

From Brave New Spacetime: Quantum Gravity

“Postcards from the Very Edge, With Love from IceCube”

outline

1. Test of Fundamental Physics
2. Neutrino interferometry with IceCube
3. Astrophysics neutrino flavour physics
4. Conclusions



Tepppei Katori for the IceCube collaboration
King's College London
APS April meeting, NYC, USA, April 12, 2022

1. Test of Fundamental Physics

2. Neutrino interferometry with IceCube

3. Astrophysics neutrino flavour physics

4. Conclusions

1. Violation of fundamental physics

All fundamental physics phenomena must be experimentally tested including **Lorentz symmetry**, isotropy of the space-time

Fundamental physics laws are basis of all science, so the violation, if it exists, must be **very small**

Einstein and Lorentz



Lorentz Institute

1. Violation of fundamental physics

All fundamental physics phenomena must be experimentally tested including **Lorentz symmetry**, isotropy of the space-time

Fundamental physics laws are basis of all science, so the violation, if it exists, must be **very small**

However, **quantum gravity** theories show it is possible to violate fundamental physics laws

- string theory
 - noncommutative field theory
- etc.

Discovery of a new space-time structure is the breakthrough to understand quantum gravity theories!

Einstein and Lorentz



Lorentz Institute

1. Violation of fundamental physics

Coupling of ordinary particles (photons, neutrinos, etc) and new space-time structure might modify behaviour of particles in vacuum

- Energy spectrum
 - Neutrino flavour
- etc.

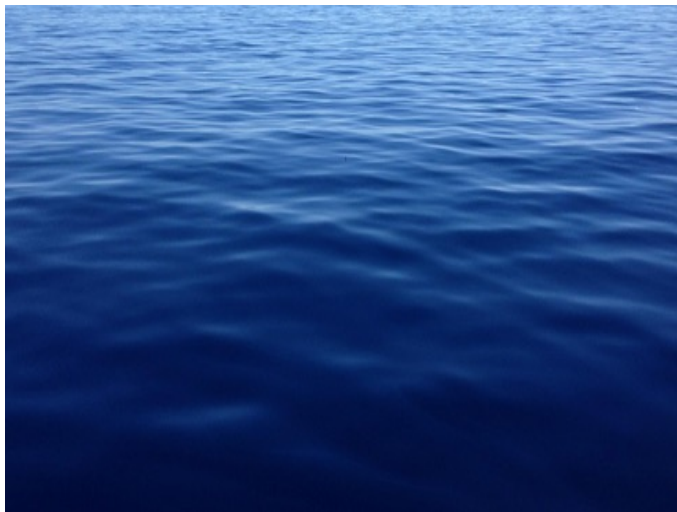
$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu\psi + \bar{\psi}\gamma^\mu c_{\mu\nu}\partial^\nu\psi \dots$$

The equation is annotated with a blue box labeled "Standard Model" under the first three terms and a green box labeled "New physics" under the last two terms. A green arrow points from the "New physics" box to the right.

Expected effect is small. We need **high-precision measurements** to find such new physics

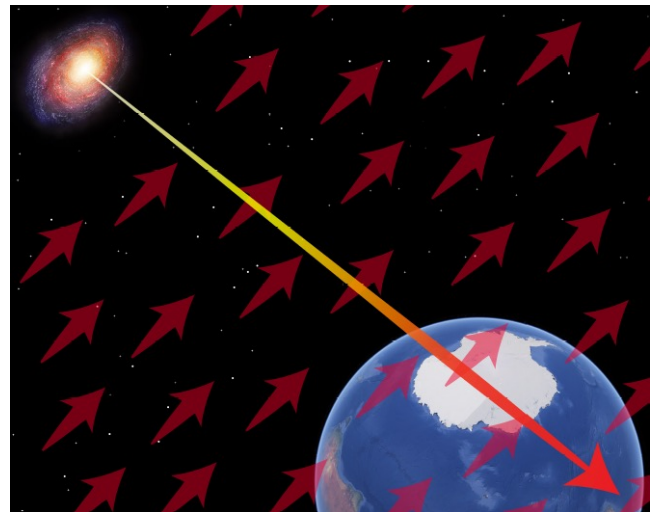
quantum foam

- quantum fluctuation of space-time

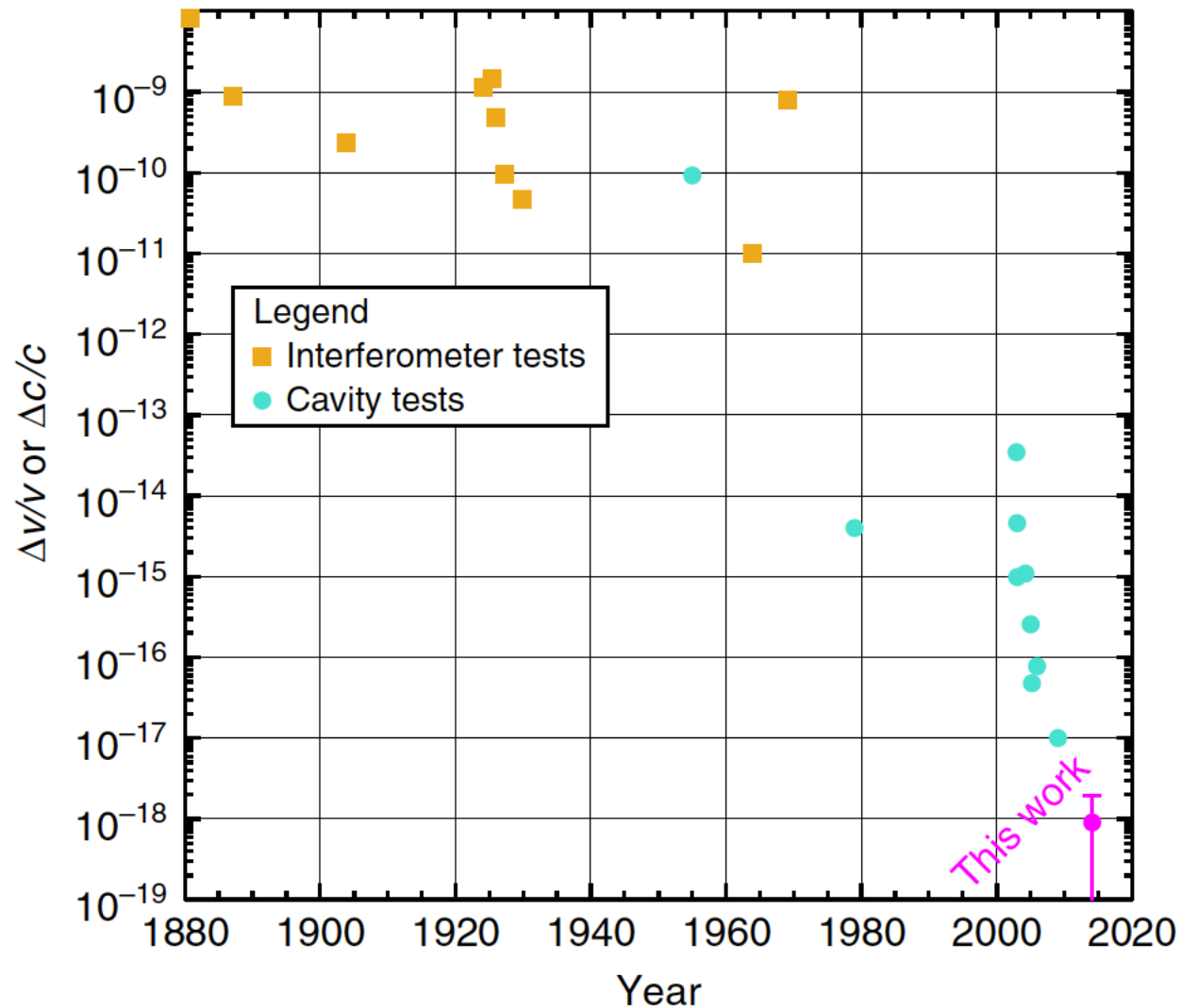


Lorentz violating field

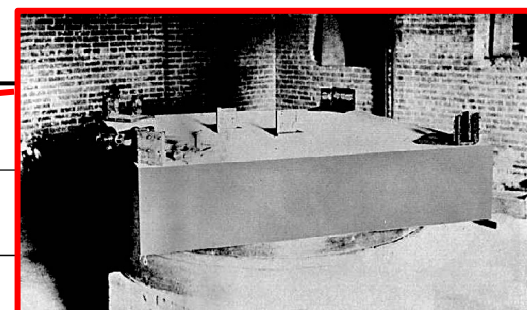
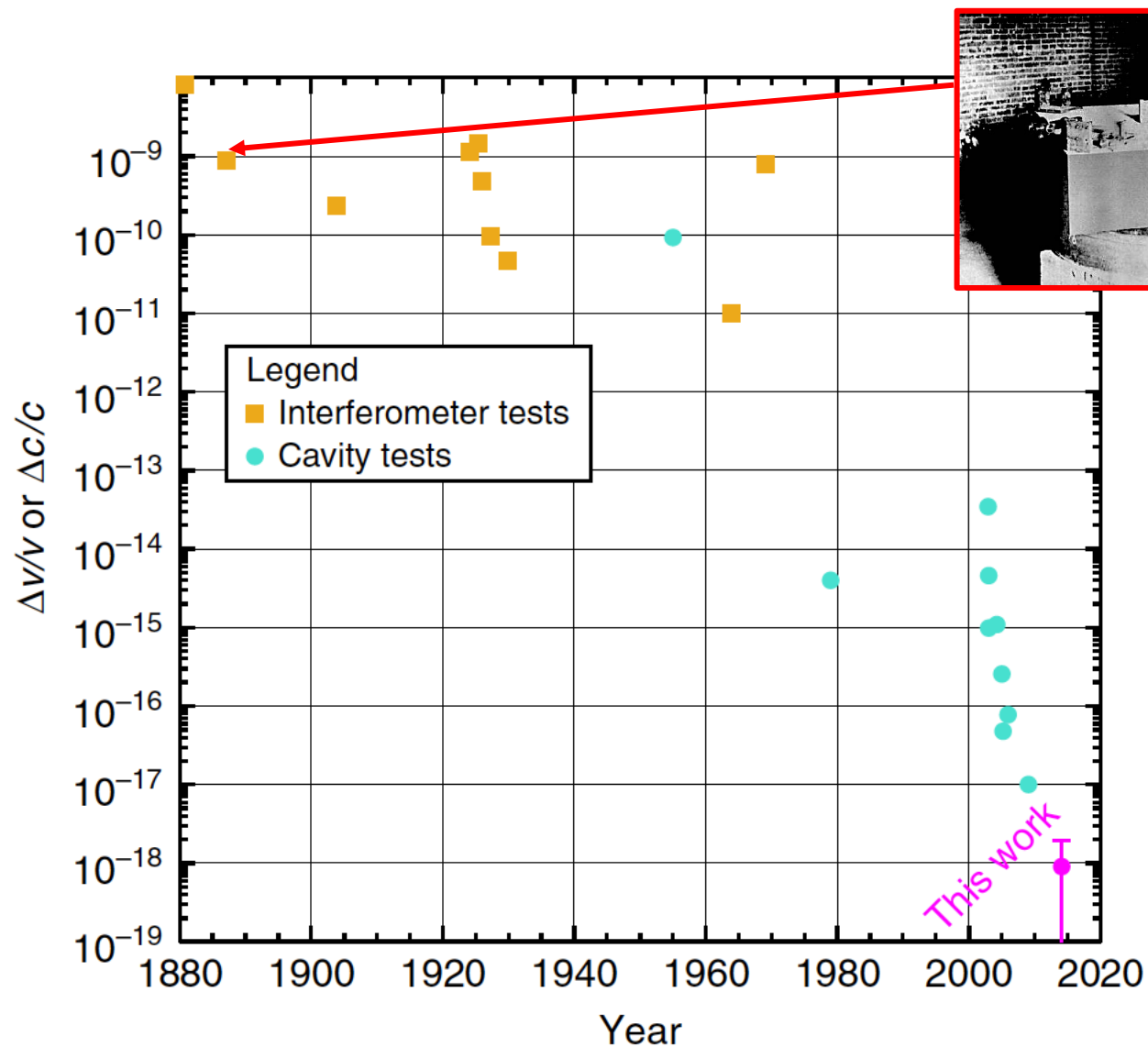
- new field saturating the universe (æther)



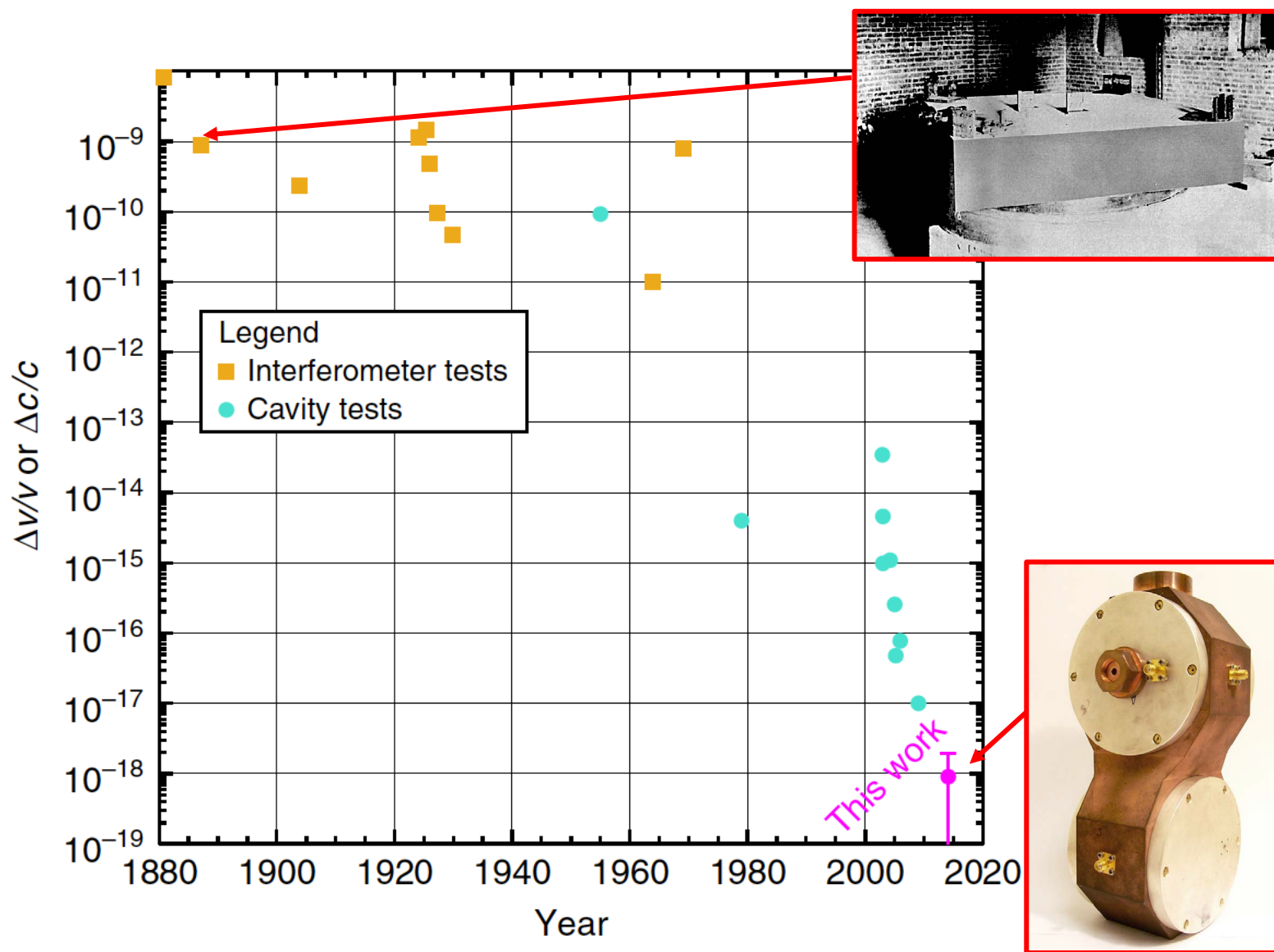
1. History of Michelson-Morley experiment



1. History of Michelson-Morley experiment (1887)



1. History of Michelson-Morley experiment (2015)



From King's College London to IceCube

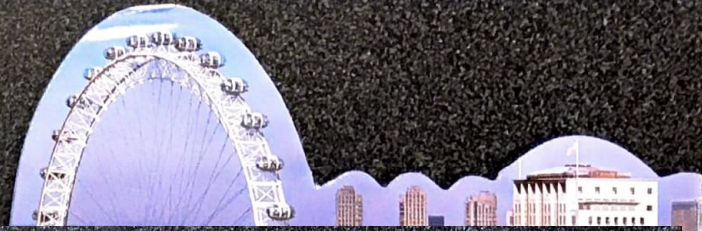


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From King's College London to IceCube



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& King's
College
London


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Tel: 01707 271710. Printed in E.C.



Greetings,
IceCube allows me to work on
many topics from dinner skits
to search of Lorentz Violation [1].
We are so close to beat
Einstein and find Quantum Gravity!

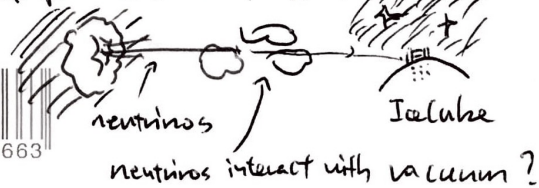
to: IceCube
222 W. Washington Ave.
Suite 500
Madison, WI 53703
U.S. A.

BY AIR MAIL
par avion
Royal Mail®

Ciao,
Tepper  Katoni
Reader (associate professor)
King's College London
WC2E 2LS London, UK

IceCube
Since 2014

[1] about Lorentz Violation. Astrophysical Neutrinos propagate long distance straight, and any tiny interaction with vacuum may change flavor. This is the way to look for the smallest effect in space-time.



From King's College London to IceCube

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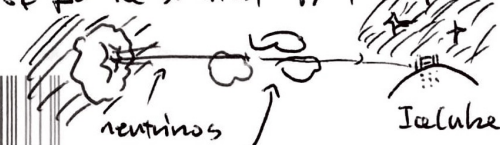


neutrinos interact with vacuum?

Ciao,
Tepper  Katoni

IceCube
Since 2014

[1] about Lorentz Violation. Astrophysical Neutrinos propagate long distance straight, and any tiny interaction with vacuum may change flavor. This is the way to look for the smallest effect in space-time.



neutrinos interact with vacuum?

High-energy astrophysical neutrinos are the highest energy particles propagating the longest distance in straight



42980

42980

1. Test of Fundamental Physics

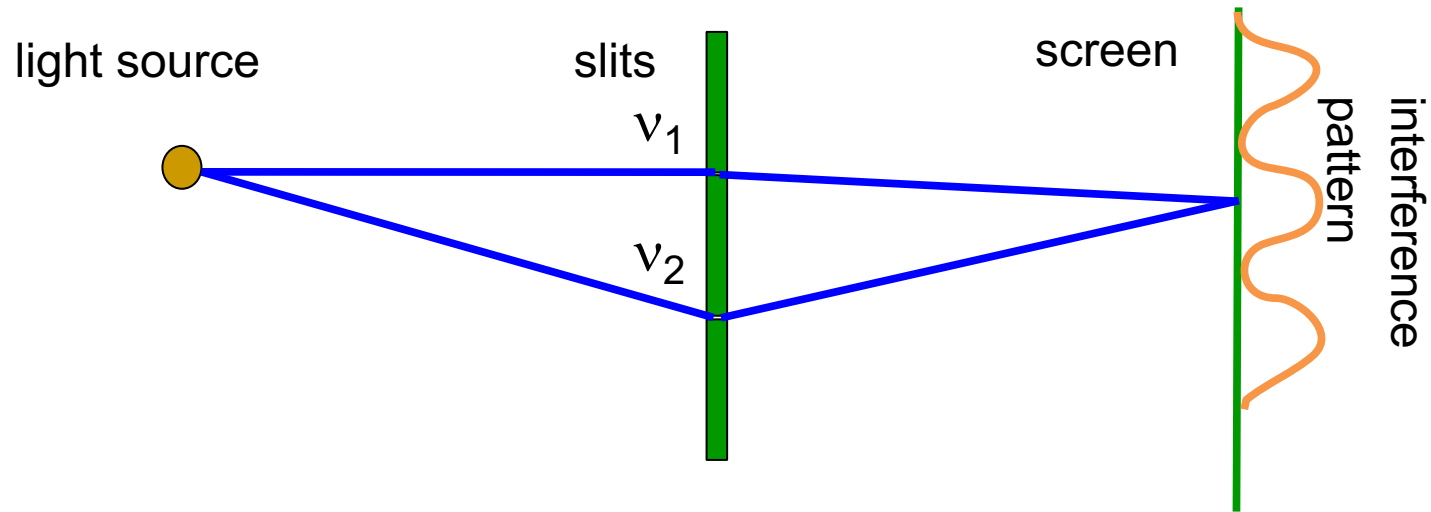
2. Neutrino interferometry with IceCube

3. Astrophysics neutrino flavour physics

4. Conclusions

2. Double slit experiment

Neutrino flavour conversion is an interference experiment

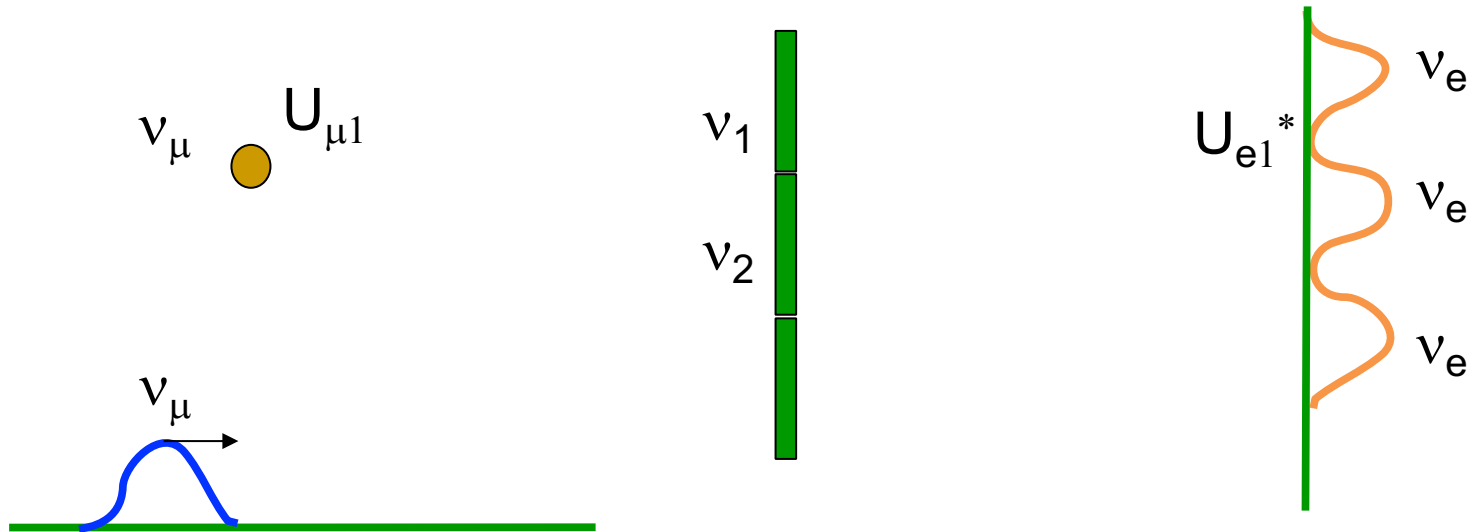


For double slit experiment, if path v_1 and path v_2 have different length, they have different phase rotations and it causes interference.

Interference pattern carries the information of an invisibly small slit size

2. Neutrino interferometry for neutrino mass measurement

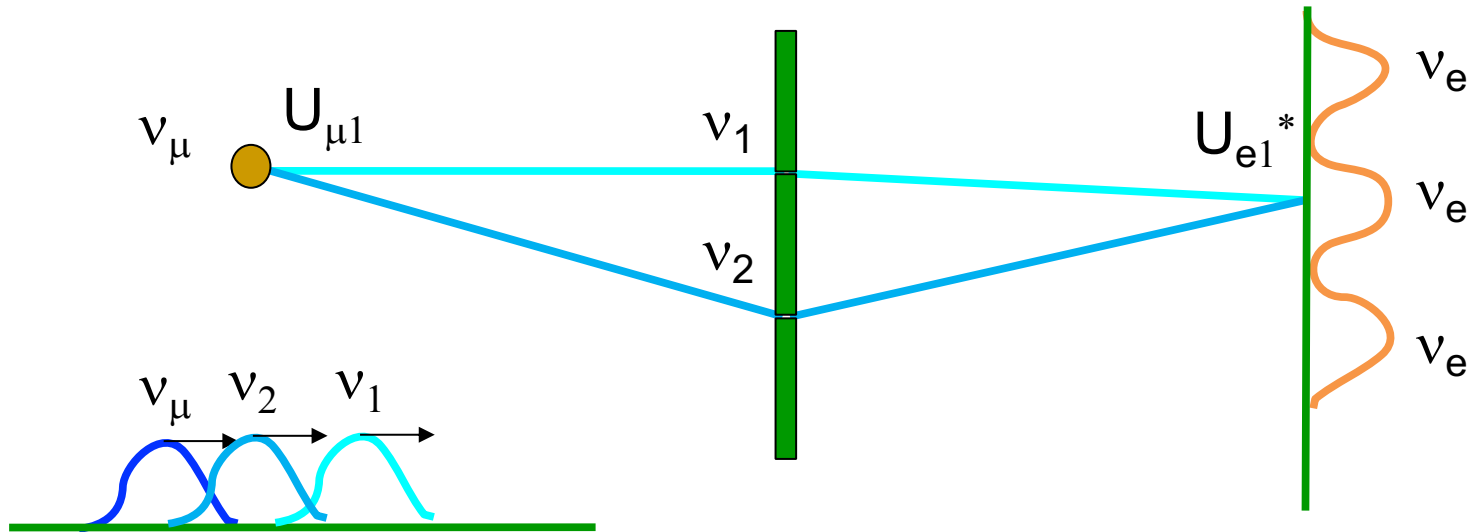
Neutrino flavour conversion is an interference experiment



Neutrinos are produced in flavour eigenstates, but they propagate as Hamiltonian eigenstates, then detected in flavour eigenstates

2. Neutrino interferometry for neutrino mass measurement

Neutrino flavour conversion is an interference experiment

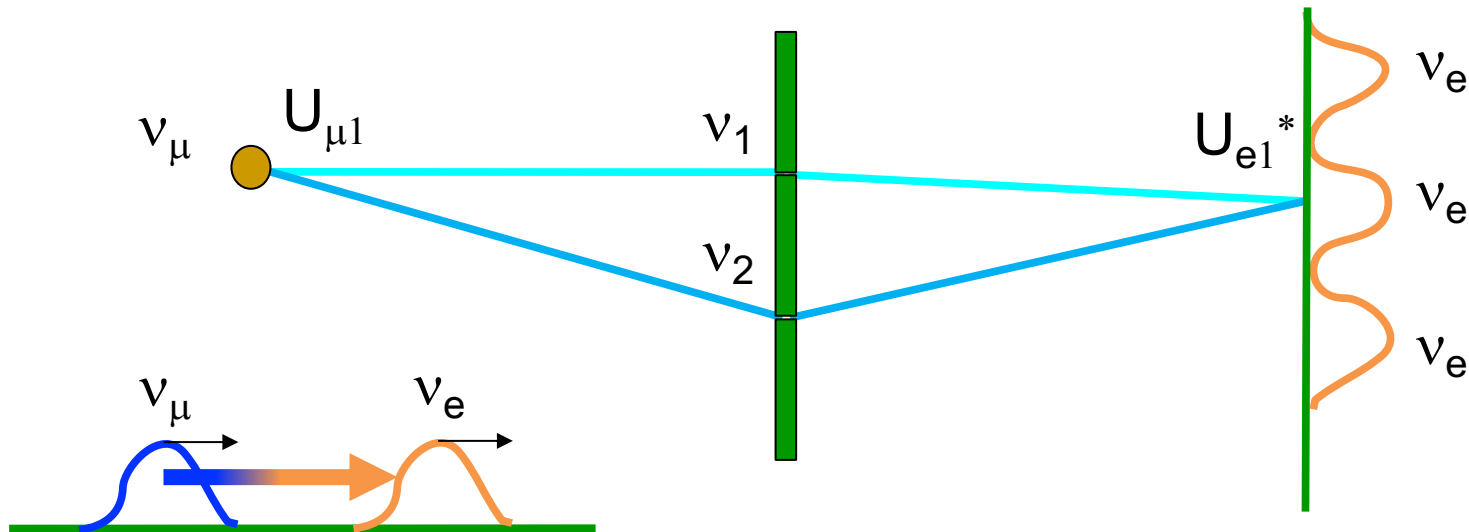


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If ν_1 and ν_2 , have different masses, they have different velocity and they don't overlap exactly at the detection

2. Neutrino interferometry for neutrino mass measurement

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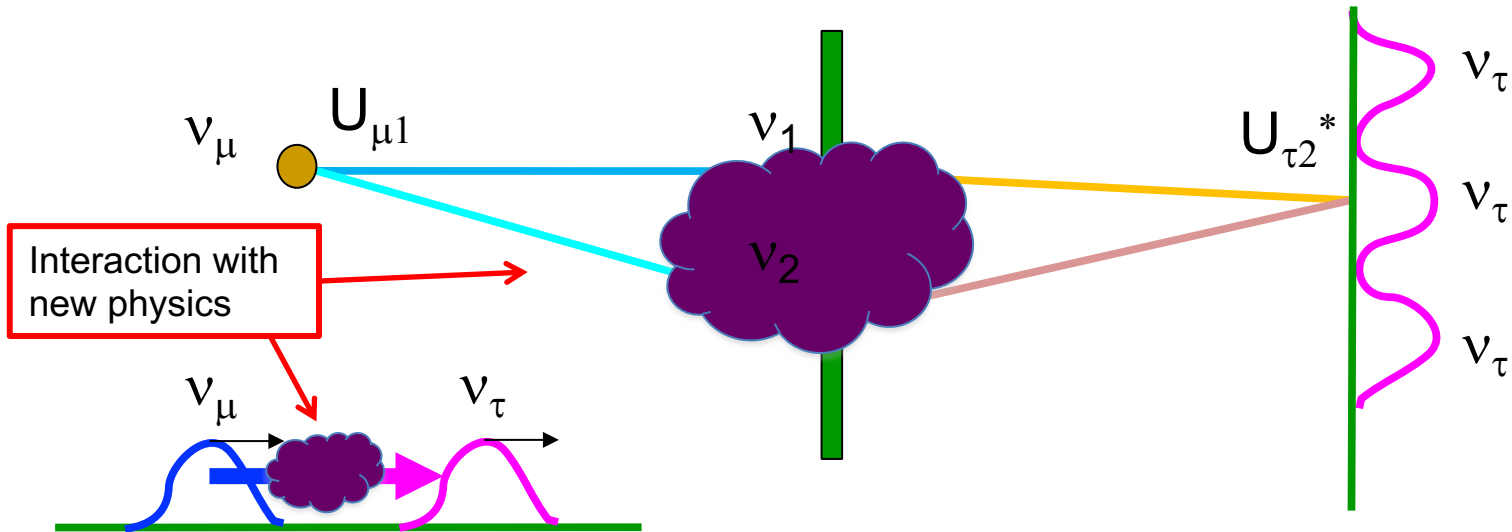
Neutrinos are produced in flavour eigenstates, but they propagate as Hamiltonian eigenstates, then detected in flavour eigenstates

If ν_1 and ν_2 , have different masses, they have different velocity and they don't overlap exactly at the detection

Neutrino flavour carries an information of immeasurably tiny neutrino masses

2. Neutrino interferometry for new physics search

Neutrino flavour conversion is an interference experiment



Neutrinos are produced in flavour eigenstates, and they propagate as Hamiltonian eigenstates, then detected in flavour eigenstates

If neutrinos couple with new physics in vacuum, this modifies neutrino flavour. The sensitivity of “**neutrino interferometry**” can go beyond precise atomic and optical interferometers.

Longer propagation length

- LIGO = 4km,
- Astrophysical neutrinos >100Mpc

Higher energy

- LHC ~ 7 TeV
- Astrophysical neutrinos ~ 1000 TeV

2. High-energy astrophysical neutrinos

High-energy particles (>60 TeV) propagating a long distance (>100 Mpc)
- Neutrinos can probe brave new spacetime!

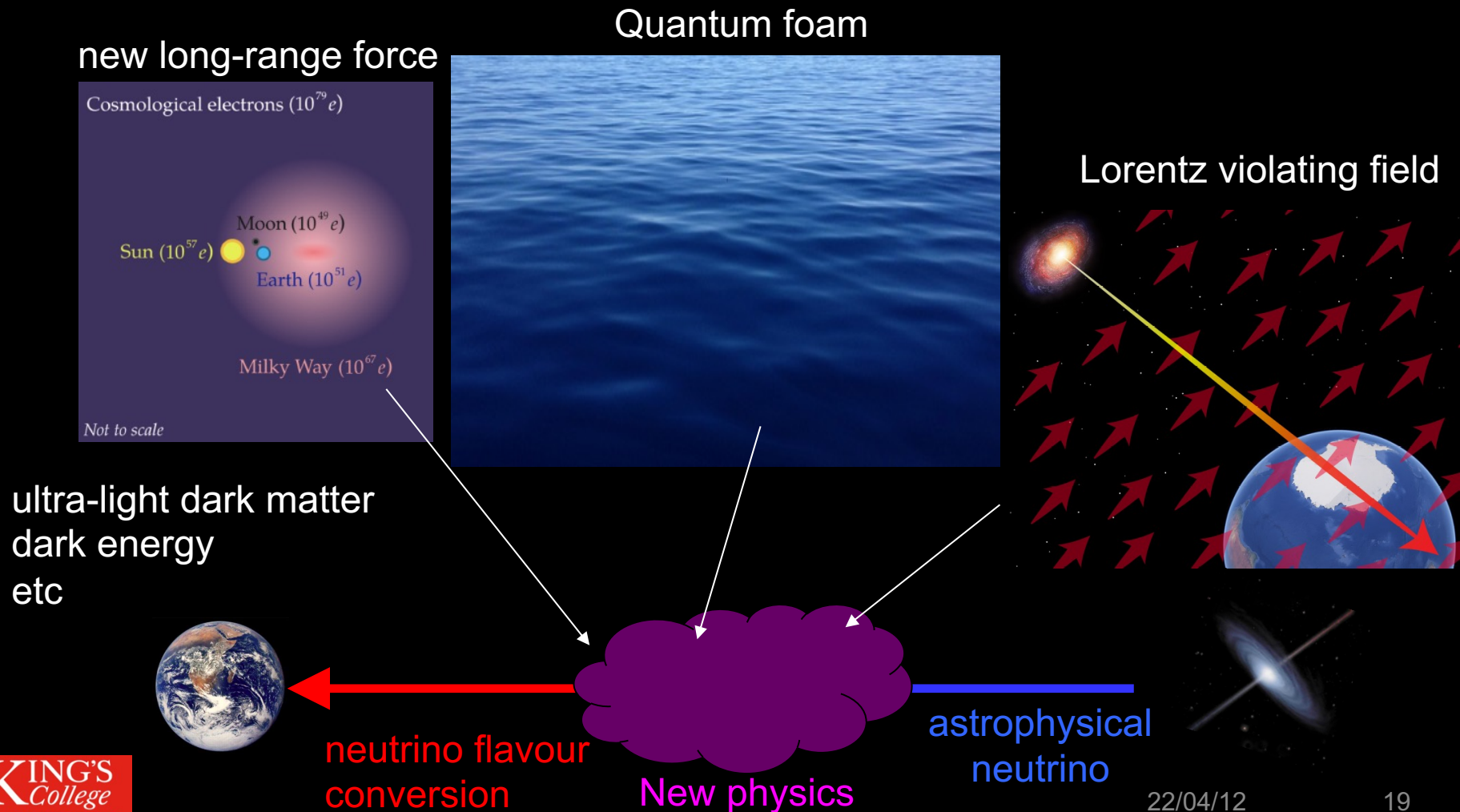


astrophysical
neutrino



2. High-energy astrophysical neutrinos

High-energy particles (>60 TeV) propagating a long distance (>100 Mpc)
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2. Flavor new physics search with effective operators

Standard Model Extension (SME) is an effective field theory to look for Lorentz violation

$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu \psi + \bar{\psi}\gamma^\mu c_{\mu\nu}\partial^\nu\psi \dots$$

Standard Model New physics

Effective Hamiltonian can be written from here

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} \dots$$

Standard Model New physics (renormalizable) higher dimension operator (non-renormalizable)

$E^3 c_{\alpha\beta}^{(6)} = E^3 \begin{pmatrix} c_{ee}^{(6)} & c_{e\mu}^{(6)} & c_{\tau e}^{(6)} \\ c_{e\mu}^{(6)*} & c_{\mu\mu}^{(6)} & c_{\mu\tau}^{(6)} \\ c_{\tau e}^{(6)*} & c_{\mu\tau}^{(6)*} & c_{\tau\tau}^{(6)} \end{pmatrix}$

IceCube is sensitive to higher dimension operators

dimension-6 operator natural scale: $c^{(6)} \sim \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$

2. Neutrino interferometry – Atmospheric neutrinos

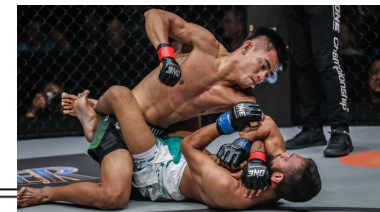
dim.	method	type	sector	limits	ref.
3	CMB polarization	astrophysical	photon	$\sim 10^{-43}$ GeV	[6]
	He-Xe comagnetometer	tabletop	neutron	$\sim 10^{-34}$ GeV	[10]
	torsion pendulum	tabletop	electron	$\sim 10^{-31}$ GeV	[12]
	muon g-2	accelerator	muon	$\sim 10^{-24}$ GeV	[13]
	neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{a}_{\mu\tau}^{(3)}) , \text{Im}(\hat{a}_{\mu\tau}^{(3)}) < 2.9 \times 10^{-24}$ GeV (99% C.L.) $< 2.0 \times 10^{-24}$ GeV (90% C.L.)	this work
4	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-38}$	[7]
	Laser interferometer	LIGO	photon	$\sim 10^{-22}$	[8]
	Sapphire cavity oscillator	tabletop	photon	$\sim 10^{-18}$	[5]
	Ne-Rb-K comagnetometer	tabletop	neutron	$\sim 10^{-29}$	[11]
	trapped Ca^+ ion	tabletop	electron	$\sim 10^{-19}$	[14]
neutrino oscillation	atmospheric	neutrino	$ \text{Re}(\hat{c}_{\mu\tau}^{(4)}) , \text{Im}(\hat{c}_{\mu\tau}^{(4)}) < 3.9 \times 10^{-28}$ (99% C.L.) $< 2.7 \times 10^{-28}$ (90% C.L.)	this work	
5	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-34}$ GeV^{-1}	[7]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-22}$ to 10^{-18} GeV^{-1}	[9]
	neutrino oscillation	atmospheric	neutrino	$\text{Re}(\hat{a}_{\mu\tau}^{(5)}) , \text{Im}(\hat{a}_{\mu\tau}^{(5)}) < 2.3 \times 10^{-32}$ GeV^{-1} (99% C.L.) $< 1.5 \times 10^{-32}$ GeV^{-1} (90% C.L.)	this work
6	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-31}$ GeV^{-2}	[7]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-42}$ to 10^{-35} GeV^{-2}	[9]
	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-31}$ GeV^{-2}	[15]
	neutrino oscillation	atmospheric	neutrino	$\text{Re}(\hat{c}_{\mu\tau}^{(6)}) , \text{Im}(\hat{c}_{\mu\tau}^{(6)}) < 1.5 \times 10^{-36}$ GeV^{-2} (99% C.L.) $< 9.1 \times 10^{-37}$ GeV^{-2} (90% C.L.)	this work
7	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-28}$ GeV^{-3}	[7]
	neutrino oscillation	atmospheric	neutrino	$\text{Re}(\hat{a}_{\mu\tau}^{(7)}) , \text{Im}(\hat{a}_{\mu\tau}^{(7)}) < 8.3 \times 10^{-41}$ GeV^{-3} (99% C.L.) $< 3.6 \times 10^{-41}$ GeV^{-3} (90% C.L.)	this work
8	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-46}$ GeV^{-4}	[15]
	neutrino oscillation	atmospheric	neutrino	$\text{Re}(\hat{c}_{\mu\tau}^{(8)}) , \text{Im}(\hat{c}_{\mu\tau}^{(8)}) < 5.2 \times 10^{-45}$ GeV^{-4} (99% C.L.) $< 1.4 \times 10^{-45}$ GeV^{-4} (90% C.L.)	this work

TABLE I: Comparison of attainable best limits of SME coefficients in various fields.

IceCube atmospheric neutrino limit, $c^{(6)} < 10^{-36} \text{GeV}^{-2}$

Astrophysical neutrino sensitivity reach the benchmark value, $c^{(6)} \sim 1/M_p^2 \sim 10^{-38} \text{GeV}^{-2}$

2. Neutrino interferometry – Atmospheric neutrinos

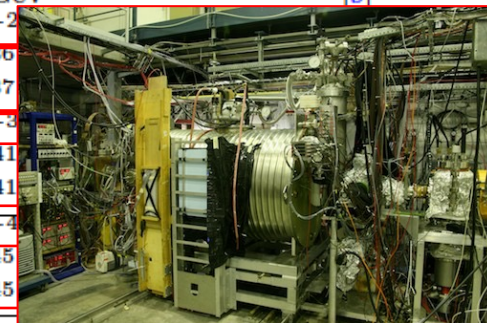
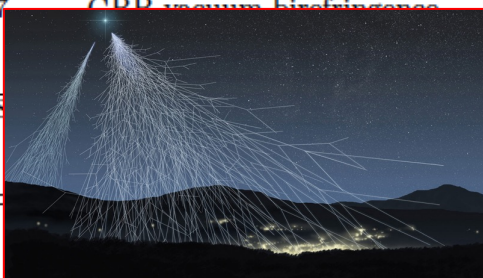


Physics MMA

[13]

this work

dim.	method	type	limits
3	GRB	astrophysical	$\sim 10^{-43}$ GeV
4	tabletop	tabletop	$\sim 10^{-34}$ GeV
4	tabletop	tabletop	$\sim 10^{-31}$ GeV
4	accelerator	accelerator	$\sim 10^{-24}$ GeV
4	atmospheric	atmospheric	$< 2.9 \times 10^{-24}$ GeV (99% C.L.)
4			$< 2.0 \times 10^{-24}$ GeV (90% C.L.)
4			$\sim 10^{-38}$
4	LIGO	astrophysical	[7]
4	neutrino oscillation	astrophysical	[8]
4		tabletop	[5]
4		tabletop	[11]
4		tabletop	[14]
4		atmospheric	this work
5	neutrino oscillation	astrophysical	[7]
5		astrophysical	[9]
5		atmospheric	this work
6		astrophysical	[7]
6		astrophysical	[9]
6		atmospheric	this work
6		astrophysical	[7]
6		astrophysical	[9]
6		atmospheric	$< 1.5 \times 10^{-36}$
6		atmospheric	$< 9.1 \times 10^{-37}$
6		atmospheric	10^{-28} GeV ⁻³
6		atmospheric	$< 8.3 \times 10^{-41}$
6		atmospheric	$< 3.6 \times 10^{-41}$
6		atmospheric	10^{-46} GeV ⁻⁴
6		atmospheric	$< 5.2 \times 10^{-45}$
6		atmospheric	$< 1.4 \times 10^{-45}$
6		astrophysical	comparison of attainable best limits of SMNS coefficients in various fields.



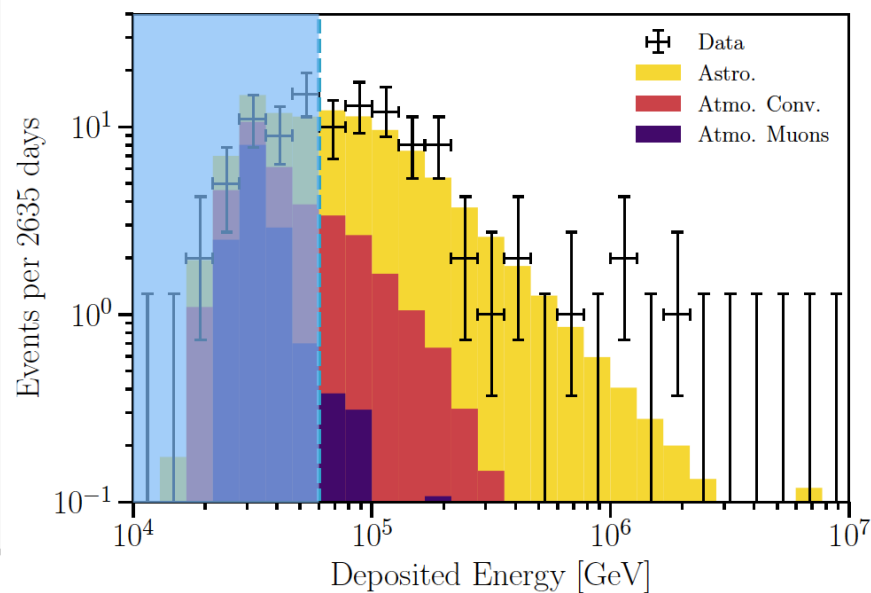
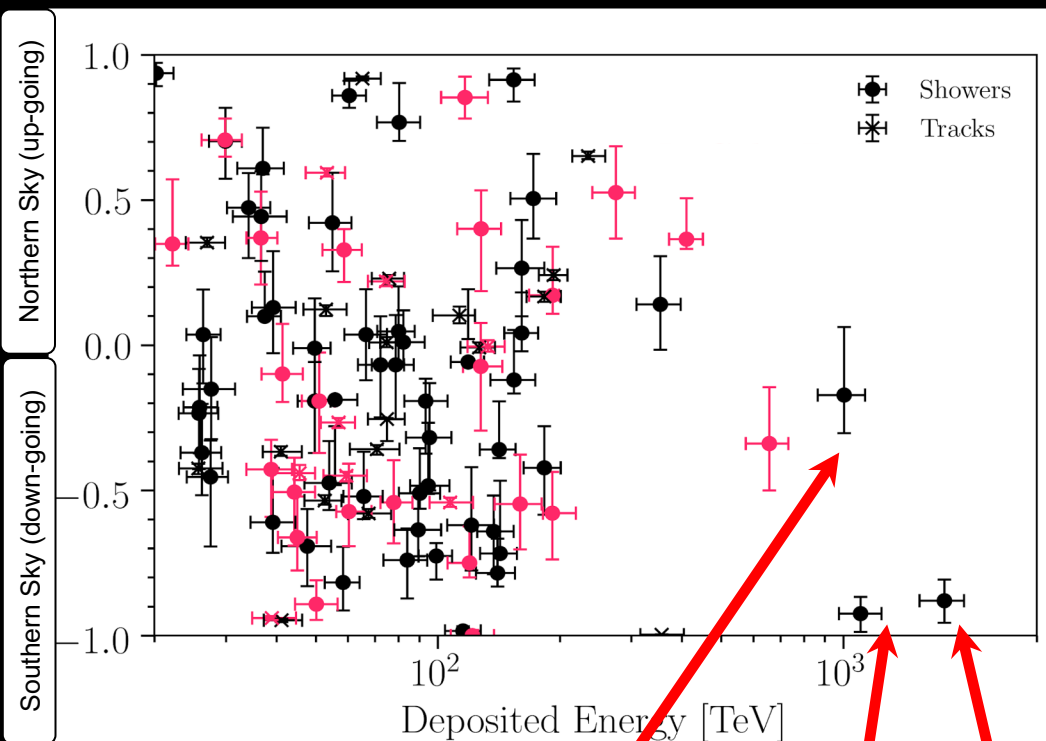
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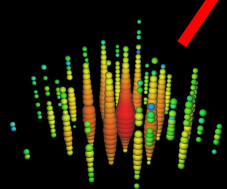
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2. Neutrino interferometry with IceCube
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3. High-energy astrophysical neutrinos

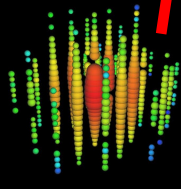
60-2000 TeV astrophysical neutrinos have been observed by IceCube Neutrino Observatory



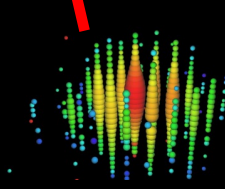
“Bert”
1.1 PeV



“Ernie”
1.0 PeV



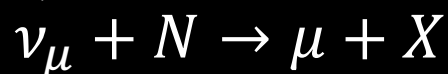
“Big Bird”
2.0 PeV



3. IceCube event morphology

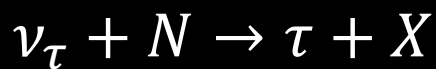
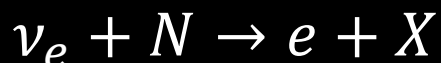
Track

ν_μ CC



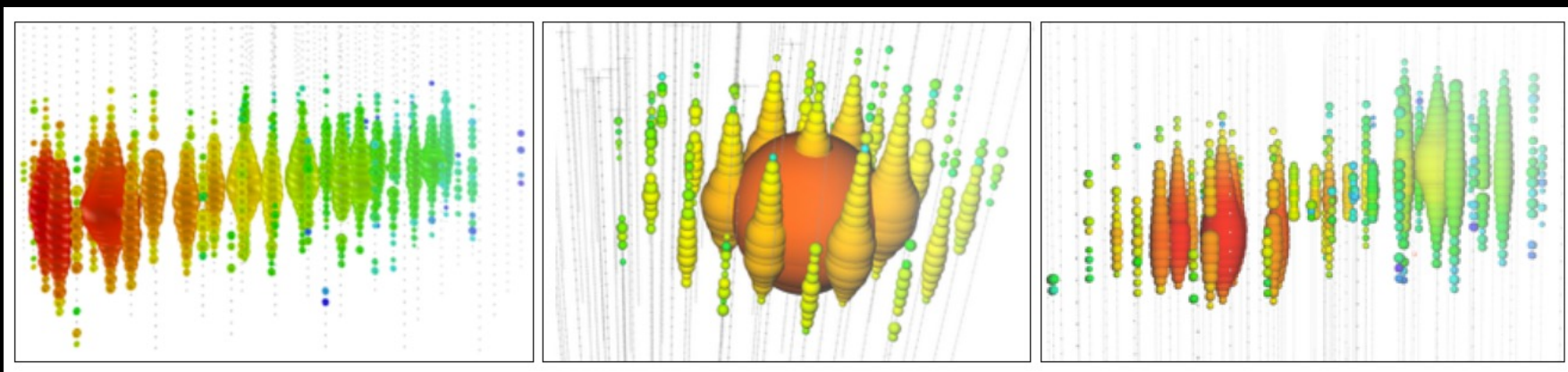
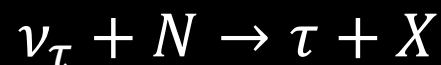
Cascade

ν_e CC, ν_τ CC, NC



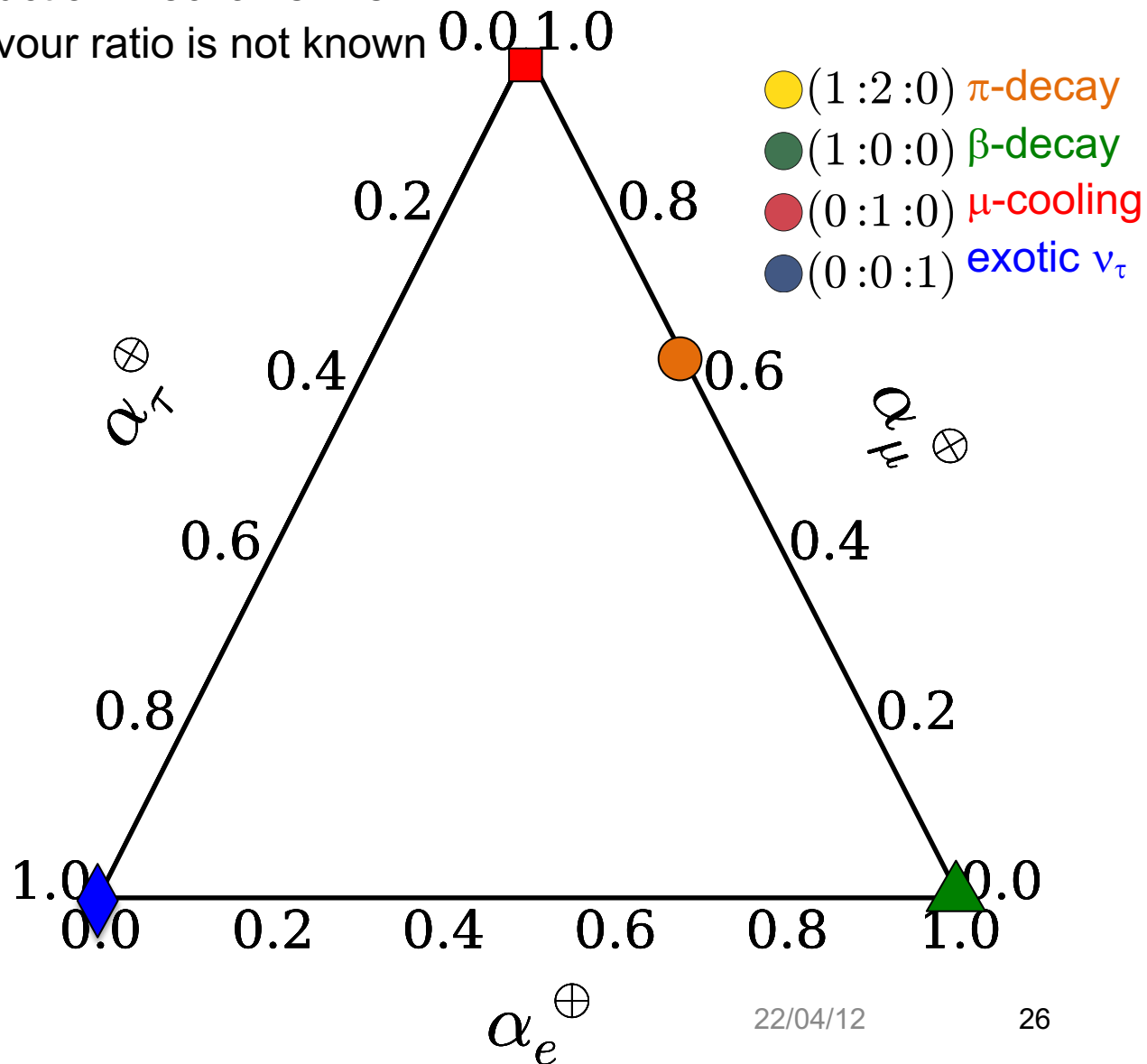
Double cascade

ν_τ CC ($L \sim 50 \text{m} \cdot E/\text{PeV}$)



3. Neutrino flavor ratio ($\nu_e : \nu_\mu : \nu_\tau$)

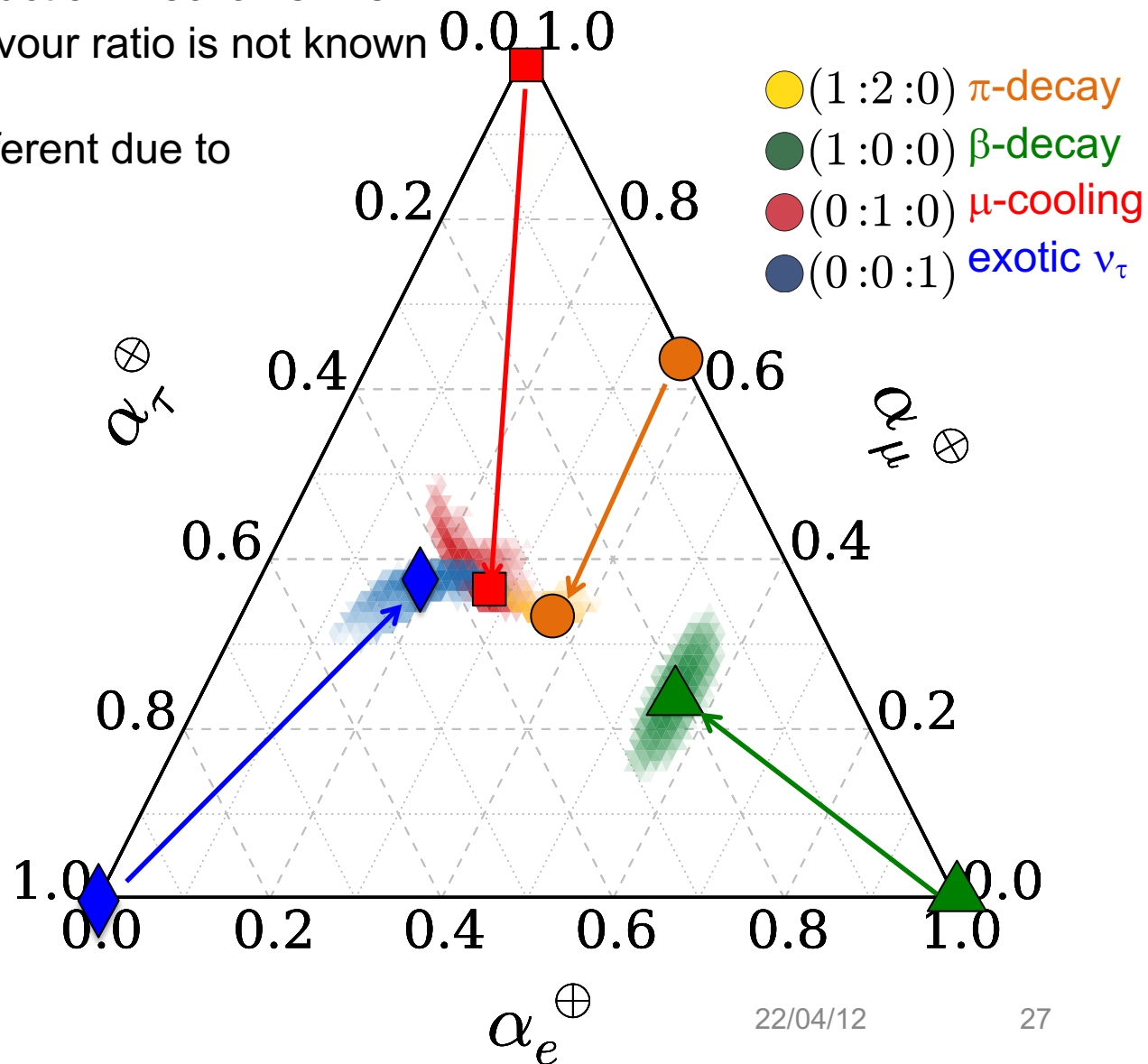
Astrophysical neutrino production mechanism is not known \rightarrow production flavour ratio is not known



3. Neutrino flavor ratio ($\nu_e : \nu_\mu : \nu_\tau$)

Astrophysical neutrino production mechanism is not known \rightarrow production flavour ratio is not known

Flavour ratio on Earth is different due to mixing by neutrino masses

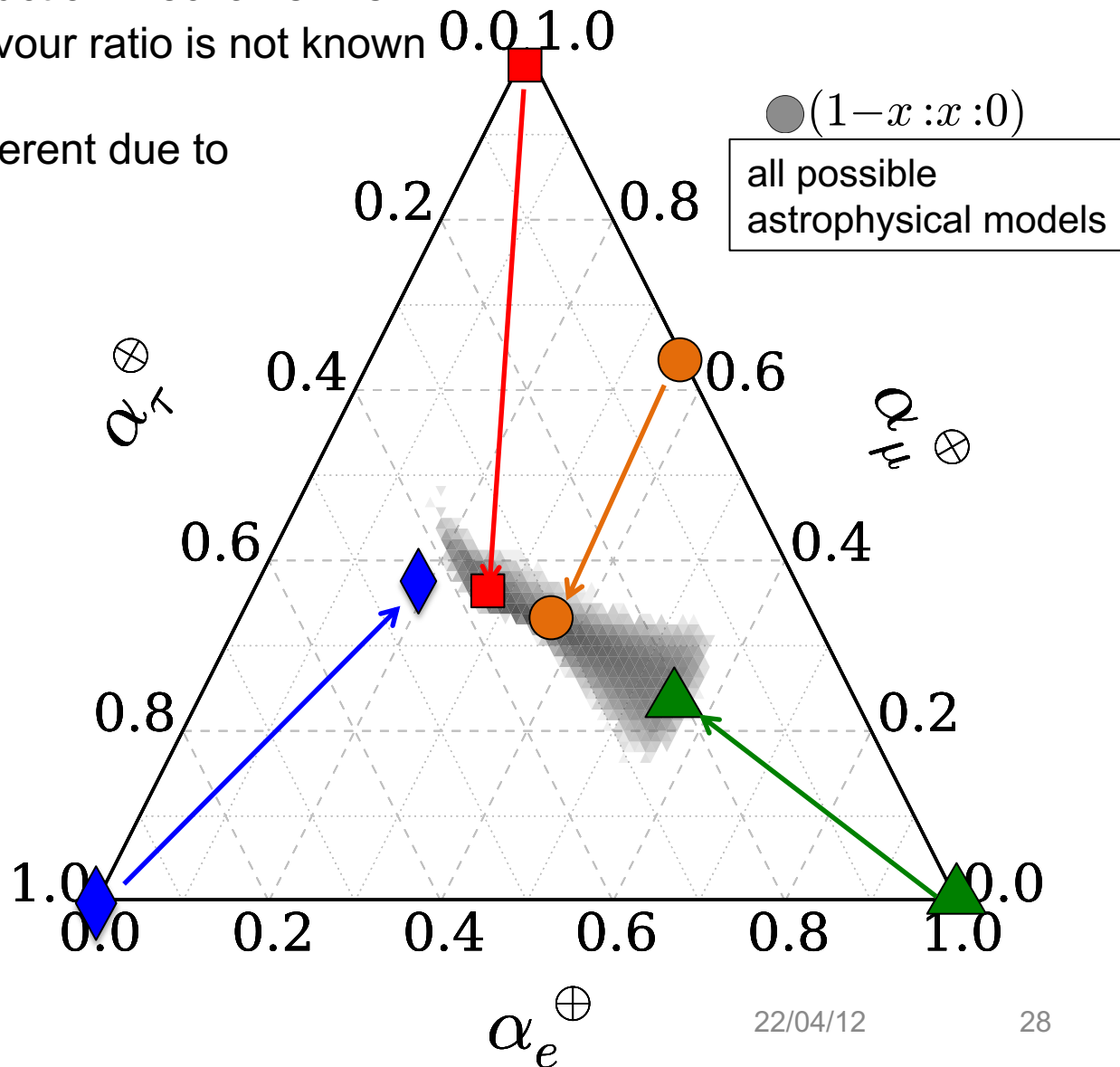


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All possible flavour ratio is confined in a small space



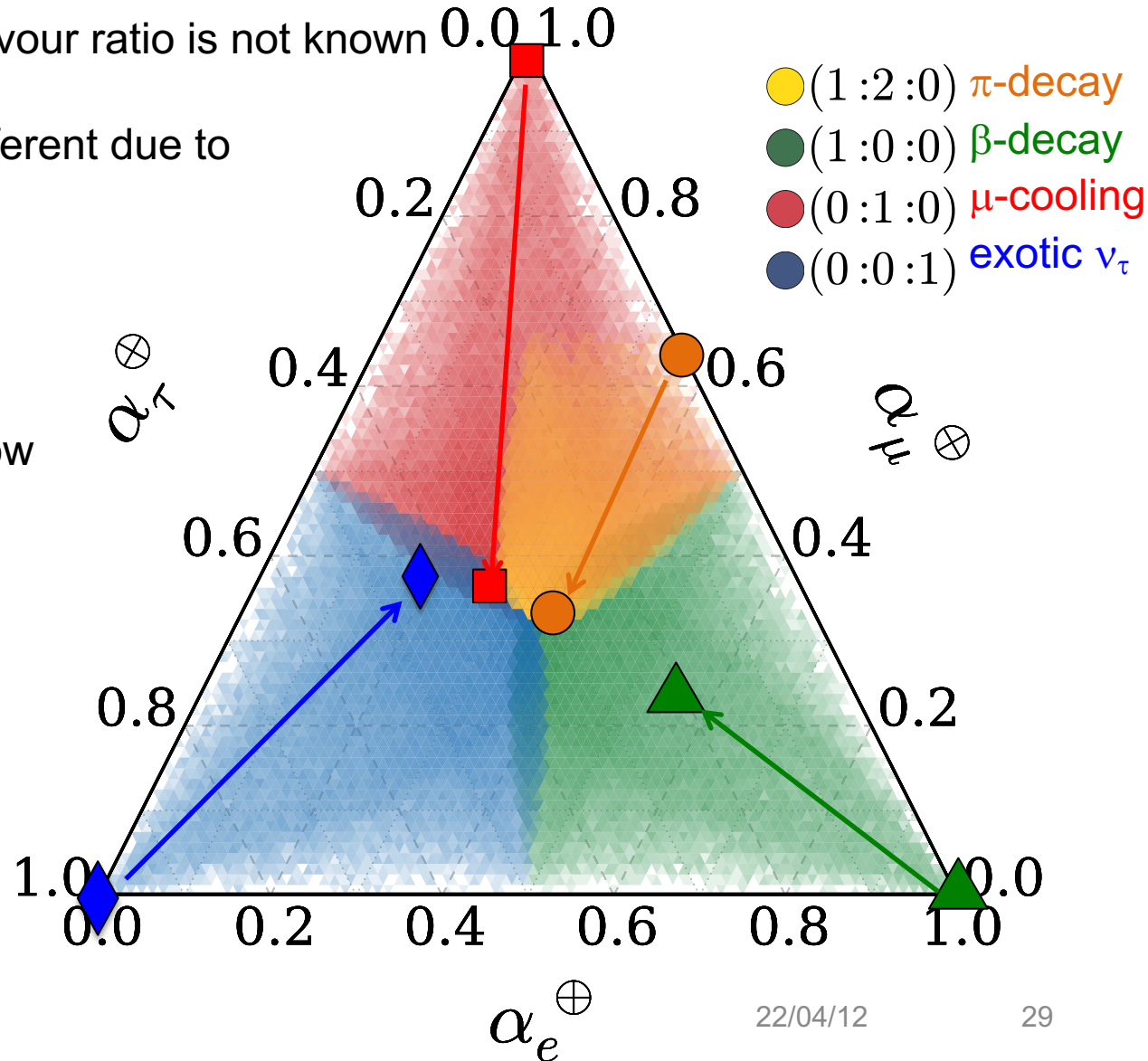
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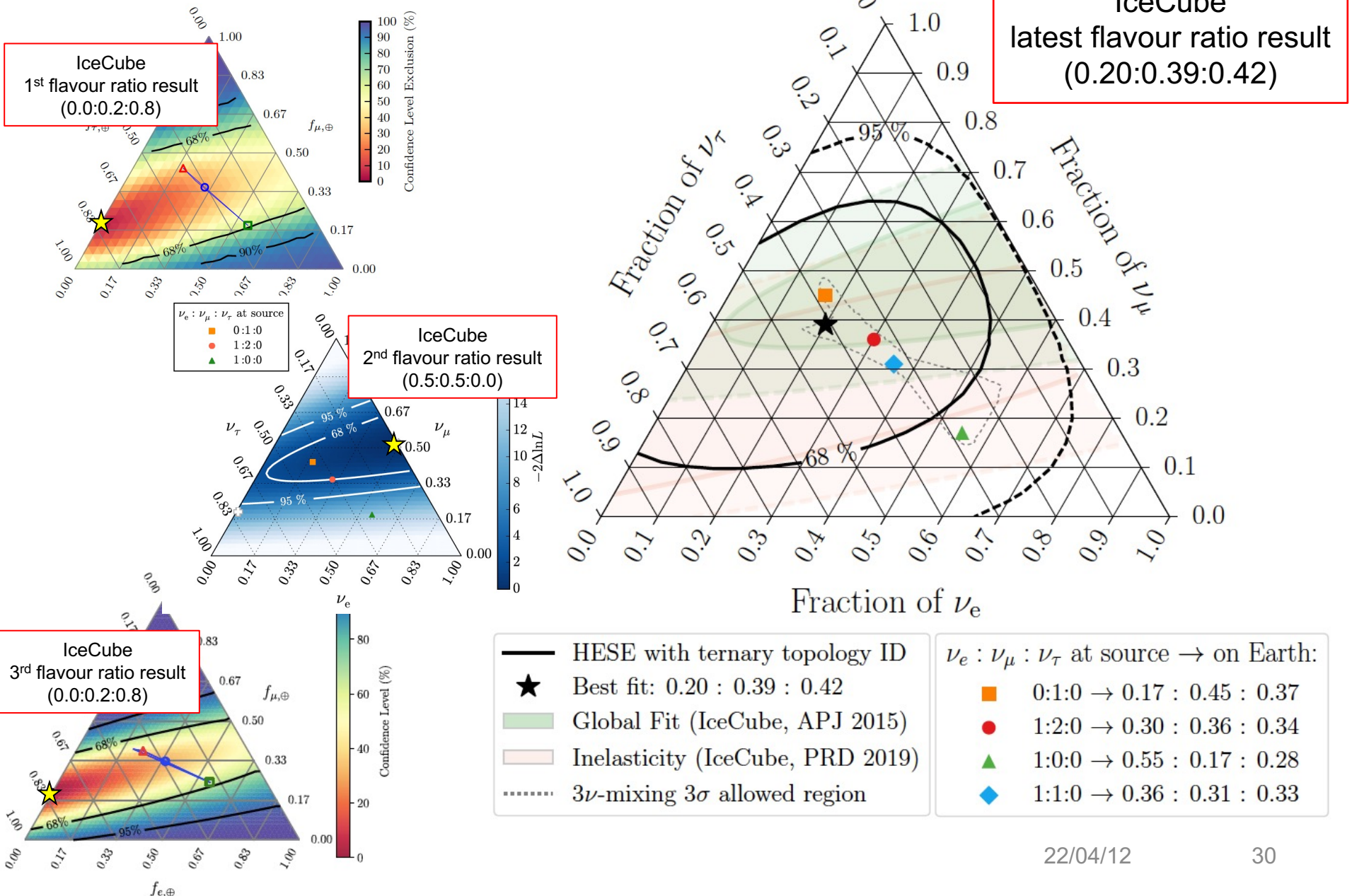
Flavour ratio on Earth is different due to mixing by neutrino masses

All possible flavour ratio is confined in a small space

e.g.) New physics just below the limit can produce any flavour ratio



3. HESE 7.5-yr flavor ratio



3. HESE 7.5-yr flavor ratio

60 HESE events in 60 TeV – 2 PeV
First identification of tau neutrinos

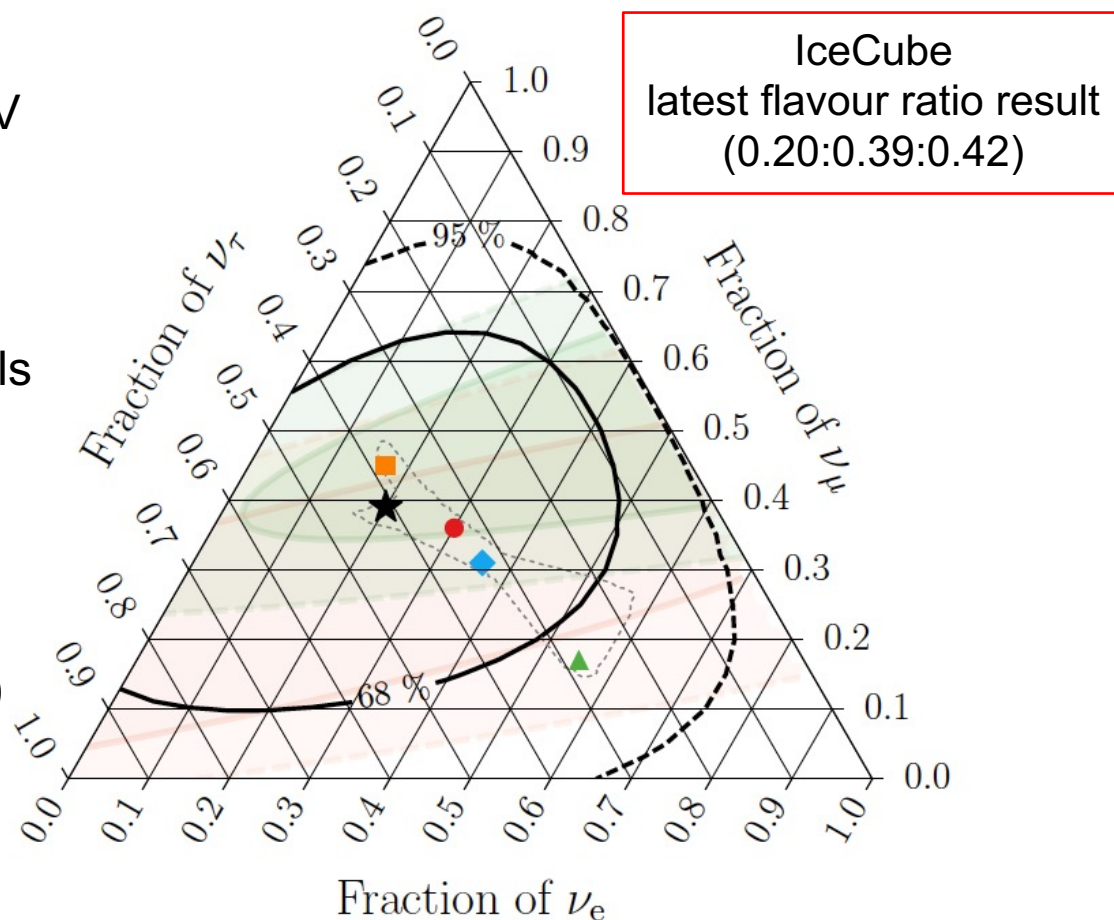
New flavour ratio measurement

- contour is too big, most of models are accepted by data

We will not find new physics

We need;

- higher statistics (IceCube-Gen2)
- better PID (software)



— HESE with ternary topology ID
★ Best fit: 0.20 : 0.39 : 0.42
■ Global Fit (IceCube, APJ 2015)
■ Inelasticity (IceCube, PRD 2019)
⋯⋯⋯ 3ν-mixing 3σ allowed region

$\nu_e : \nu_\mu : \nu_\tau$ at source \rightarrow on Earth:
■ 0:1:0 \rightarrow 0.17 : 0.45 : 0.37
● 1:2:0 \rightarrow 0.30 : 0.36 : 0.34
▲ 1:0:0 \rightarrow 0.55 : 0.17 : 0.28
◆ 1:1:0 \rightarrow 0.36 : 0.31 : 0.33

3. HESE 7.5-yr flavor ratio

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New flavour ratio measurement

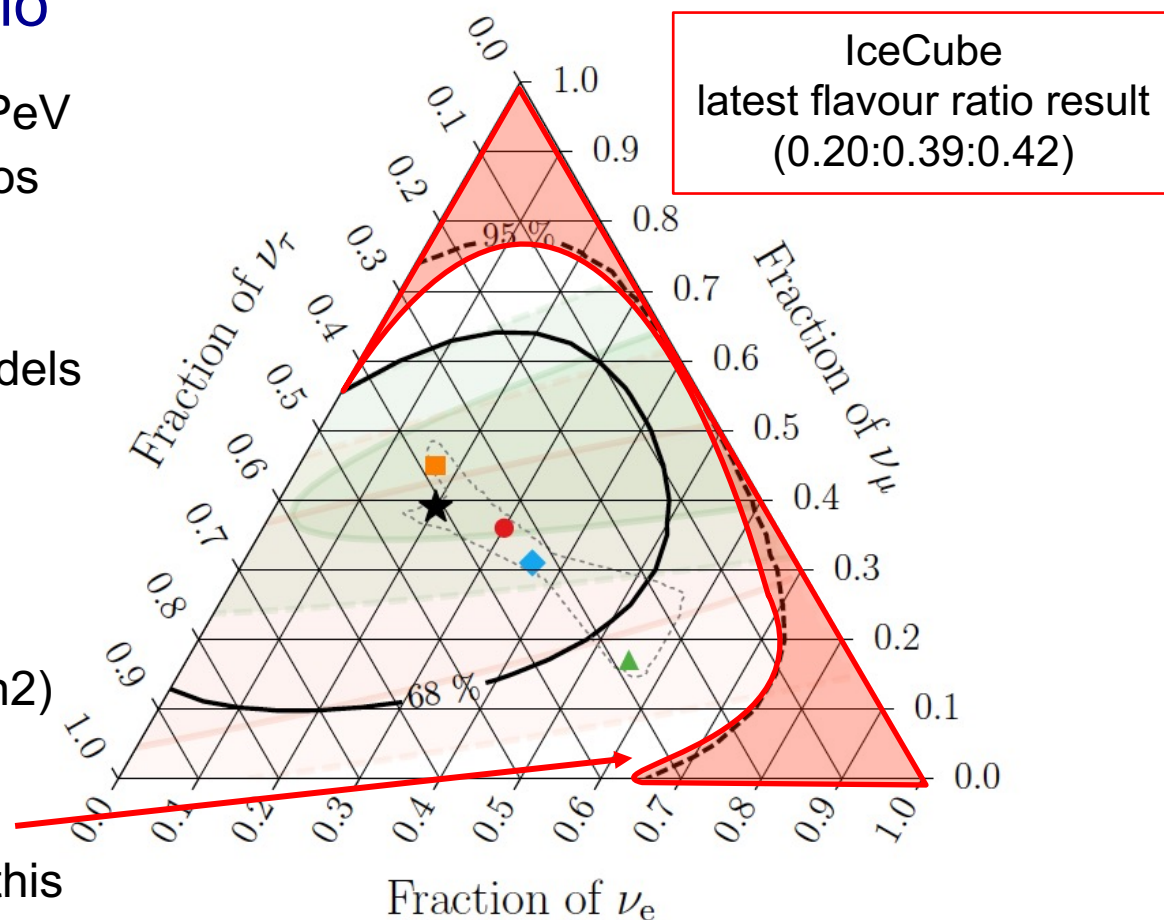
- contour is too big, most of models are accepted by data

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Models predict flavour ratios at this region can be rejected



	HESE with ternary topology ID	$\nu_e : \nu_\mu : \nu_\tau$ at source \rightarrow on Earth:
	Best fit: 0.20 : 0.39 : 0.42	0:1:0 \rightarrow 0.17 : 0.45 : 0.37
	Global Fit (IceCube, APJ 2015)	1:2:0 \rightarrow 0.30 : 0.36 : 0.34
	Inelasticity (IceCube, PRD 2019)	1:0:0 \rightarrow 0.55 : 0.17 : 0.28
	3ν -mixing 3σ allowed region	1:1:0 \rightarrow 0.36 : 0.31 : 0.33

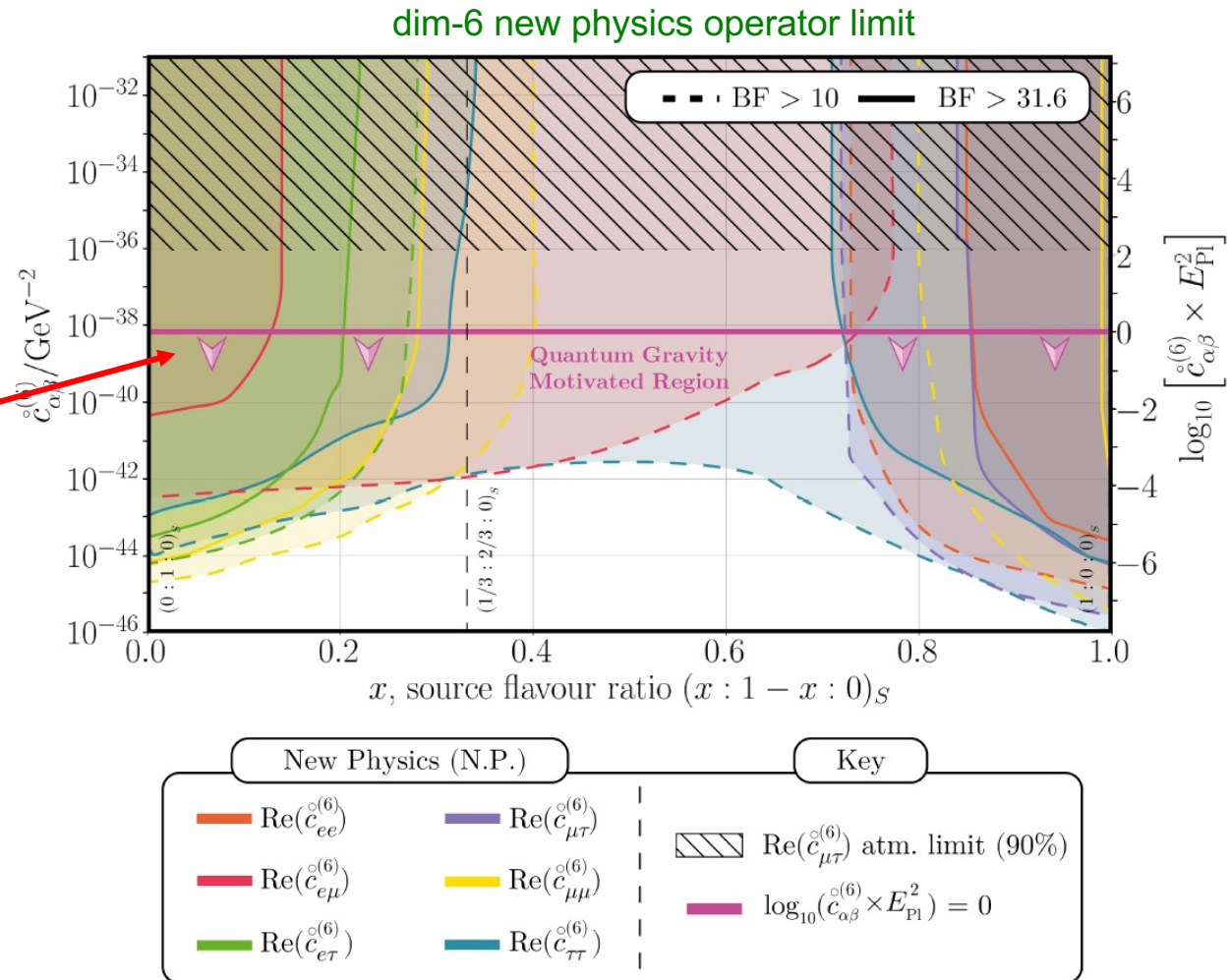
3. HESE 7.5-yr flavor new physics search

60 HESE events in 60 TeV – 2 PeV

First identification of tau neutrinos

Strong limits for many parameters depending on assumed initial flavour ratio

$$1/M_P^2 \sim 10^{-38} \text{ GeV}^{-2}$$



3. HESE 7.5-yr flavor new physics search

60 HESE events in 60 TeV – 2 PeV

First identification of tau neutrinos

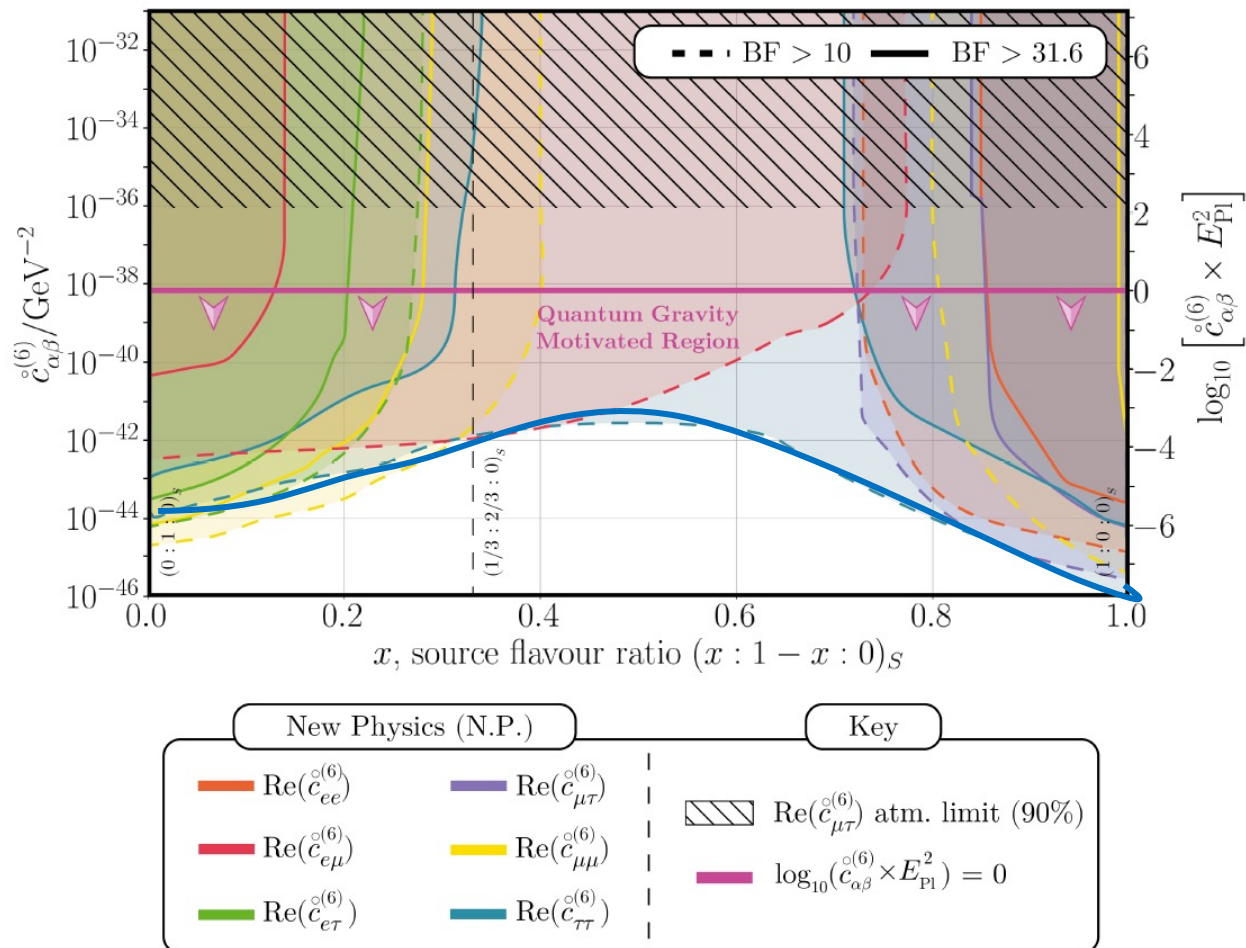
Strong limits for many parameters depending on assumed initial flavour ratio

We obtain model-independent limits for $c_{\tau\tau}^{(6)}$

dim coefficient limit (BF > 10.0)

3	$\text{Re}(\hat{a}_{\tau\tau}^{(3)})$	$2 \times 10^{-26} \text{ GeV}$
4	$\text{Re}(\hat{c}_{\tau\tau}^{(4)})$	2×10^{-31}
5	$\text{Re}(\hat{a}_{\tau\tau}^{(5)})$	$2 \times 10^{-37} \text{ GeV}^{-1}$
6	$\text{Re}(\hat{c}_{\tau\tau}^{(6)})$	$3 \times 10^{-42} \text{ GeV}^{-2}$
7	$\text{Re}(\hat{a}_{\tau\tau}^{(7)})$	$3 \times 10^{-47} \text{ GeV}^{-3}$
8	$\text{Re}(\hat{c}_{\tau\tau}^{(8)})$	$2 \times 10^{-52} \text{ GeV}^{-4}$

dim-6 new physics operator limit

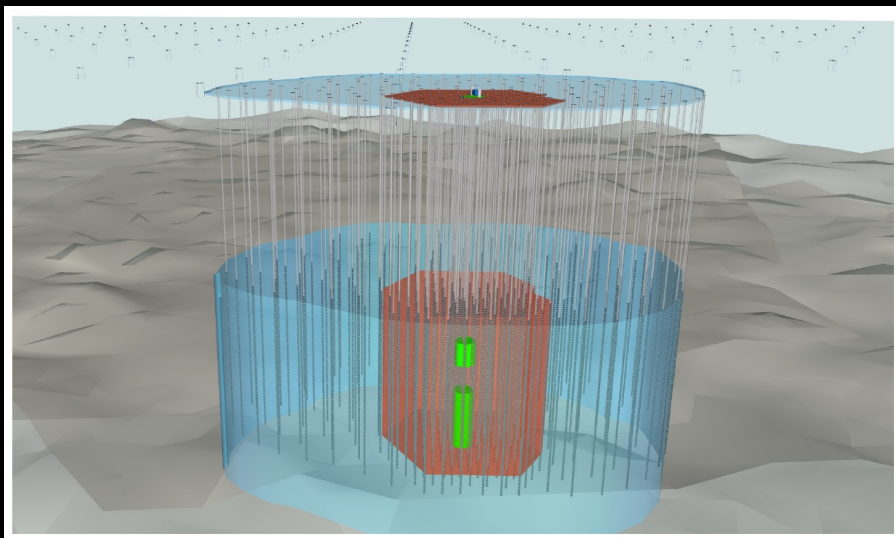




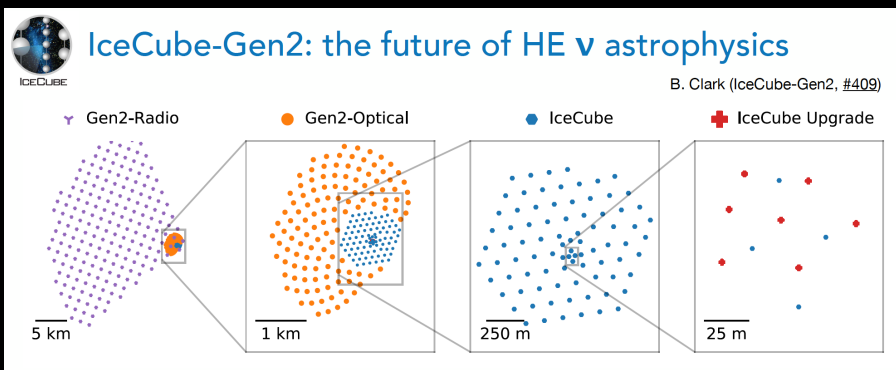
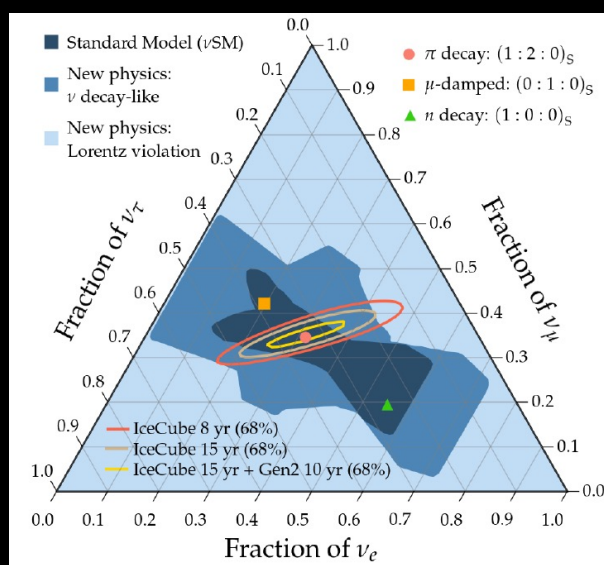
ICECUBE
GEN2

3. IceCube-Gen2

Larger separation (125m \rightarrow \sim 200-300m) to cover larger volume
- 120 new strings with 100 sensors, 240 m separation, x10 coverage



IceCube-Gen2 flavour ratio sensitivity



The first stage of Gen2
(IceCube upgrade) is ongoing



22/04/12

Conclusion

Quantum gravity may create a new space-time structure in vacuum.

Neutrino interferometry is a powerful technique to look for new physics.

Astrophysical neutrino mixing sensitivity reaches to naïve expectation of Planck scale physics. We need more statistics and better particle identification algorithm to find quantum gravity motivated physics.

IceCube-Gen2 collaboration



Thank you for your attention!

22/04/12



Backup

Neutrino Standard Model (ν SM) - Unknowns

SM + 3 active massive neutrinos

Neutrinos are least known particles!

There are several unknowns and anomalies

→ Do they indicate new physics?

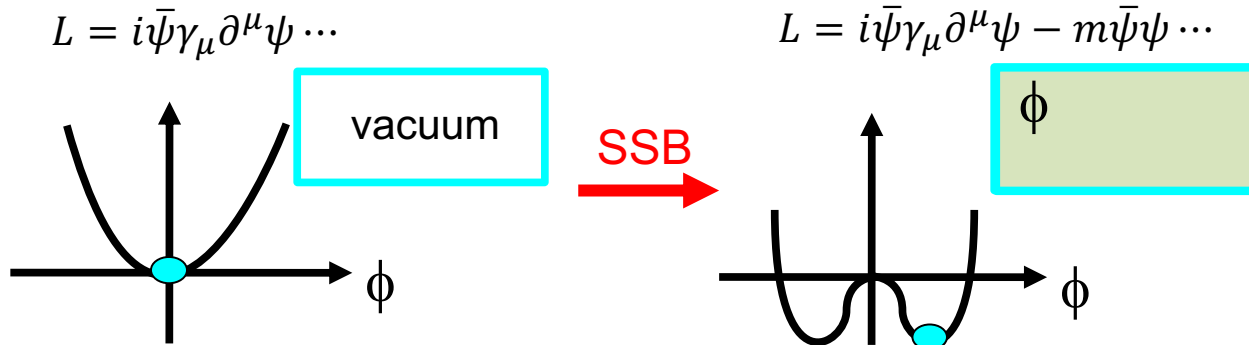
Unknown parameters of ν SM

1. Dirac CP phase
2. θ_{23} ($\theta_{23}=40^\circ$ and 50° are same for $\sin 2\theta_{23}$, but not for $\sin\theta_{23}$)
3. normal mass ordering $m_1 < m_2 < m_3$ or inverted mass ordering $m_3 < m_1 < m_2$
4. Dirac or Majorana
5. Majorana phase
6. Absolute neutrino mass

1. Spontaneous Lorentz symmetry breaking (SLSB)

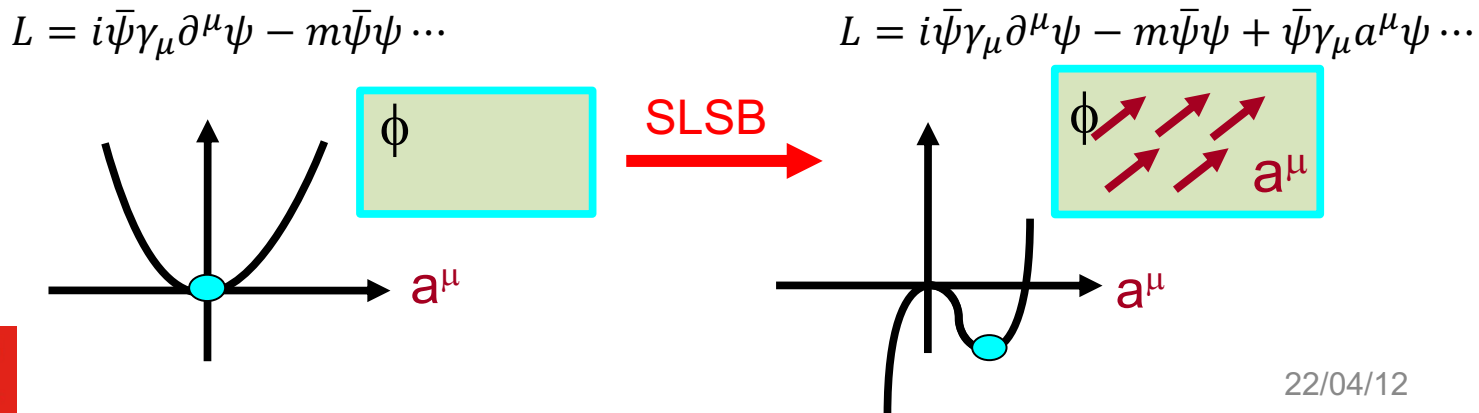
SSB of scalar field in Standard Model (SM)

- A scalar field generates vacuum expectation value (VEV), reason unknown
- Particle acquires mass term, spontaneously violating gauge invariance

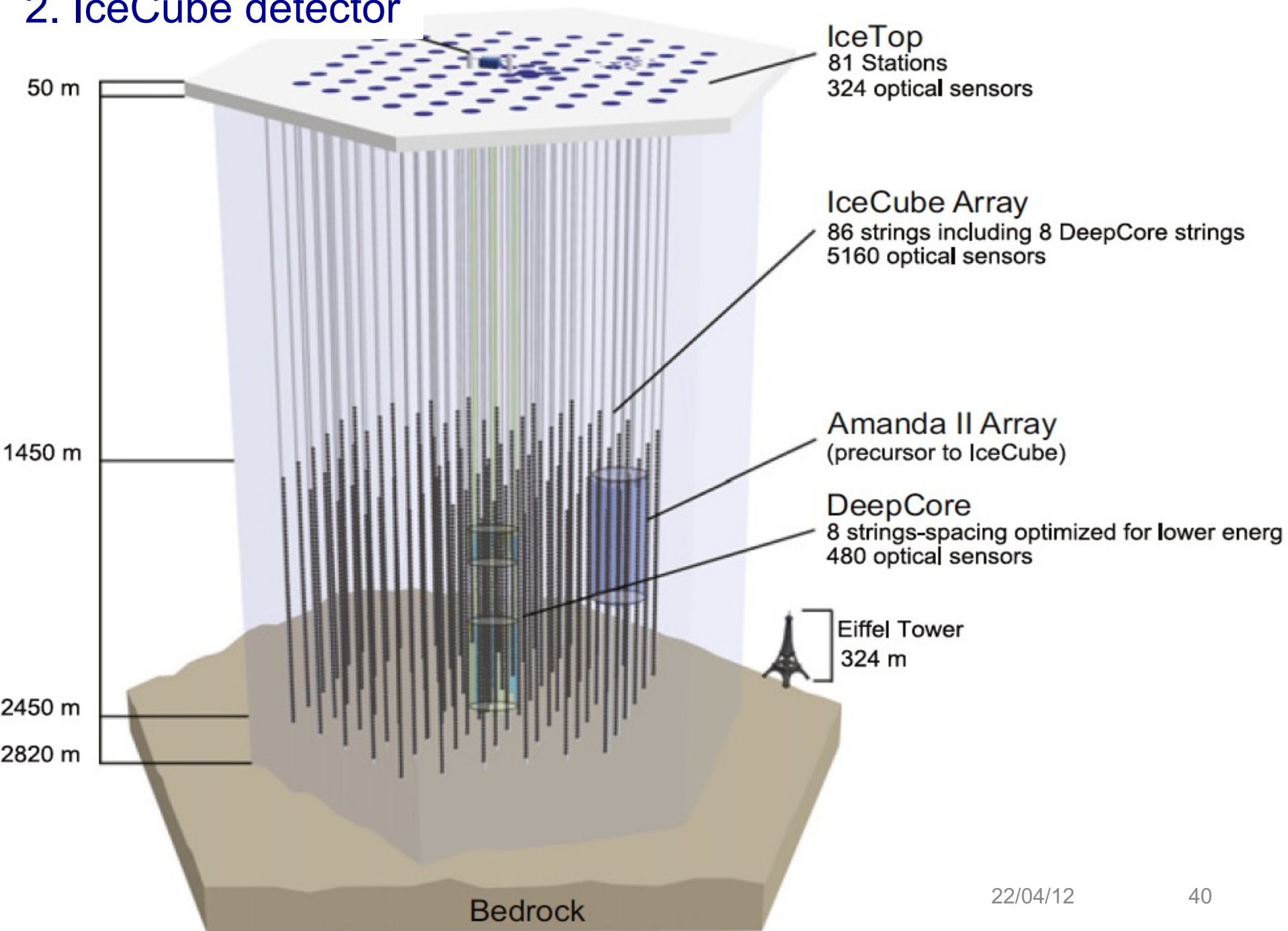


SLSB in string field theory

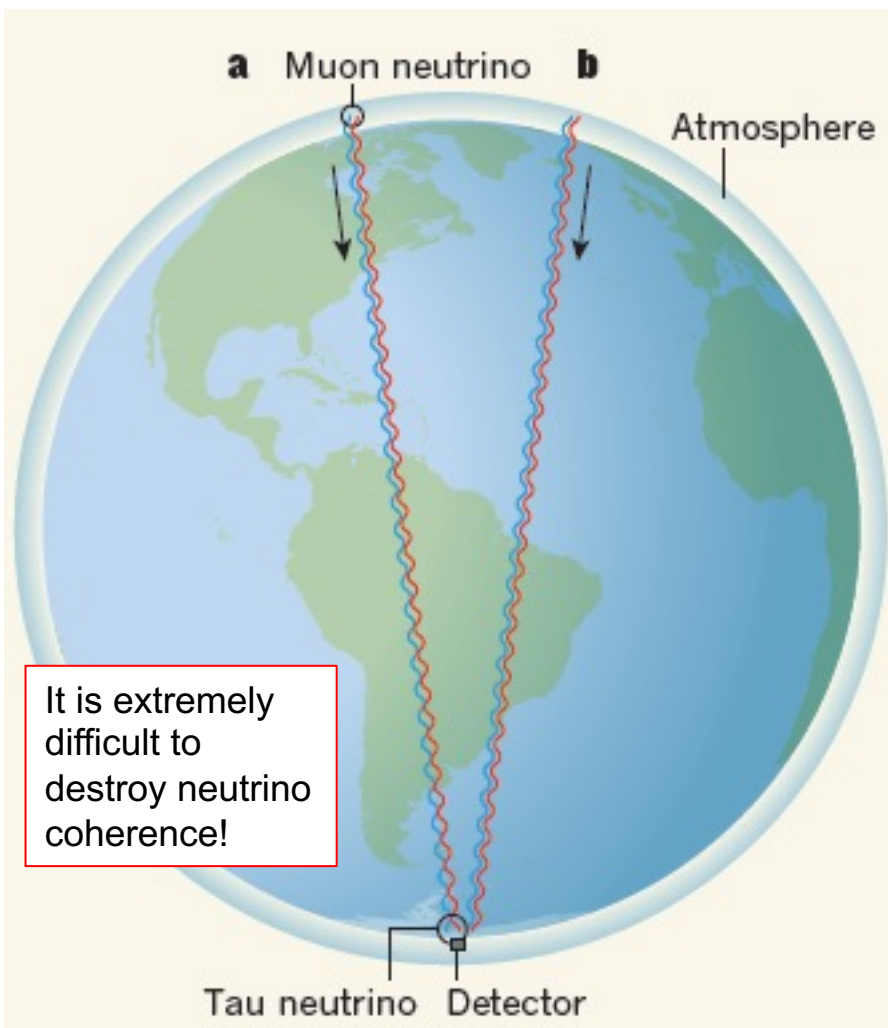
- Vector fields can generate VEVs
- Lorentz symmetry is spontaneously broken



2. IceCube detector



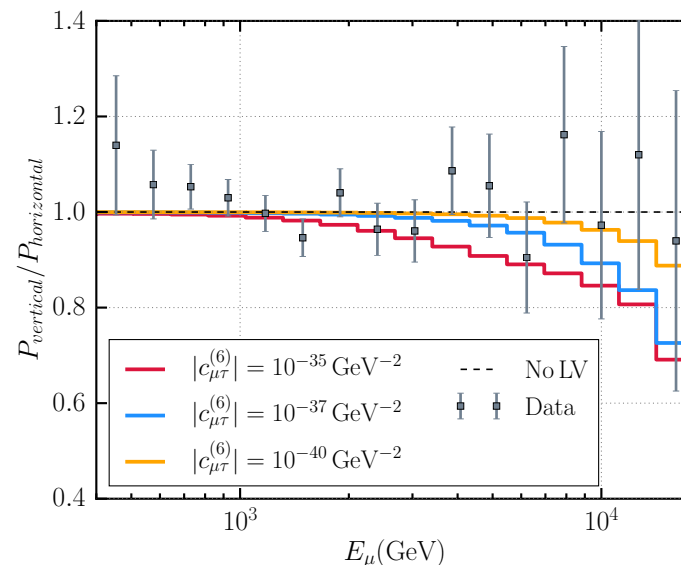
3. Neutrino interferometry – Atmospheric neutrinos



Neutrino oscillation is a nature interferometer. Any extra interactions in the Lagrangian contribute the phase shift

The highest energy - 20 TeV
The longest baseline - 12700km

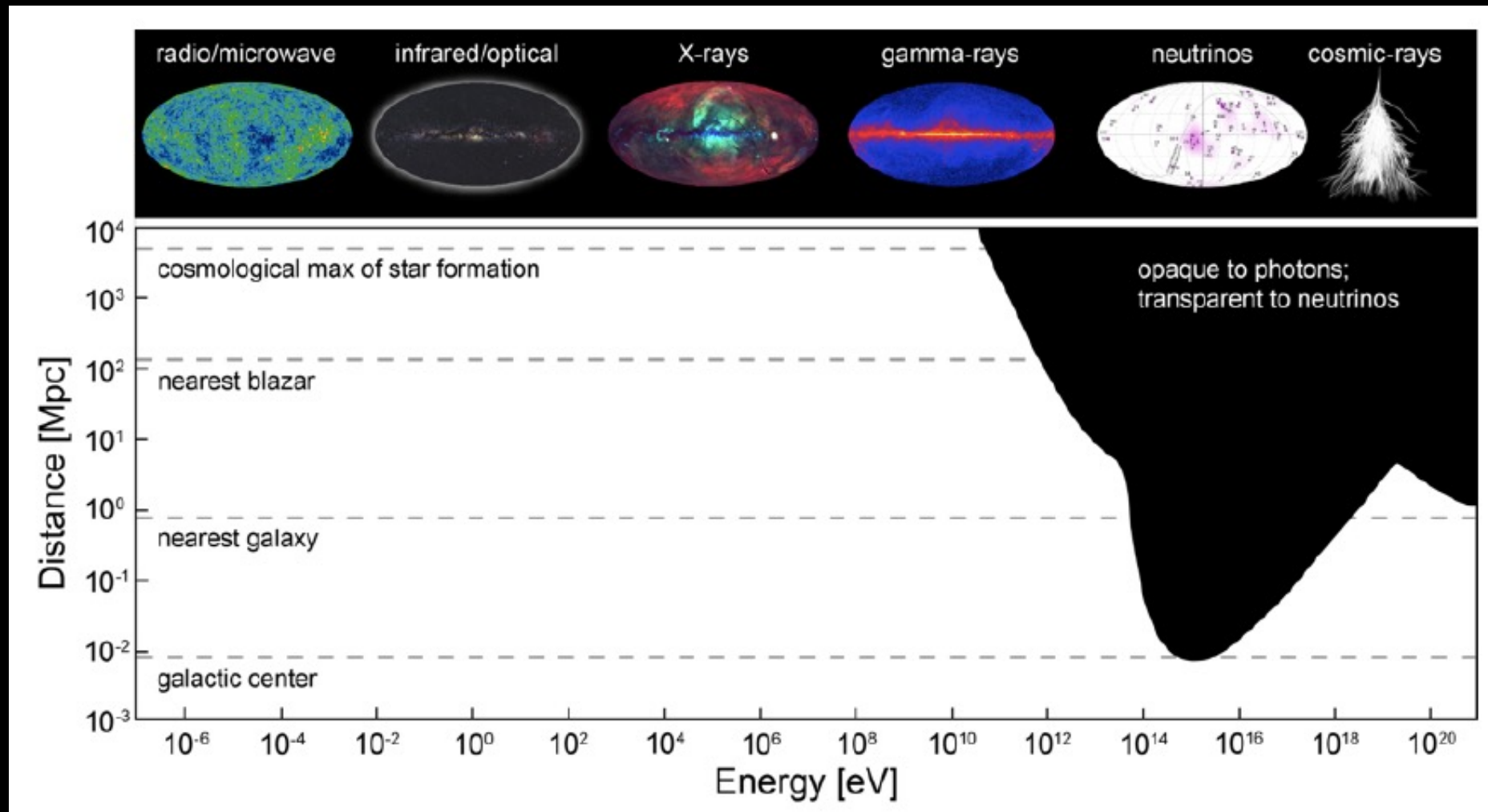
If anomalous coupling with neutrinos in vacuum cause a phase shift in similar order, we can see it from **spectrum distortion of atmospheric neutrinos**



IceCube atmospheric neutrino limit, $c^{(6)} < 10^{-36} GeV^{-2}$
This is close to the target signal region, $c^{(6)} \sim 10^{-38} GeV^{-2}$

2. High-energy astrophysical neutrinos

Above ~ 100 TeV, neutrinos are only particles pointing to their high-energy sources

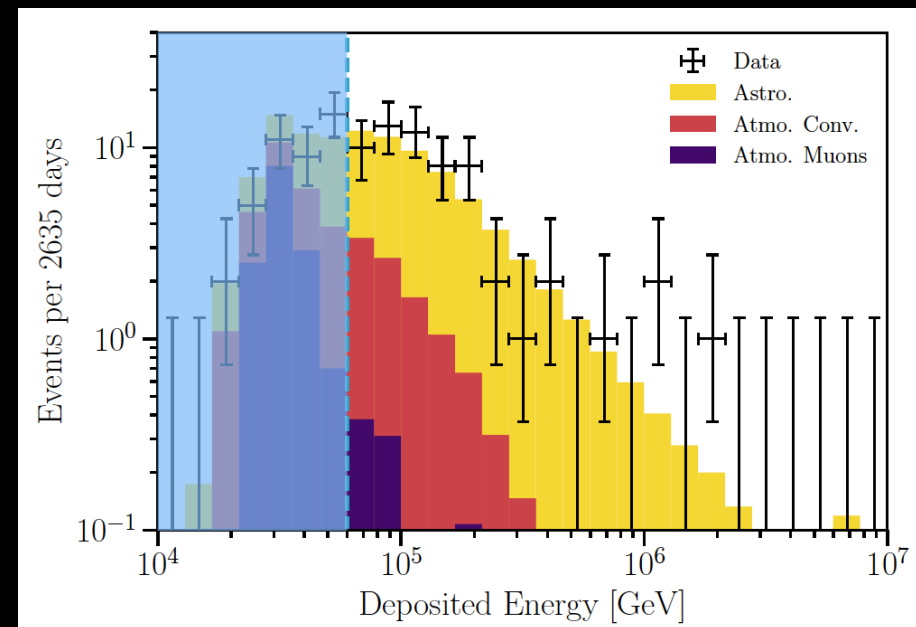
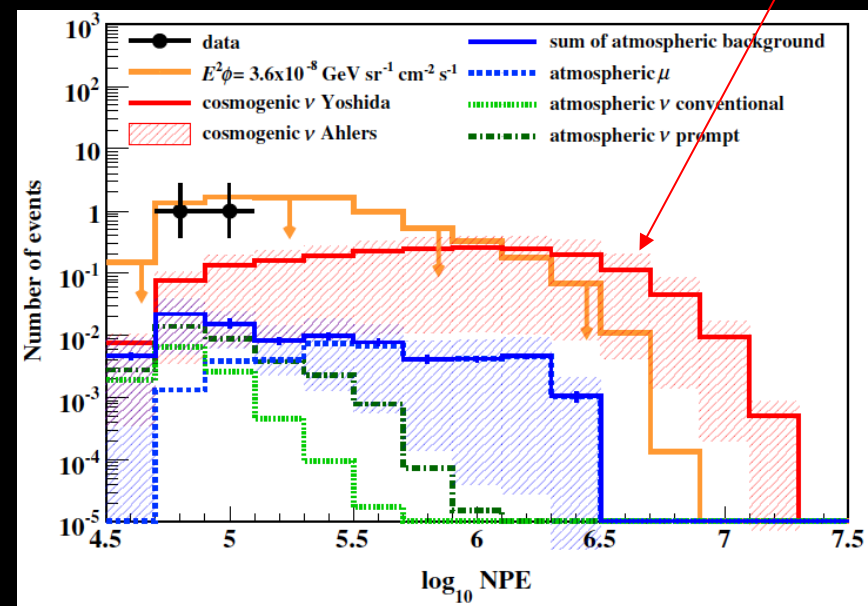


2. Astrophysical Very-High-Energy Neutrinos

First observation (2013) by IceCube Neutrino Observatory

- 60-2000 TeV neutrinos
- Too high-energy as atmospheric neutrinos
- Too low-energy as GZK neutrinos

$$p + \gamma \rightarrow \Delta \rightarrow \pi \rightarrow \nu$$



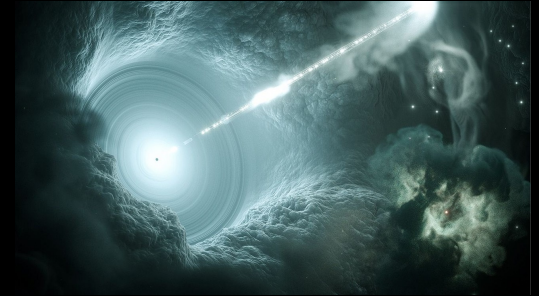
2. Astrophysical Very-High-Energy Neutrinos

First observation (2013) by IceCube Neutrino Observatory

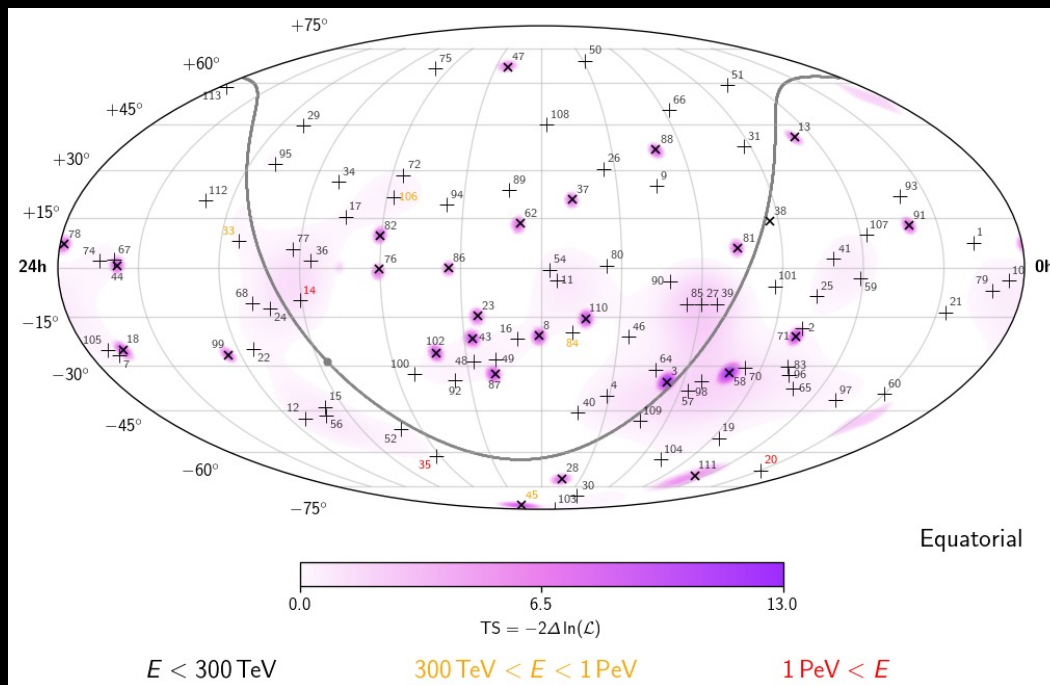
- 60-2000 TeV neutrinos
- Too high-energy as atmospheric neutrinos
- Too low-energy as GZK neutrinos
- Sources are mostly unknown (diffuse)

Evidence of Blazar Neutrino

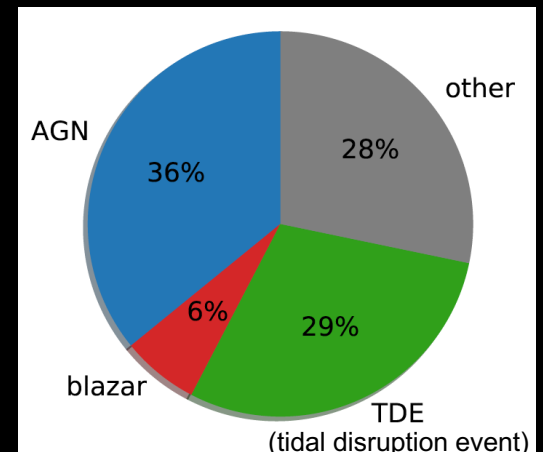
- IC170922A
- TXS 0506+056



IceCube, Science361(2018)147
IceCube et al.(2018)eaat1378



IceCube astrophysical high-energy neutrino source contribution

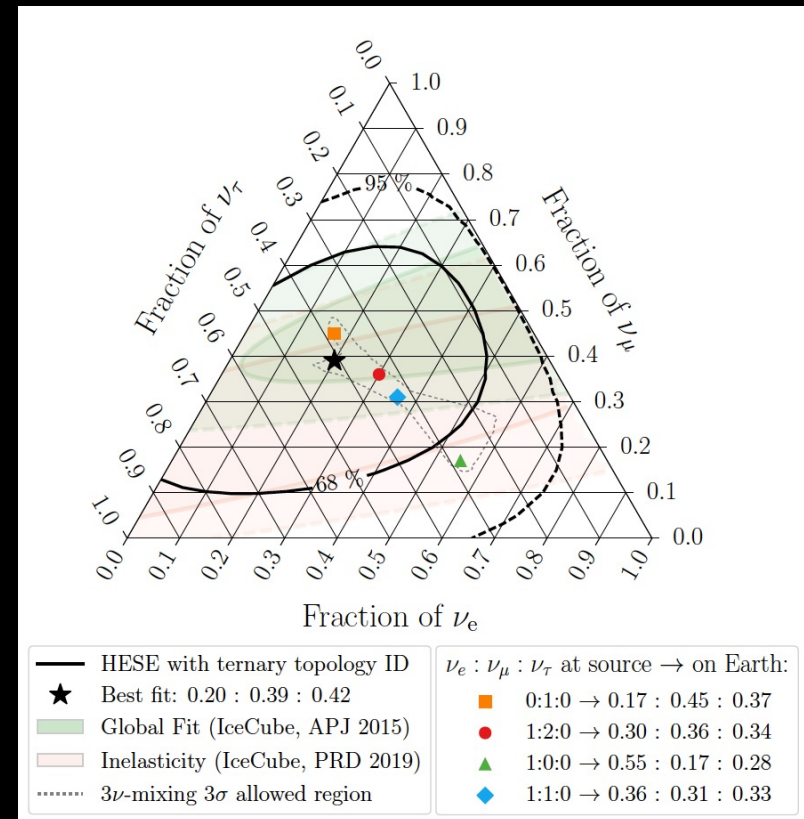
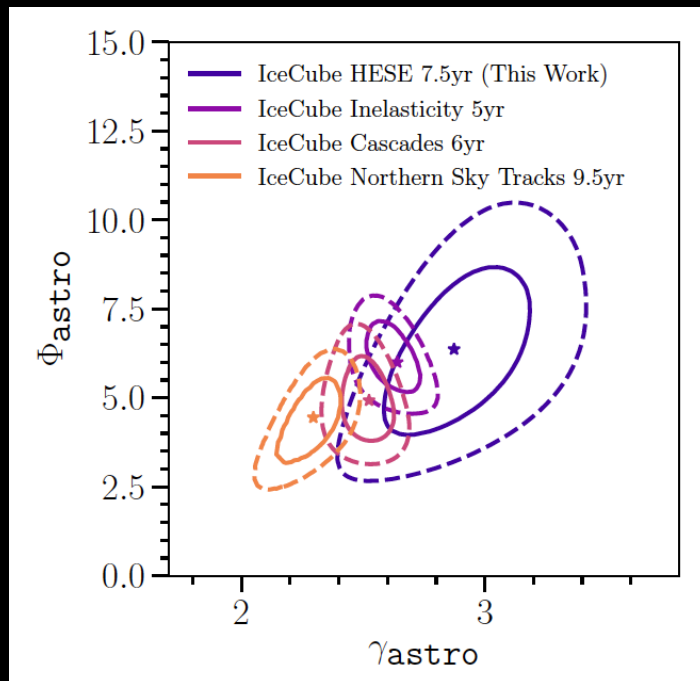


ArXiv:2105.03792

2. Astrophysical Very-High-Energy Neutrinos

First observation (2013) by IceCube Neutrino Observatory

- 60-2000 TeV neutrinos
- Too high-energy as atmospheric neutrinos
- Too low-energy as GZK neutrinos
- Sources are mostly unknown (diffuse)
- Large uncertainty on spectrum and flavor structure

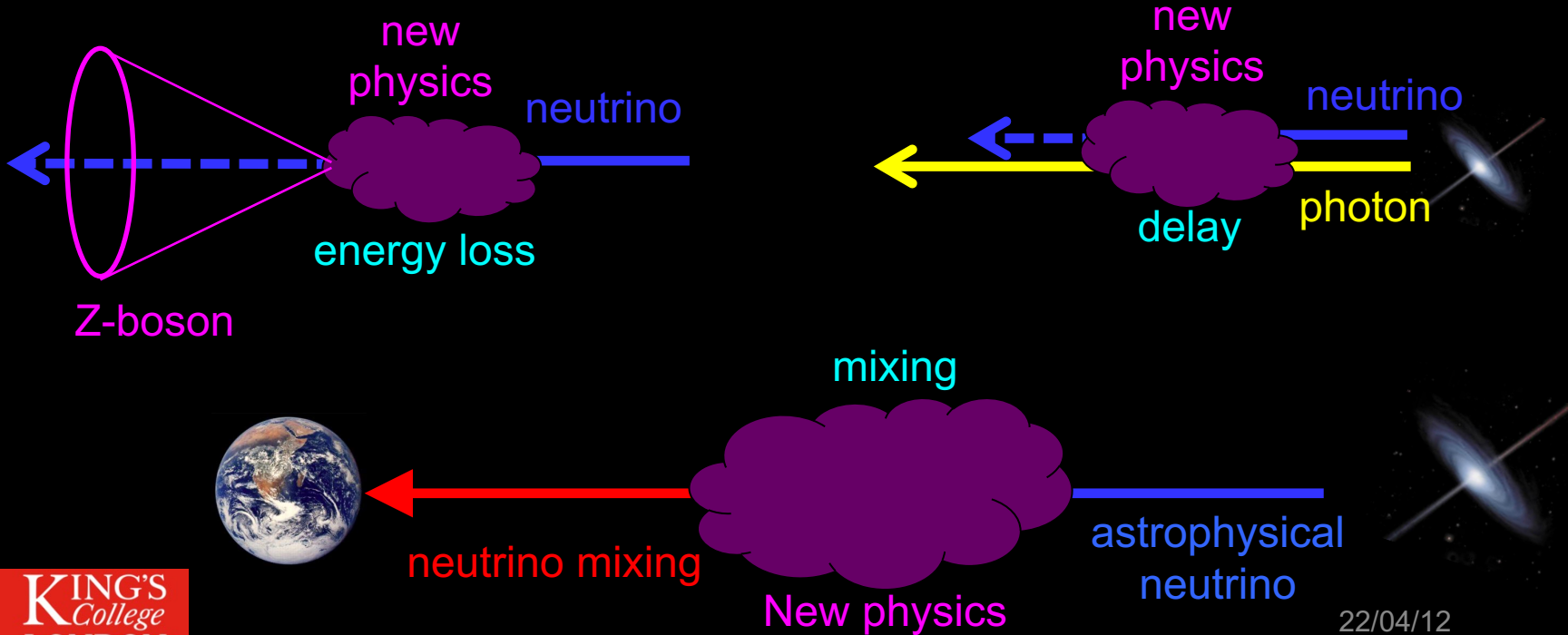


2. Search for Lorentz violation with astrophysical neutrinos

High-energy particles (>100 TeV) propagating a long distance (>100 Mpc)
- Neutrinos can probe new physics in the universe

New physics search

- Spectrum distortion (vacuum Cherenkov radiation)
- Time of Flight (modified dispersion)
- New flavour structure (new vacuum effect)



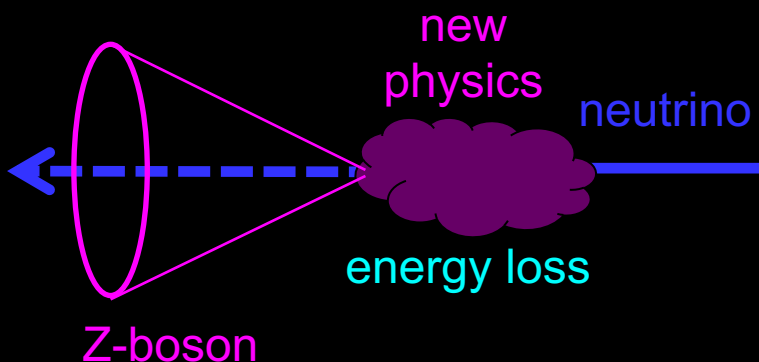
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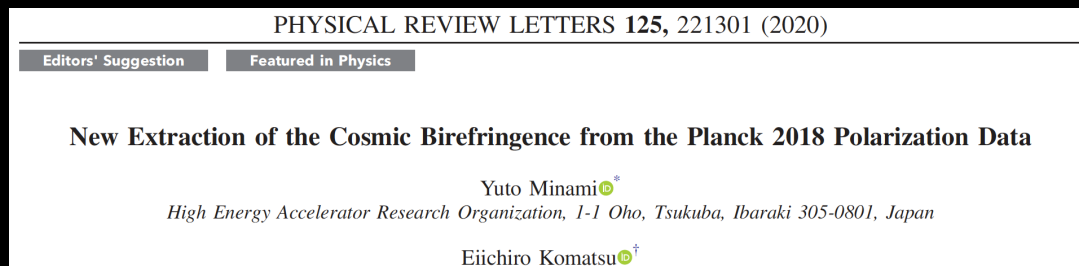
New physics search

- Spectrum distortion (vacuum Cherenkov radiation)
- Time of Flight (modified dispersion)
- New flavour structure (new vacuum effect)



Lorentz violating field cause
Cherenkov radiation in vacuum

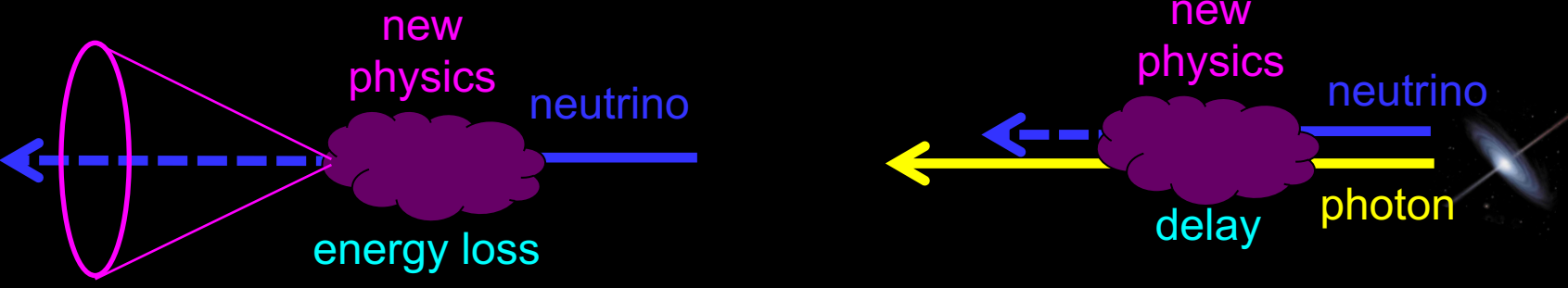
CMB polarization data
may indicate nonzero
vacuum birefringence
 $k^{(3)}_{00} \sim 10^{-43}$ GeV



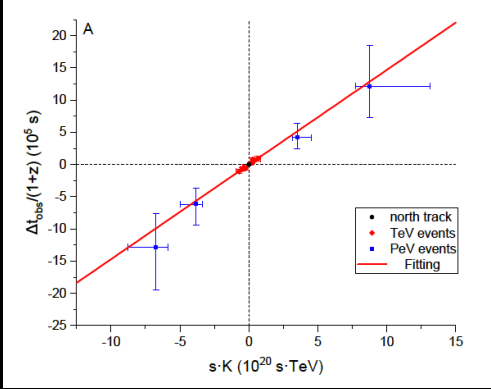
2. Search for Lorentz violation with astrophysical neutrinos

High-energy particles (>100 TeV) propagating a long distance (>100 Mpc)
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- New physics search
- Spectrum distortion (vacuum Cherenkov radiation)
 - Time of Flight (modified dispersion)
 - New flavour structure (new vacuum effect)



Z-boson
 nonzero LV
 $E_{LV} \sim 10^{17}$ GeV



Modified dispersion due to quantum foam cause unexpected delay/advance for neutrinos

$$\frac{\Delta t_{obs}}{1+z} = \Delta t_{in} + s \cdot \frac{K}{E_{LV}}$$

2. Search for Lorentz violation with astrophysical neutrinos

High-energy particles (>100 TeV) propagating a long distance (>100 Mpc)

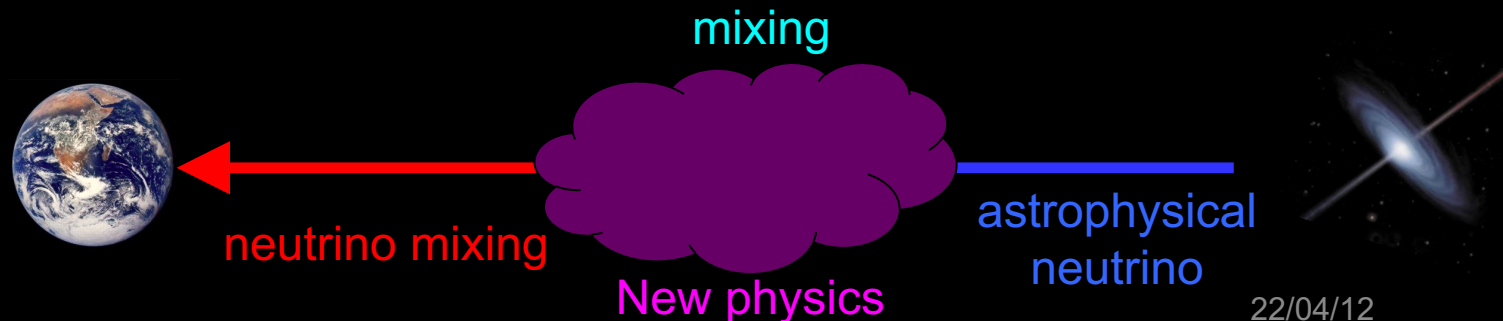
- Neutrinos can probe new physics in the universe

New physics search

- Spectrum distortion (vacuum Cherenkov radiation)
- Time of Flight (modified dispersion)
- **New flavour structure (new vacuum effect)**

Neutrino interferometry


- Macroscopic quantum effect and sensitive to small effects



Higher order operators in effective field theory (EFT)

Higher-dimension operators may be related to new physics

- Dimension-5 operator (unit: GeV^{-1}), example: Majorana mass
- Dimension-6 operator (unit: GeV^{-2}), example: Fermi constant (G_F)


nonrenormalizable


SME Lagrangian

$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu^{(3)}\psi + \bar{\psi}\gamma^\mu c_{\mu\nu}^{(4)}\partial^\nu\psi \dots$$

SME motivated effective Hamiltonian for neutrinos

$$h_{eff} \sim \frac{1}{2E} M^2 + V_{CC} + a^{(3)} + E c^{(4)} + E^2 a^{(5)} + E^3 c^{(6)} \dots$$

 nonrenormalizable

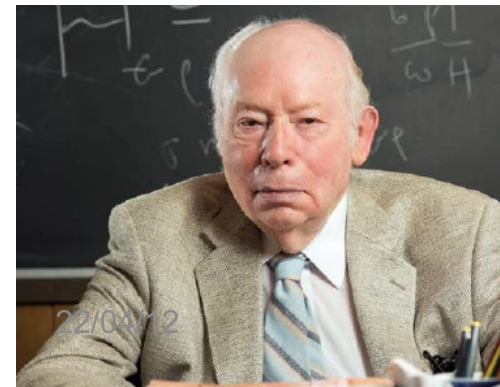
We focus on higher-dimension Lorentz violating operator search

If, Lorentz violation is related to Planck scale physics, it is suppressed inverse of Planck energy, $1/E_{\text{Planck}}^2 \sim 10^{-38} \text{ GeV}^{-2}$
 \rightarrow natural scale of dimension-6 Lorentz violating operator

Limits from this operator by atmospheric neutrino is $\sim 10^{-36} \text{ GeV}^{-1}$

“In a sense it is beyond the SM, but I would rather say it is beyond the leading terms – the renormalizable, unsuppressed part of the SM,” says Weinberg. “But hell – so is gravity! The symmetries of general relativity don’t allow any renormalizable interactions of massless spin-2 particles called gravitons.”

Steve Weinberg
 (CERN Courier, Nov 2017)



Astrophysical neutrino flavor with Lorentz violation

We start from isotropic model of nonminimal SME

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} + E^4 a_{\alpha\beta}^{(7)} - E^5 c_{\alpha\beta}^{(8)} \dots$$

dim-6 isotropic SME (d=6)

$$E^3 c_{\alpha\beta}^{(6)} = E^3 \frac{1}{\sqrt{4\pi}} \left(c_{\alpha\beta}^{(6)} \right)_{00} = E^3 \begin{pmatrix} c_{ee}^{(6)} & c_{e\mu}^{(6)} & c_{\tau e}^{(6)} \\ c_{e\mu}^{(6)*} & c_{\mu\mu}^{(6)} & c_{\mu\tau}^{(6)} \\ c_{\tau e}^{(6)*} & c_{\mu\tau}^{(6)*} & c_{\tau\tau}^{(6)} \end{pmatrix}$$

and so on...

We test dim-3 to dim-8 operators one by one to find nonzero scale (or set limit on scale)

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U - E^3 c_{\alpha\beta}^{(6)} = V^\dagger(E) \Delta V(E)$$

$$V(E) = \begin{pmatrix} V_{e1}(E) & V_{e2}(E) & V_{e3}(E) \\ V_{\mu1}(E) & V_{\mu2}(E) & V_{\mu3}(E) \\ V_{\tau1}(E) & V_{\tau2}(E) & V_{\tau3}(E) \end{pmatrix}, \quad \Delta = \begin{pmatrix} \lambda_1(E) & 0 & 0 \\ 0 & \lambda_2(E) & 0 \\ 0 & 0 & \lambda_3(E) \end{pmatrix}$$

Astrophysical neutrino flavor with Lorentz violation

Neutrino oscillation formula is written with mixing matrix elements and eigenvalues

$$P_{\alpha \rightarrow \beta}(E, L) = 1 - 4 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin^2 \left(\frac{\lambda_i - \lambda_j}{2} L \right) + 2 \sum_{i>j} \text{Im}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin \left((\lambda_i - \lambda_j) L \right)$$

However, astrophysical neutrinos propagate $O(100\text{Mpc}) \rightarrow$ lost coherence

$$P_{\alpha \rightarrow \beta}(E, \infty) \sim 1 - 2 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) = \sum_i |V_{\alpha i}|^2 |V_{\beta i}|^2$$

Astrophysical neutrino flux of flavor α at production is $\phi_\alpha^p(E) \sim \phi_\alpha^p \cdot E^{-\gamma}$. Since it's low statistics, we consider energy-averaged flavor composition β on Earth

$$\bar{\phi}_\beta^\oplus = \frac{1}{\Delta E} \int_{\Delta E} \sum_\alpha P_{\alpha \rightarrow \beta}(E, \infty) \phi_\alpha^p(E) dE$$

We take the fraction of this for each flavor.

$$f_\beta^\oplus = \frac{\bar{\phi}_\beta^\oplus}{\sum_{e,\mu,\tau} \bar{\phi}_\gamma^\oplus}$$

HESE 7.5-yr Flavor new physics search

Data, 2635 days HESE sample [IceCube, ArXiv: 2011.03545](#)

- 17 track events, 20 $\log(E)$ bins [60 TeV, 10 PeV], 10 $\cos\theta$ bins [-1.0, +1.0]
- 41 cascade events, 20 $\log(E)$ bins [60 TeV, 10 PeV], 10 $\cos\theta$ bins [-1.0, +1.0]
- 2 double cascades, 20 $\log(E)$ bins [60 TeV, 10 PeV], 10 $\log(L)$ bins [10m, 100m]

Simulation

[Bhattacharya et al., JHEP06\(2015\)110](#)

- Foregrounds, conventional (Honda flux), prompt (BERSS model), muon (CORSIKA)
- Astrophysical neutrinos, simple power law
- Interaction, NLO PDF DIS (CSMS model) [Cooper-Sarkar et al., JHEP08\(2011\)042](#)

Systematics (15 nuisance parameters)

- oscillation parameters (6)
- normalization of flux : conventional (40%), prompt (free), muon (50%), astrophysical (free)
- spectrum index : primary cosmic ray (5%) astrophysical neutrinos (free)
- Ice model : (20%)
- DOM efficiency : overall (10%), angular dependence (50%)

Limits

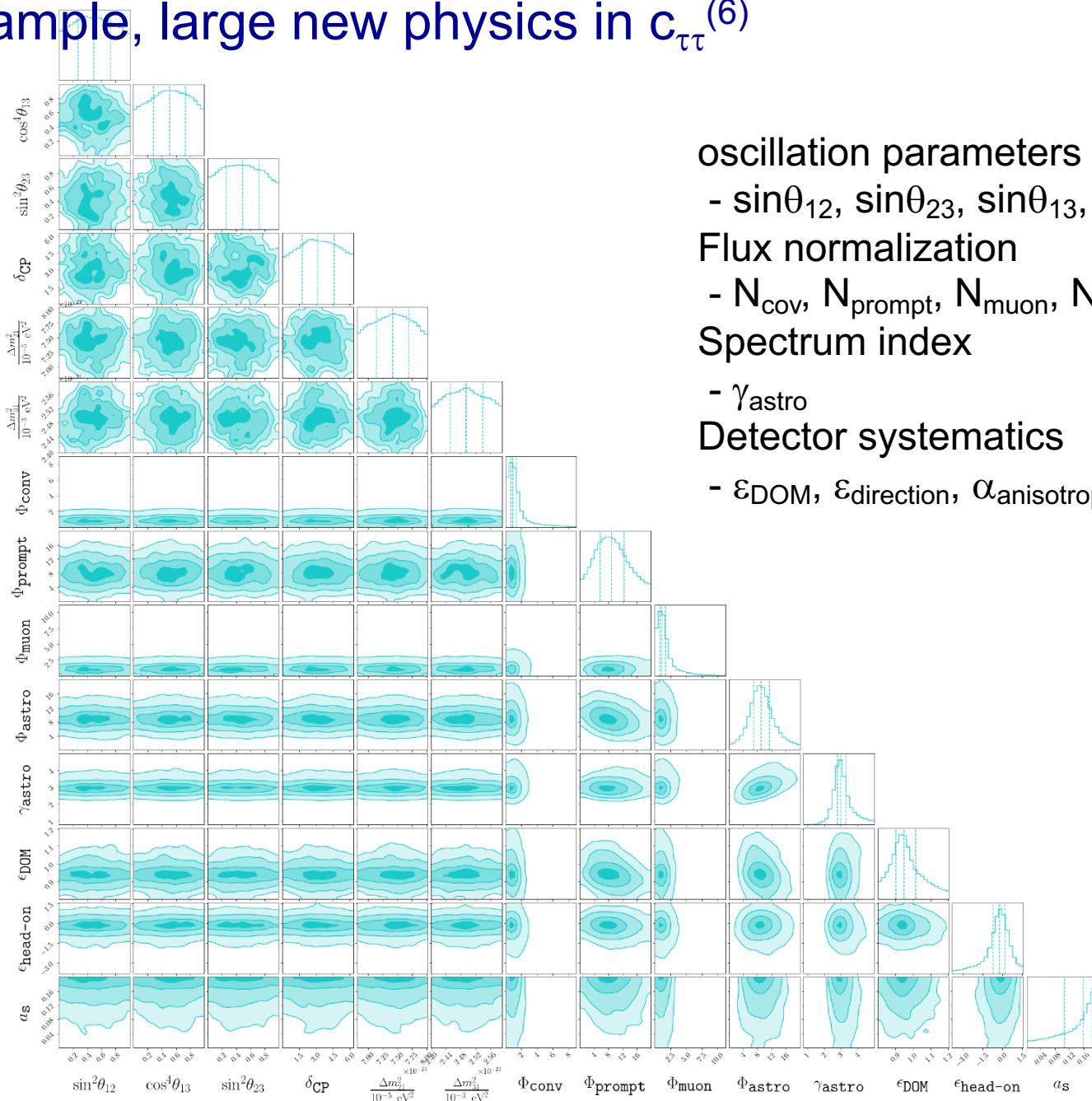
[Feroz et al., Mon. Not. Roy. Astron. Soc. 398,1601\(2009\)1601](#)

- Bayesian: MCMC with Multinest, Bayes factor with Jefferey' scale “strong” limit
- Frequentist: Wilks' theorem

Systematic errors

Parameter	Prior (constraint)	Range	Description
Astrophysical neutrino flux:			
Φ_{astro}	-	$[0, \infty)$	Normalization scale
γ_{astro}	-	$(-\infty, \infty)$	Spectral index
Atmospheric neutrino flux:			
Φ_{conv}	1.0 ± 0.4	$[0, \infty)$	Conventional normalization scale
Φ_{prompt}	-	$[0, \infty)$	Prompt normalization scale
$R_{K/\pi}$	1.0 ± 0.1	$[0, \infty)$	Kaon-Pion ratio correction
$2\nu / (\nu + \bar{\nu})_{\text{atmo}}$	1.0 ± 0.1	$[0, 2]$	Neutrino-anti-neutrino ratio correction
Cosmic-ray flux:			
$\Delta\gamma_{\text{CR}}$	0.0 ± 0.05	$(-\infty, \infty)$	Cosmic-ray spectral index modification
Φ_{μ}	1.0 ± 0.5	$[0, \infty)$	Muon normalization scale
Detector:			
ϵ_{DOM}	0.99 ± 0.1	$[0.80, 1.25]$	Absolute energy scale
$\epsilon_{\text{head-on}}$	0.0 ± 0.5	$[-3.82, 2.18]$	DOM angular response
a_{s}	1.0 ± 0.2	$[0.0, 2.0]$	Ice anisotropy scale

Fit example, large new physics in $c_{\tau\tau}$ ⁽⁶⁾



oscillation parameters

- $\sin\theta_{12}$, $\sin\theta_{23}$, $\sin\theta_{13}$, Δm_{12} , Δm_{23} , δ

Flux normalization

- N_{cov} , N_{prompt} , N_{muon} , N_{astro}

Spectrum index

- γ_{astro}

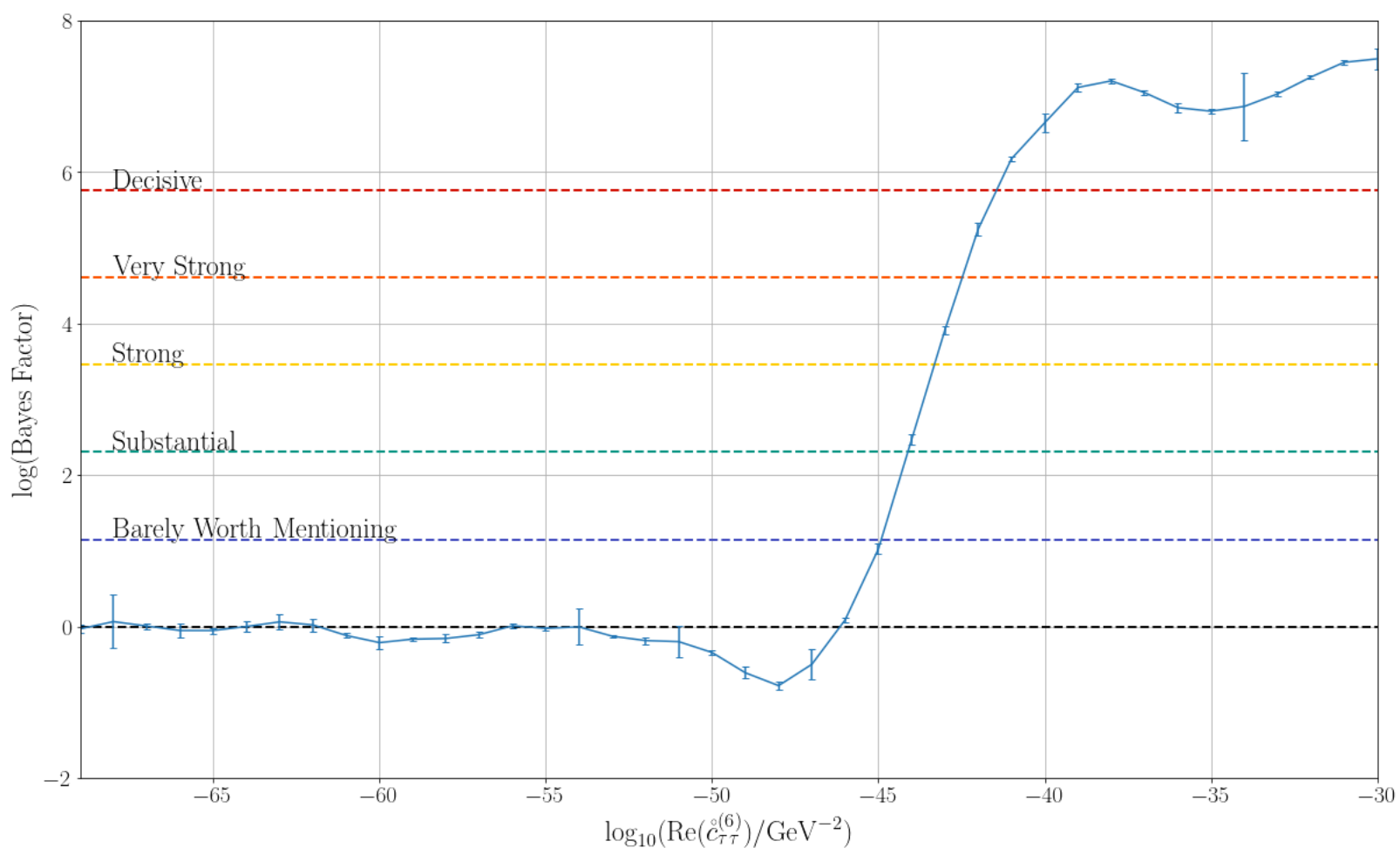
Detector systematics

- ϵ_{DOM} , $\epsilon_{\text{direction}}$, $\alpha_{\text{anisotropy}}$

Fit example, large new physics in $c_{\tau\tau}^{(6)}$

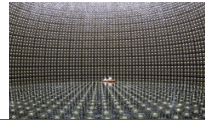
Bayesian analysis

- Bayes factor is computed with new physics parameter
- Repeat this to find the threshold to set the limit



Test of Lorentz violation with neutrinos

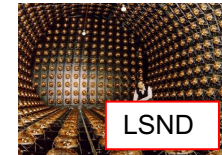
Spectral distortion



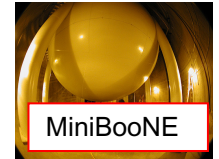
Super-Kamiokande
PRD91(2015)052003



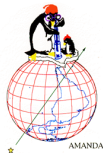
Daya Bay
PRD98(2018)092013



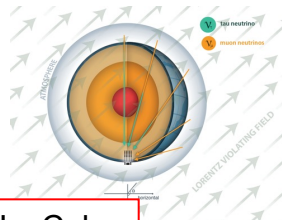
LSND
PRD72(2005)076004



MiniBooNE
PLB718(2013)1303



AMANDA
PRD79(2009)102005



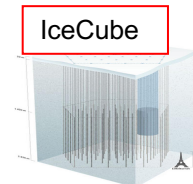
IceCube
Nature Physics
14(2018)961



MINOS ND
PRL101(2008)151601



MINOS FD
PRL105(2010)151601



IceCube
PRD82(2010)112003

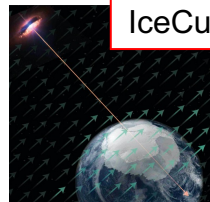


Double Chooz
PRD86(2013)112009



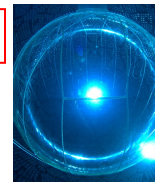
T2K ND
PRD95(2017)111101

Flavor ratio



IceCube
ArXiv: 2111.04654

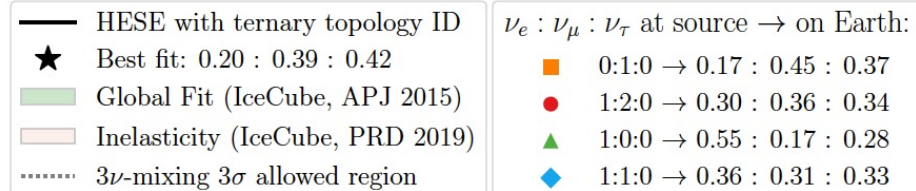
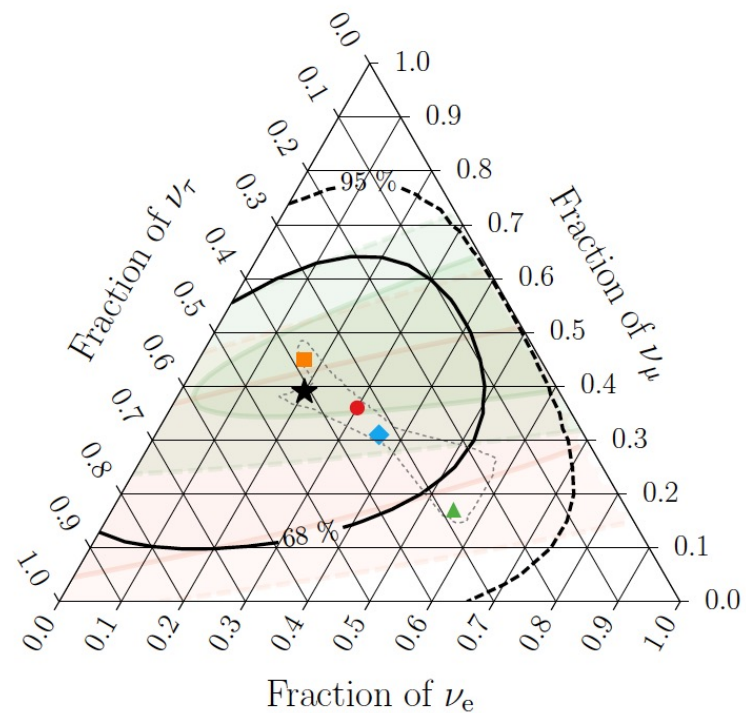
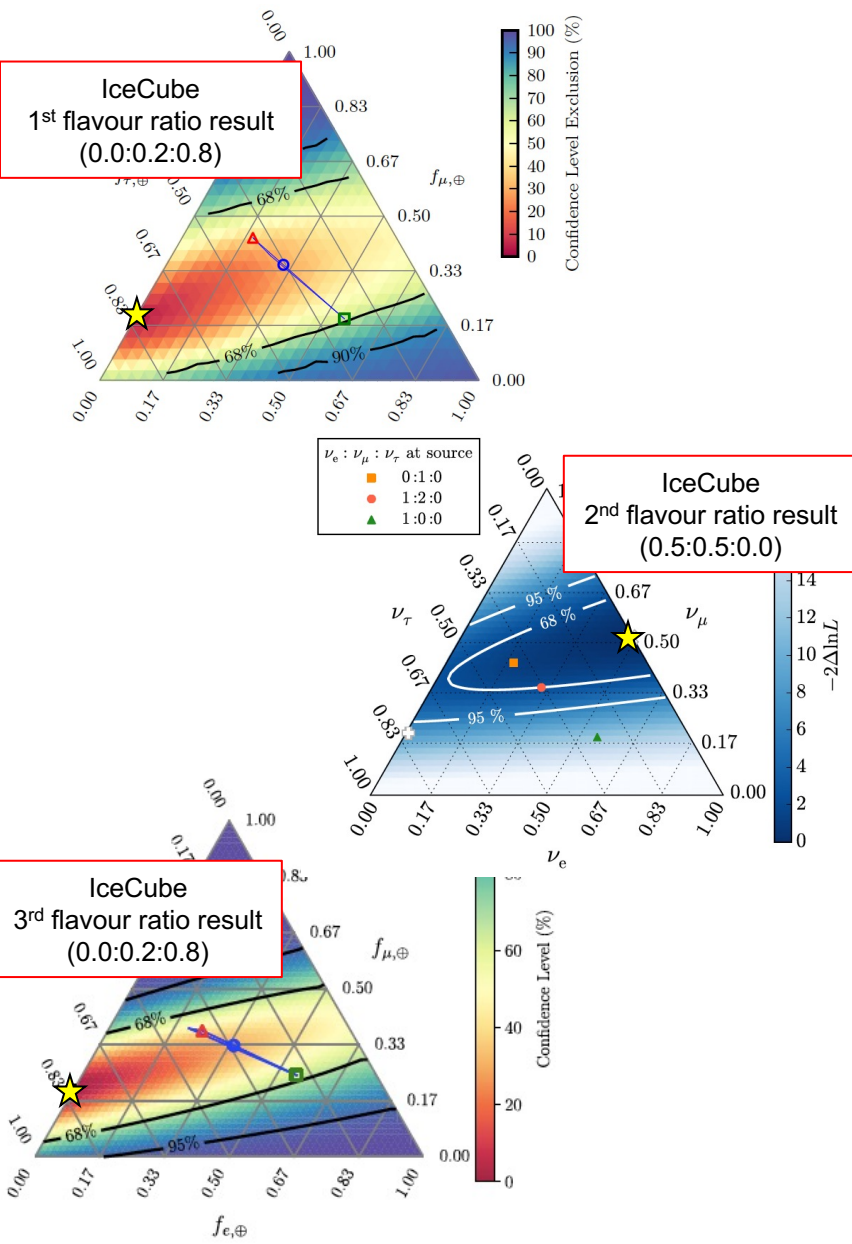
SNO



PRD98(2018)112013

Seasonal variation

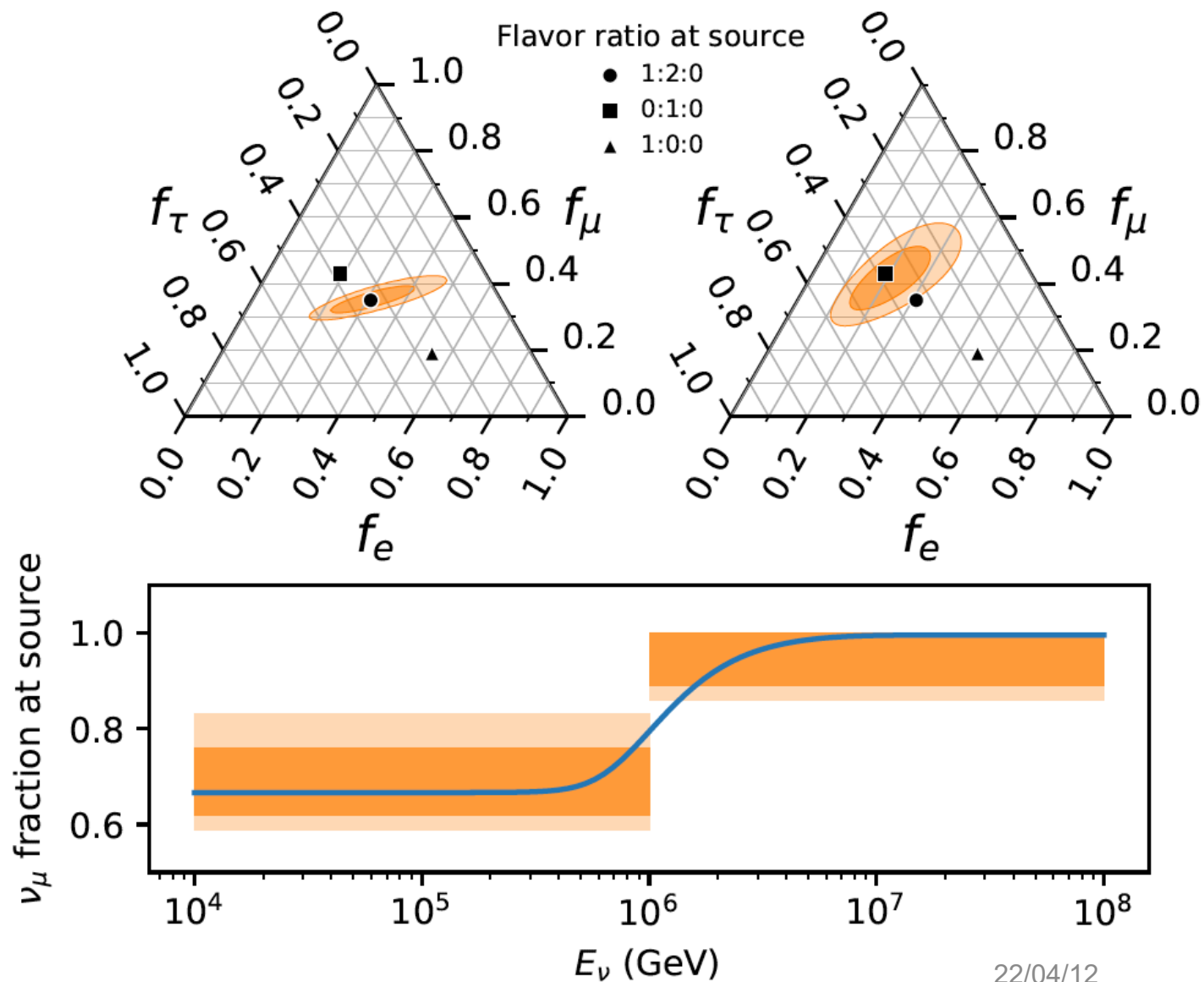
HESE 7.5-yr data (2018)



New flavour ratio measurement

- Likelihood is very shallow and fit often confuses between ν_e and ν_τ
- New flavour ratio result has some power to distinguish ν_e and ν_τ

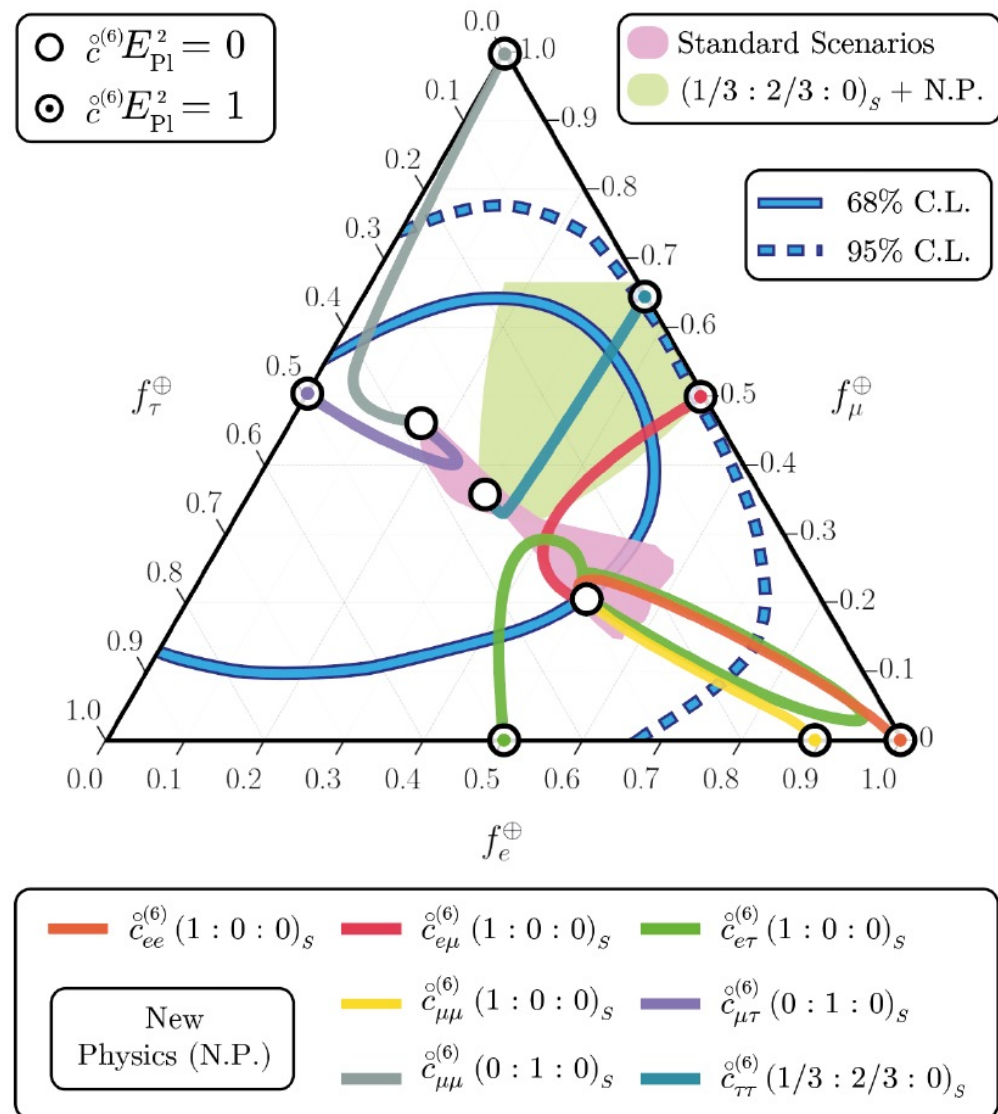
Energy dependence of flavor ratio



HESE 7.5-yr flavor new physics search

Various standard astrophysical neutrino production models predict different neutrino flavour ratios, however, they all end up in the pink region. \circ indicated characteristic model predictions. Nonzero new physics moves standard predictions \circ to different locations \odot depending on the types of new physics operators.

If the new physics models bring the standard predictions outside of the data contour, such model can be rejected by current data



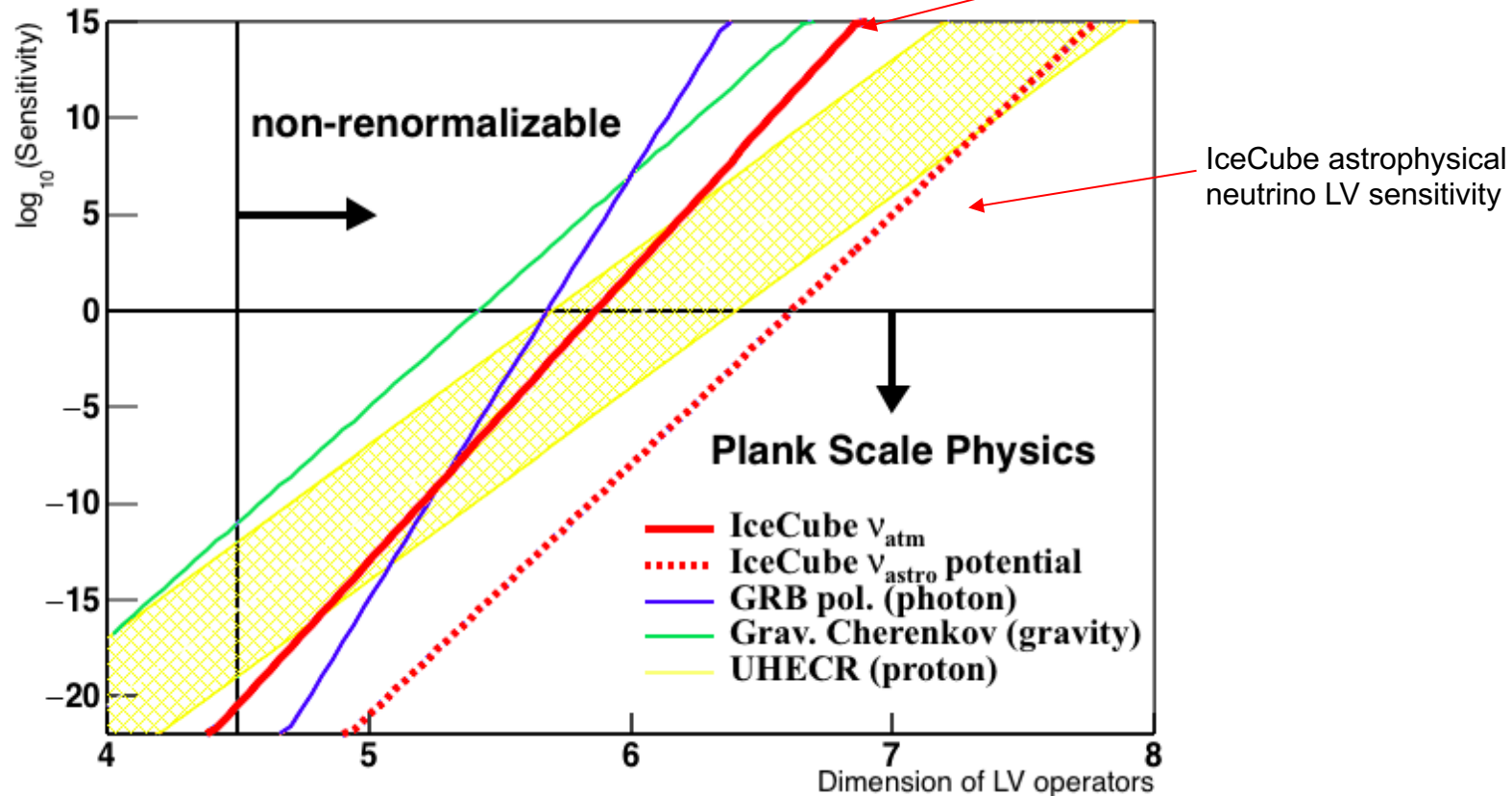
Neutrino interferometry – Astrophysical neutrinos

Higher-dimension operators may be related to new physics

- Dimension-5 operator (unit: GeV^{-1}), example: Majorana mass
- Dimension-6 operator (unit: GeV^{-2}), example: Fermi constant (G_F)

IceCube atmospheric
neutrino LV sensitivity
[Nature Physics 14\(2018\)961](#)

New physics limits and projected sensitivity



Astrophysical neutrino dim-6 LV operator search can reach quantum gravity motivated region ($\sim 1/M_{\text{Planck}}^2 \sim 10^{-38} \text{ GeV}^{-2}$)