)102005



IceCube

Nature Physics  
14(2018)961



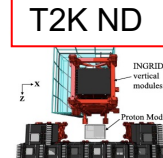
IceCube

PRD82(2010)112003



Double Chooz

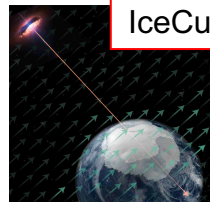
PRD86(2013)112009



T2K ND

PRD95(2017)111101

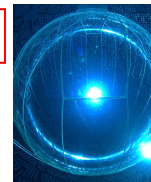
## Flavor ratio



IceCube

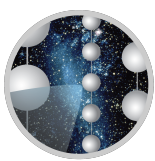
ArXiv:2111.04654

SNO



PRD98(2018)112013

## Seasonal variation



# Energy dependence of flavor ratio

