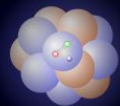


Neutrino Interactions with Nucleons and Nuclei

Ulrich Mosel

Based on work with
T. Leitner, O. Lalakulich and K. Gallmeister



**Institut für
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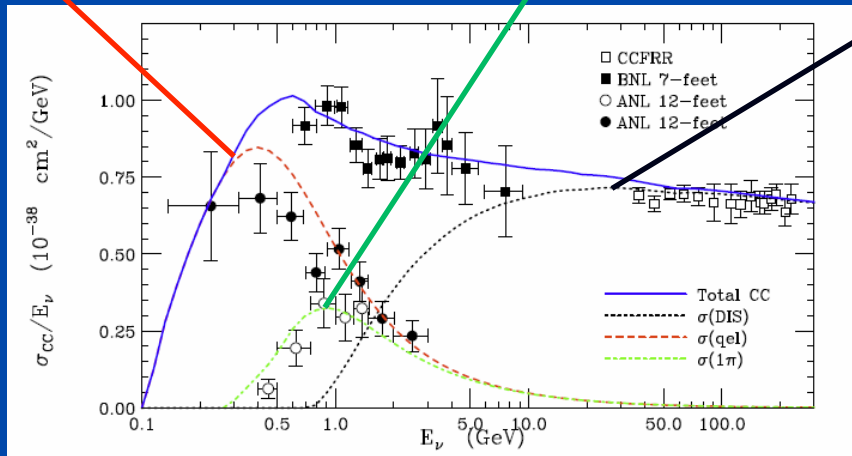
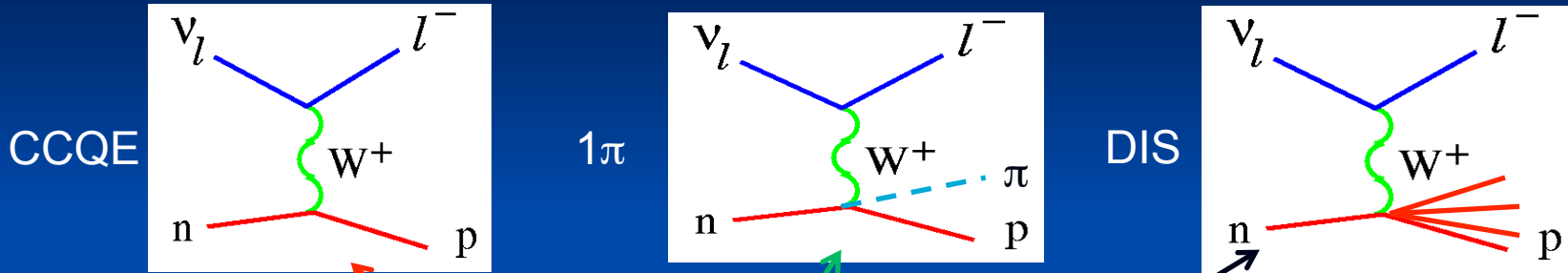


Motivation

- Neutrino properties can be extracted from Long Baseline Experiments only if energy is known
- Both calorimetry and QE-based energy reconstruction methods require understanding of the full event
- Theory has to be able to describe the full final states of all particles, inclusive X-sections are not sufficient

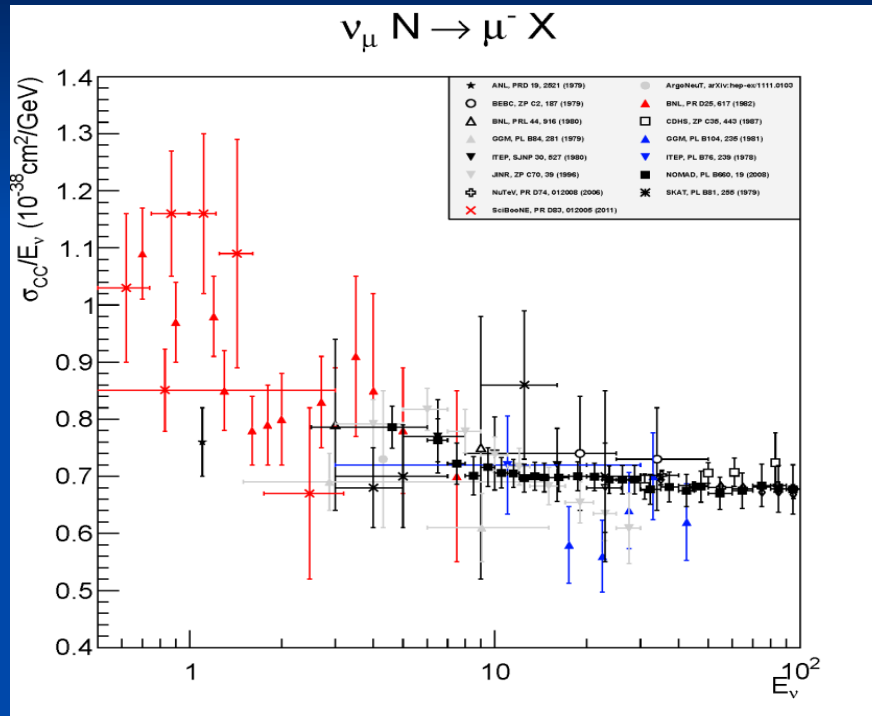


Neutrino-nucleon cross section



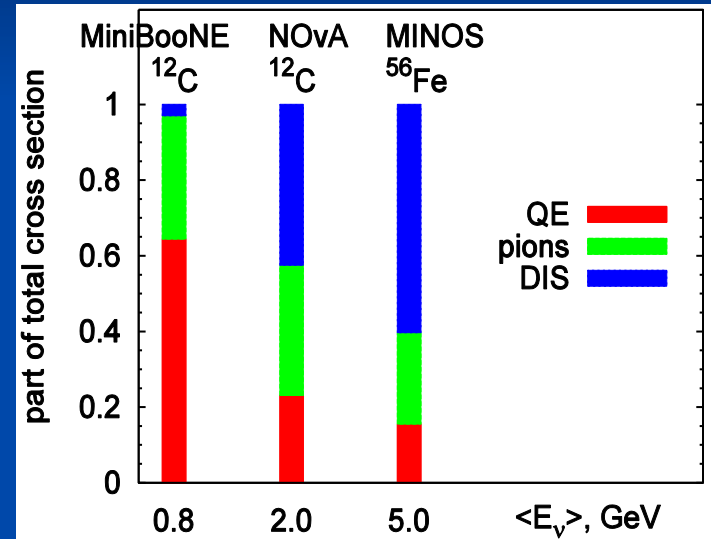
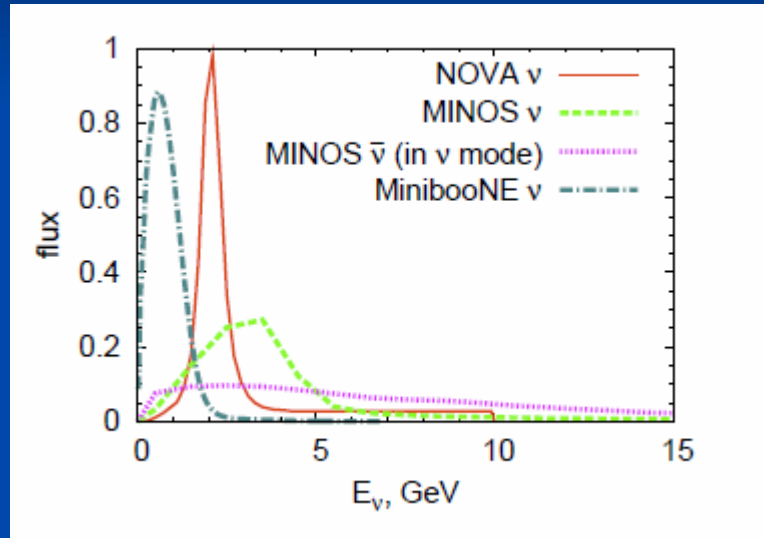
note:
 $10^{-38} \text{ cm}^2 = 10^{-11} \text{ mb}$

Neutrino-Nucleon Cross Sections



Neutrino Beams

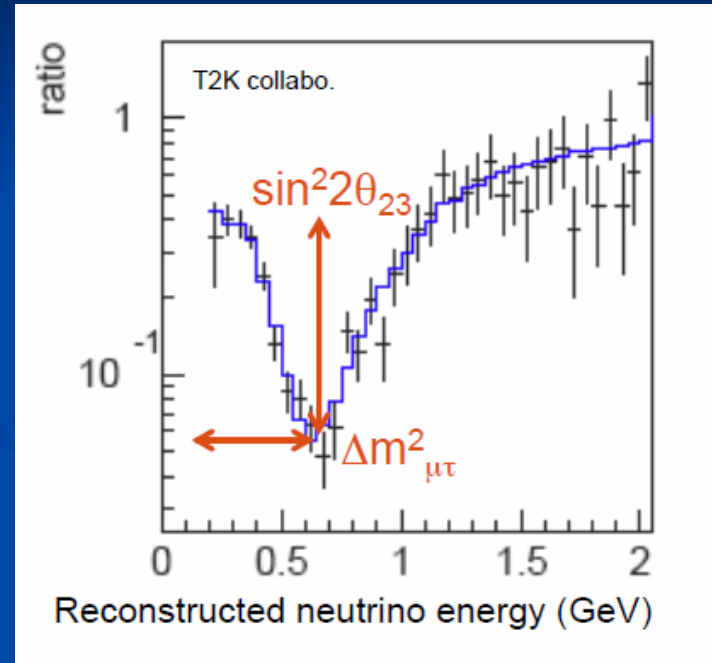
- Neutrinos do not have fixed energy:



Have to reconstruct energy from final state of reaction

Observable Oscillation Parameters

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E_\nu} \right)$$



Neutrino Oscillations

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} \\
 &- \alpha \sin 2\theta_{13} \xi \sin \delta \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha \sin 2\theta_{13} \xi \cos \delta \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2} \\
 &\equiv O_1 + O_2(\delta) + O_3(\delta) + O_4 .
 \end{aligned}$$

appearance probability

$$\Delta = \frac{\Delta m_{21}^2 L}{4E} \quad \alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \quad \xi = \cos \theta_{13} \sin(2\theta_{12}) \sin(2\theta_{23})$$

$$\hat{A} = \frac{2\sqrt{2}G_F n_e E}{\Delta m_{31}^2} \quad \delta = \text{CP violating phase}$$

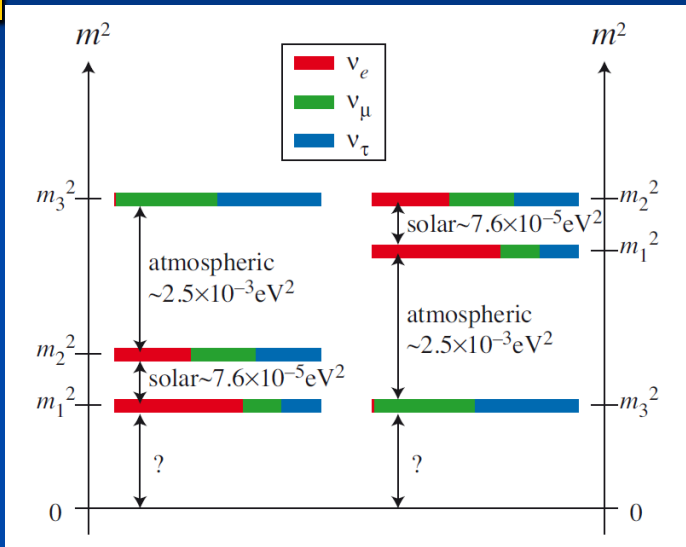
Vacuum
oscillation

Matter effects,
 n_e = electron density
Depends on sign of Δ_{31}

Oscillation depends on difference of (squared) masses only

Oscillation Signal

Dependence on Hierarchy and Mixing Angle



Energy has to be known better than 50 MeV
 Shape sensitive to hierarchy and sign of
 mixing angle

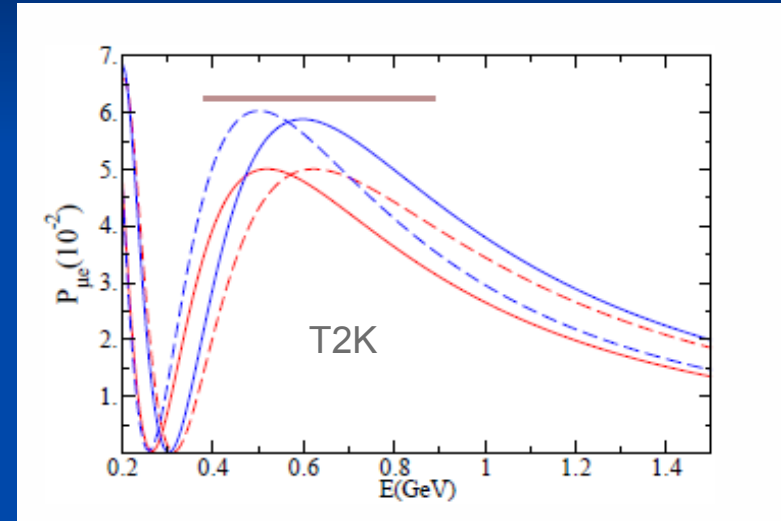
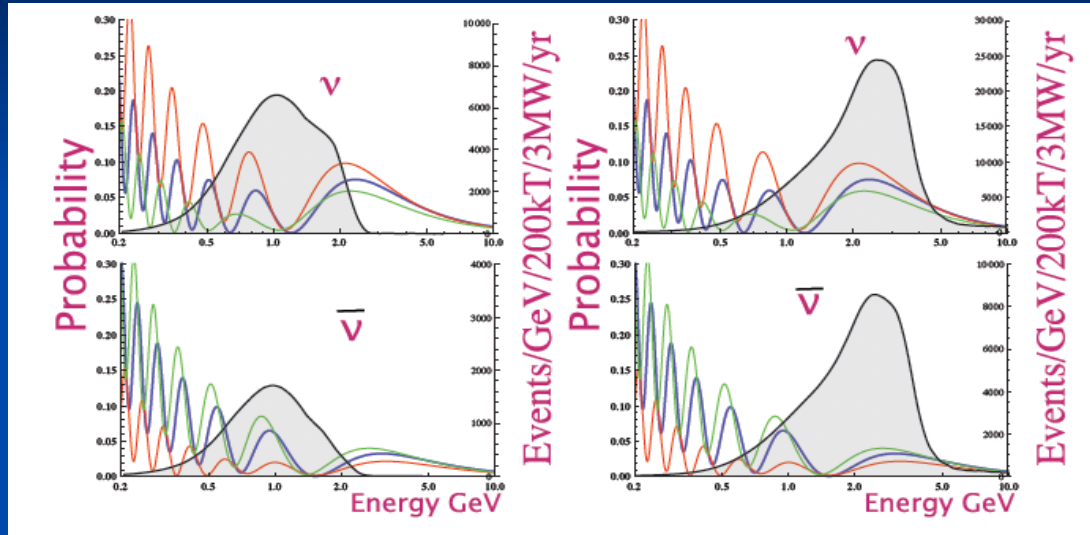


Fig. 2. $P_{\mu e}$ in matter versus neutrino energy for the T2K experiment. The blue curves depict the normal hierarchy, red the inverse hierarchy. Solid curves depict positive θ_{13} , dashed curves negative θ_{13}

D.J. Ernst et al., arXiv:1303.4790 [nucl-th]

LBNE, δ_{CP} sensitivity

From: Bishai et al., hep-ex 12034090



8 GeV

60 GeV

proton energy

From:
Bishai et al
arXiv:1203.409

$$\delta_{CP} = 0$$

$$\delta_{CP} = \pi/2$$

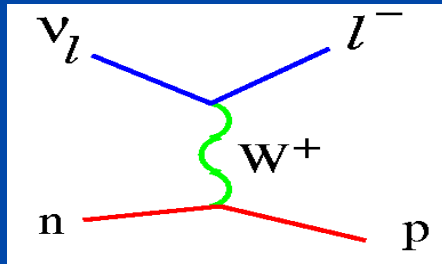
$$\delta_{CP} = -\pi/2$$

Need energy within 100 MeV to distinguish between different δ_{CP}



Energy Reconstruction by QE

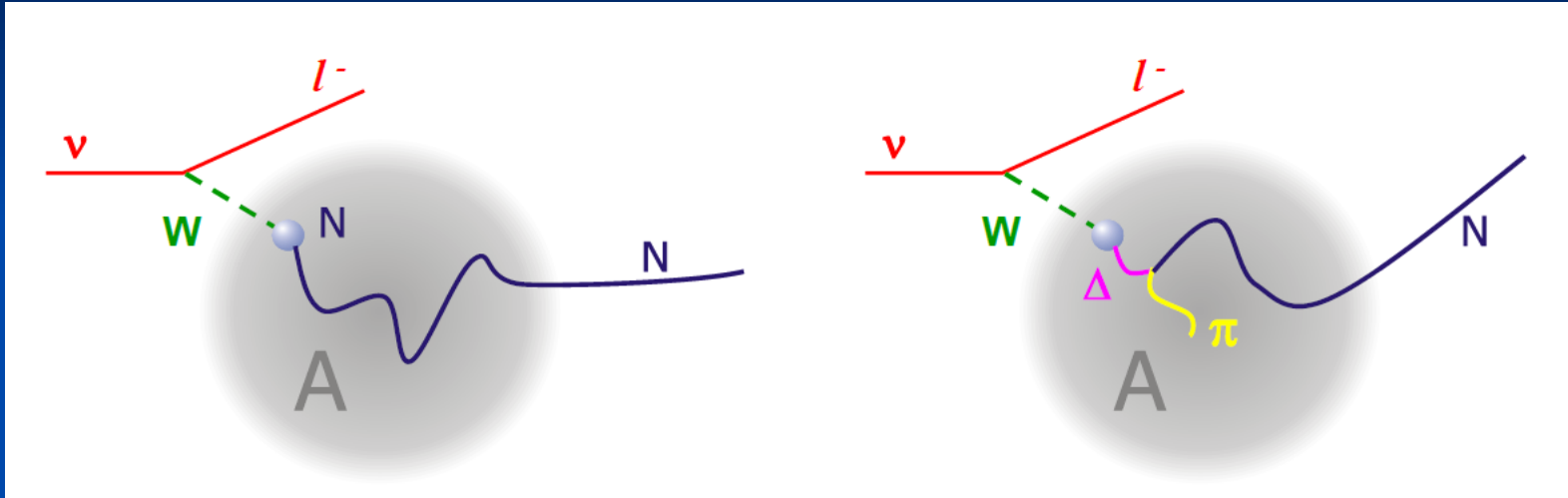
- In QE scattering on nucleon at rest, only $l + p$, 0π , is outgoing. lepton determines neutrino energy:



$$E_\nu = \frac{2M_N E_\mu - m_\mu^2}{2(M_N - E_\mu + p_\mu \cos \theta_\mu)}$$

- **Trouble:** all presently running exps use nuclear targets
 1. Nucleons are Fermi-moving
 2. Final state interactions may hinder correct event identification

FSI in Nuclear Targets



Complication to identify QE, entangled with π production

Both must be treated at the same time

Nuclear Targets (K2K, MiniBooNE, T2K, MINOS, Minerva, LBNE)

- **GiBUU : Theory and Event Simulator**
based on a BM solution of Kadanoff-Baym equations
- Physics content and details of implementation in:
Buss et al, Phys. Rept. 512 (2012) 1- 124
Code available from gibuu.hepforge.org

Mine of information on theoretical treatment of potentials, collision terms, spectral functions and cross sections, useful for any generator

Transport Equation

- Kadanoff-Baym equation for space-time development of one particle spectral phase space density F (*Wigner Function*) after gradient expansion

$$\mathcal{D}F(x, p) + \text{tr} \left\{ \text{Re} \tilde{S}^{\text{ret}}(x, p), -i \tilde{\Sigma}^<(x, p) \right\}_{\text{pb}} = C(x, p).$$

F = spectral phase-space density:

$$F(x, p) = -2f(x, p) \text{tr}[\text{Im}(\tilde{S}^{\text{ret}}(x, p))\gamma^0],$$

$$\mathcal{D}F = \{p_0 - H, F\}_{\text{pb}} \quad \text{with } H = E^*(x, p) - \text{Re} \tilde{\Sigma}_V^0(x, p).$$

Transport Equation

Collision term

$$\mathcal{D}F(x, p) + \text{tr} \left\{ \text{Re} \tilde{S}^{\text{ret}}(x, p), -i \tilde{\Sigma}^<(x, p) \right\}_{\text{pb}} = C(x, p).$$

Drift term

$$\left[\left(1 - \frac{\partial H}{\partial p_0} \right) \frac{\partial}{\partial t} + \frac{\partial H}{\partial \mathbf{p}} \frac{\partial}{\partial \mathbf{x}} - \frac{\partial H}{\partial \mathbf{x}} \frac{\partial}{\partial \mathbf{p}} + \frac{\partial H}{\partial t} \frac{\partial}{\partial p^0} + \text{KB term} \right] F(x, p) = - \text{loss term} + \text{gain term}$$

Kadanoff-Baym equation

- LHS: drift term + backflow (KB) terms
- RHS: collision term = - loss + gain terms



Collision term

$$\begin{aligned} C^{(2)}(x, p_1) &= C_{\text{gain}}^{(2)}(x, p_1) - C_{\text{loss}}^{(2)}(x, p_1) = \frac{\mathcal{S}_{1'2'}}{2p_1^0 g_{1'} g_{2'}} \int \frac{d^4 p_2}{(2\pi)^4 2p_2^0} \int \frac{d^4 p_{1'}}{(2\pi)^4 2p_{1'}^0} \int \frac{d^4 p_{2'}}{(2\pi)^4 2p_{2'}^0} \\ &\times (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_{1'} - p_{2'}) \overline{|\mathcal{M}_{12 \rightarrow 1'2'}|^2} [F_{1'}(x, p_{1'}) F_{2'}(x, p_{2'}) \bar{F}_1(x, p_1) \\ &\times \bar{F}_2(x, p_2) - F_1(x, p_1) F_2(x, p_2) \bar{F}_{1'}(x, p_{1'}) \bar{F}_{2'}(x, p_{2'})] \end{aligned}$$

with

$$\begin{aligned} F(x, p) &= 2\pi g A(x, p) f(x, p) \\ \bar{F}(x, p) &= 2\pi g A(x, p) [1 - f(x, p)] \end{aligned}$$

More complicated expressions for 3-body interactions (e.g. pion absorption)

BM Simplification

Problem: ‚backflow‘ term does not directly depend on F

Botermans-Malfliet simplification for equilibrium, correction terms are of higher order in gradients

$$\tilde{\Sigma}_{\text{eq}}^<(x, p) = i\Gamma_{\text{eq}}(x, p)f_{\text{eq}}(x, p),$$

$$\tilde{\Sigma}_{\text{eq}}^>(x, p) = -i\Gamma_{\text{eq}}(x, p)[1 - f_{\text{eq}}(x, p)]$$

$$\Gamma(x, p) = -2\text{Im}\tilde{\Sigma}^{\text{ret}}(x, p)$$

$$\mathcal{D}F(x, p) - \text{tr} \left\{ \Gamma f, \text{Re} \tilde{S}^{\text{ret}}(x, p) \right\}_{\text{pb}} = C(x, p).$$

BM term now $\sim \Gamma$, controls off-shell transport

Spectral Function

$$F(x, p) = -2f(x, p)\text{tr}[\text{Im}(\tilde{S}^{\text{ret}}(x, p))\gamma^0],$$

$$A(x, p) := \frac{1}{g}\text{tr}[\hat{A}(x, p)\gamma^0] = -\frac{1}{g\pi}\text{tr}[\text{Im}(\tilde{S}^{\text{ret}}(x, p))\gamma^0],$$

$$F(x, p) = 2\pi g f(x, p) A(x, p).$$

„Spectral Phase Space Density“
= Product of phase-space density f and spectral function A

GiBUU and MC Event Generators

- Phase-space distribution f is solved by a testparticle method, well known in numerical fluid dynamics
- Care is taken to respect relativity and detailed balance
- GiBUU reduces to MC event generators if
 - All particles on shell
 - No potentials present
 - No in-medium effects



Theoretical Basis of GiBUU

Simplicity

- Kadanoff-Baym equation (1960s)
 - full equation can not be solved yet
 - not (yet) feasible for real world problems
- Boltzmann-Uehling-Uhlenbeck (BUU) models
 - Boltzmann equation as gradient expansion of Kadanoff-Baym equations, in Botermans-Malfliet representation (1990s): **GiBUU**
- Cascade models (typical event generators, NUANCE, GENIE, NEUT,..)
 - no mean-fields, primary interactions and FSI not consistent



Practical Basis: GiBUU

- one transport equation for each particle species (61 baryons, 21 mesons)
- coupled through the potential in H and the collision integral C
- $W < 2.5$ GeV: Cross sections from resonance model (PDG and MAID couplings), consistent with electronuclear physics
- $W > 2.5$ GeV: particle production through string fragmentation (PYTHIA), with smoothed transition
- **GiBUU: Only 'Neutrino Event Generator' that has widely been tested with various hadronic and em reactions, NO TUNING to nuclear data (except 2p2h)**



GiBUU Ingredients: ISI

- In-medium corrected primary interaction cross sections, boosted to rest frame of moving bound nucleon in local Fermigas
- Includes spectral functions for baryons and mesons (binding + collision broadening)
- *Hadronic couplings* for FSI taken from PDG (Manley anal.)
- *Vector couplings* taken from electro-production (MAID)
- *Axial couplings* modeled with PCAC



Reaction Types

- 2 major reaction types relevant:
 1. QE scattering
 - I. true QE (single particle interaction)
 - II. many-particle interactions (RPA + 2p2h + spectral functions)
 2. Pion production
 - I. through nucleon resonances ($W < 2$ GeV)
 - II. through DIS ($W > 2$ GeV)
- All reaction types are entangled:
final states may look the same

QE Scattering

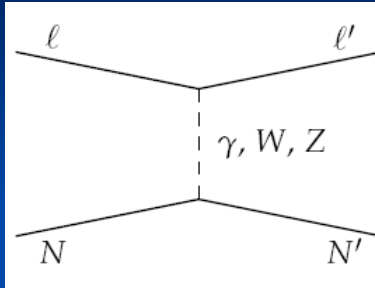
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Quasielastic Scattering



- Vector form factors from e -scattering
- axial form factors

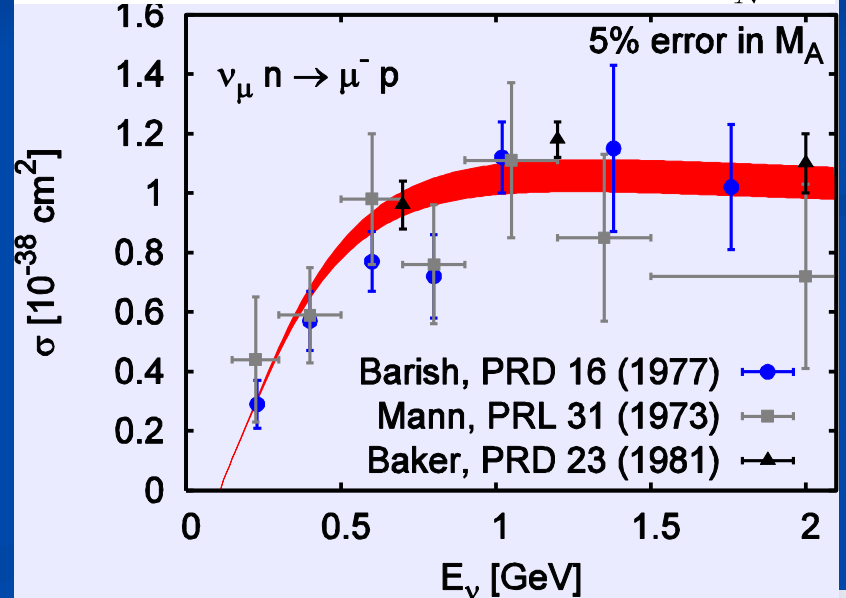
$F_A \Leftrightarrow F_P$ and $F_A(0)$ via **PCAC**

dipole ansatz for F_A with

$M_A = 1 \text{ GeV}$:

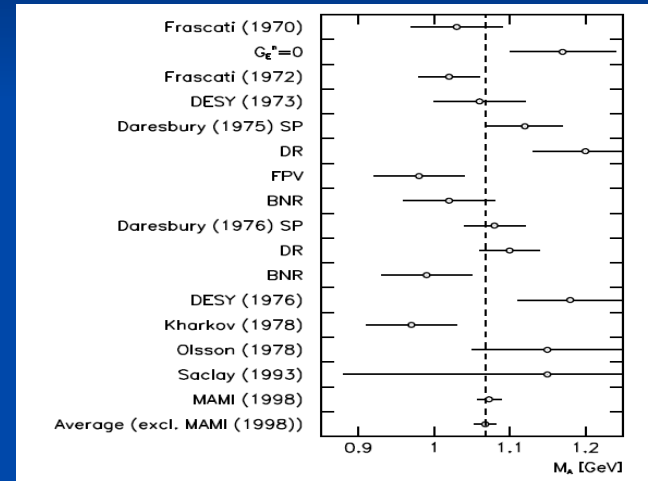
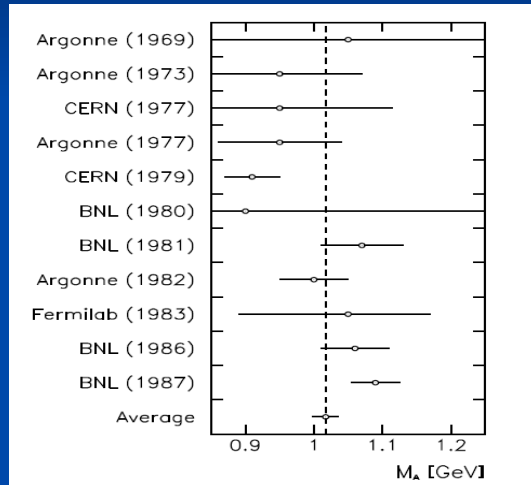
$$F_A(Q^2) = \frac{g_A}{\left(1 + \frac{Q^2}{M_A^2}\right)^2}$$

$$J_{QE}^\mu = \left(\gamma^\mu - \frac{\not{q} q^\mu}{q^2}\right) F_1^V + \frac{i}{2M_N} \sigma^{\mu\alpha} q_\alpha F_2^V + \gamma^\mu \gamma_5 F_A + \frac{q^\mu \gamma_5}{M_N} F_P$$



Axial Formfactor of the Nucleon

- neutrino data agree with electro-pion production data



$M_A \cong 1.02$ GeV world average

$M_A \cong 1.07$ GeV world average

Dipole ansatz is simplification, not good for vector FF

Spectral Functions

- Single particle spectral functions absorb effects of interactions in particle properties
- Free Fermi gas (in generators):

$$P_h(\mathbf{p}, E) = \Theta(\mathbf{p}_F - \mathbf{p}) \delta(E + T_p)$$

spiky E-dep. leads to artifacts in response

- Now: dress particle with interactions, mean field and/or additional interactions \rightarrow quasiparticles

Spectral Function in GiBUU

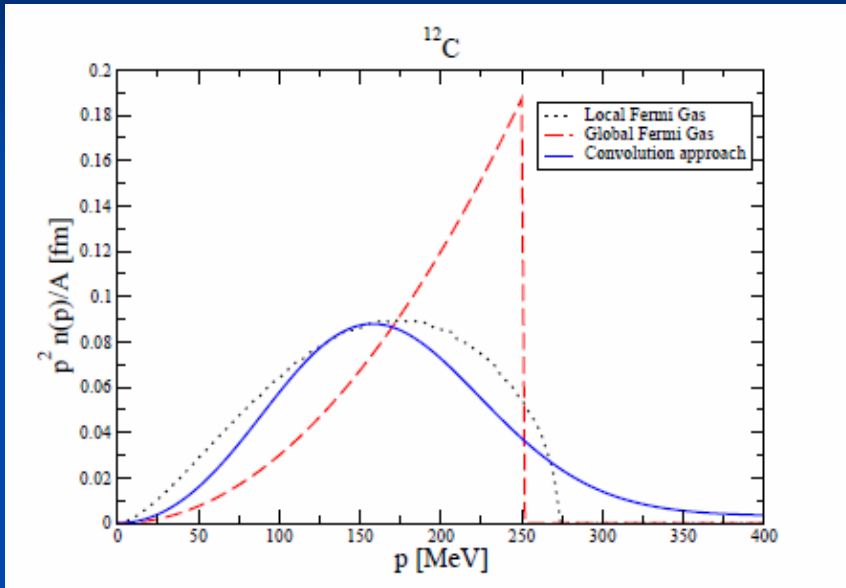
$$P_h(\mathbf{p}, E) = \int_{NV} d^3x [\Theta(p_F(\mathbf{x}) - \mathbf{p}) \delta(E + T_p + V(\mathbf{x}, \mathbf{p}))]$$

Two essential features:

1. Local TF momentum distribution removes artifacts of sharp cut at p_F
2. Particles bound in momentum- and coordinate-dependent potential, integration removes delta-function spikes in energy

Spectral function in GiBUU contains interactions in mean field

Nuclear Groundstate the same for all processes!



From:
Alvarez-Ruso, Hayato, Nieves

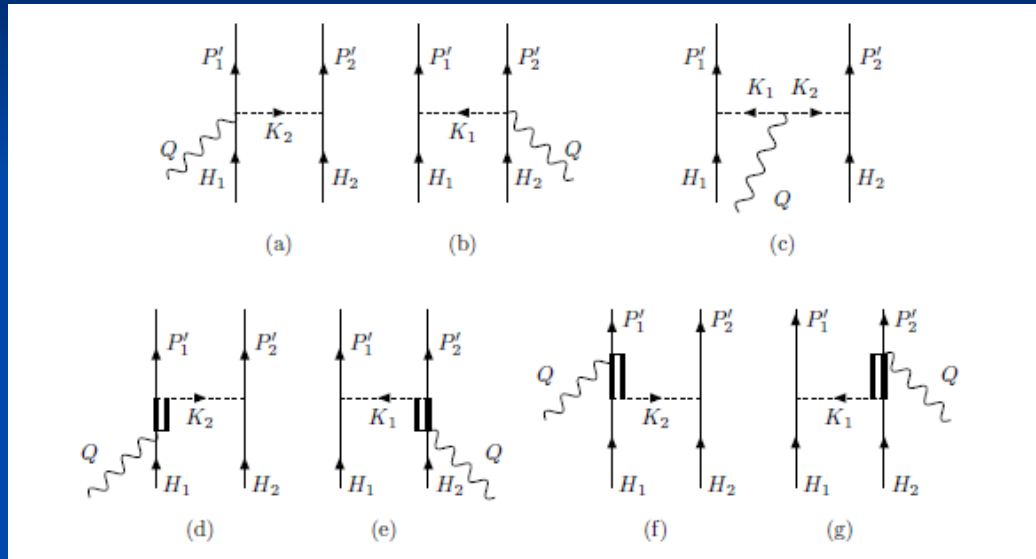
Also E -dependence is different
from Global Fermi Gas:
momentum and x -dependent
potential leads to smooth
behavior

GiBUU uses Local Fermi Gas + Nukleon mean field potential

2p-2h in Generators

- Mandatory: same nuclear ground state for 1p-1h and 2p-2h processes
 - Generators: free Fermi gas
 - Nieves 2p-2h model: dressed Fermi gas in mean field potential
- Nieves model cannot be simply added to simple generators: inconsistent → inconclusive

2p-2h and spectral functions



M.B. Barbaro et al,
2011

Cross section= sum over amplitudes squared

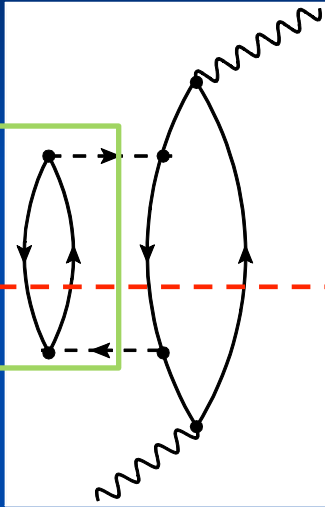
2p-2h and spectral functions

- Part of 2p-2h interactions is contained in spectral function
- Another part is missing!



2p-2p excitations and spectral functions

2nd ampl. squared



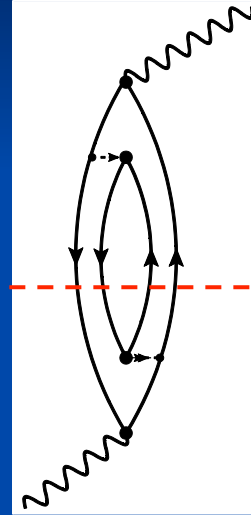
hole
selfenergy
 Σ

Cutkosky
cut

Hole Spectral Function

$$\mathcal{A}(x, p) = \frac{1}{\pi} \frac{\sqrt{p^{*2}} \Gamma_{\text{med}}}{[p^{*2} - m^{*2}]^2 + p^{*2} \Gamma_{\text{med}}^2}$$

Interference term squared



No selfenergy,
Vertex correction,
not included in spectral
function

Interference of ISI and FSI

GiBUU 2p2h

- Model for $\nu + p_1 + p_2 \rightarrow p_3 + p_4 + \mu$ (no recoil)

$$\frac{d^2\sigma}{dE'_l d(\cos\theta')} \propto \frac{k'}{k} \int_{NV} d^3r \int \prod_{j=1}^2 \frac{d^3p_j}{(2\pi)^3 2E_j} f_1 f_2 \overline{|M|^2} (1-f_3)(1-f_4) \delta^4(p)$$

with flux averaged matrixelement

$$\overline{|M|^2} = \int \Phi(E_\nu) L_{\mu\nu} W^{\mu\nu} dE_\nu$$

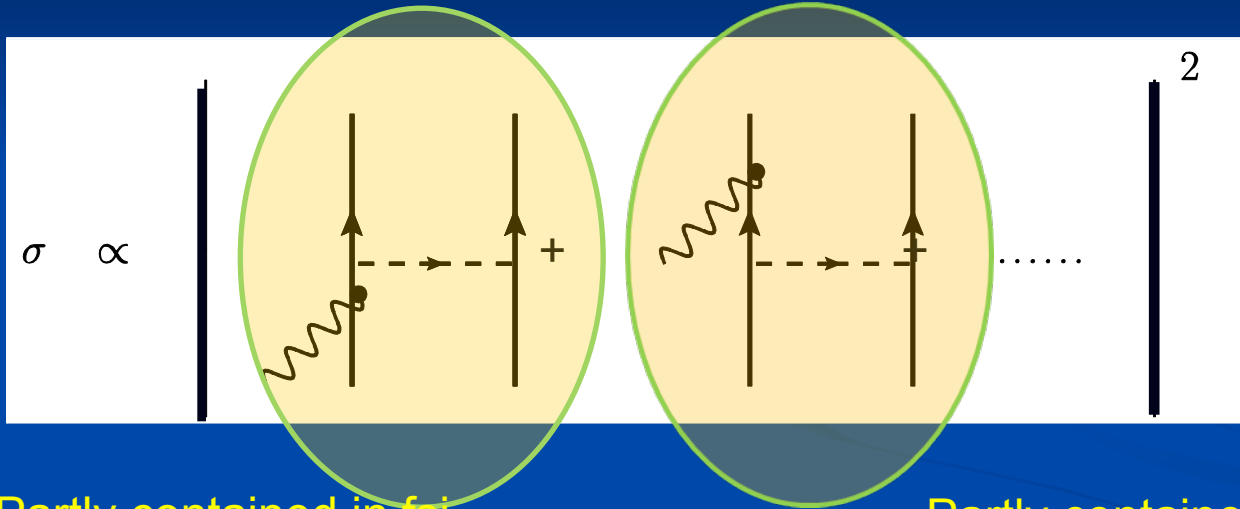
Flux smears out details in hadron tensor W
 W contains 2p-2h and poss. RPA effects

GiBUU 2p2h

- $W^{\mu\nu} = F(Q^2) P^{\mu\nu}_T(q)$
- Integration over initial states; final state phase space not integrated,
- Final state phase space calculated in 2p cm-system, then Lorentz-boosted to lab and Pauli-blocking applied



2p-2h Problems



Partly contained in fsi

Partly contained in SF

Double Counting Problem for 2p2h Implementation in Generators

Only adhoc ‚tune‘ in GiBUU

- Educated guess for 2p2h in GiBUU with tuned strength
- Big open question: up to which neutrino energies (or Q^2, ν) are models good?
- Compare with Lightbody-Bosted analysis



Pions

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Pion Production

$$J_{\Delta}^{\alpha\mu} = \left[\frac{C_3^V}{M_N} (g^{\alpha\mu} \not{q} - q^{\alpha} \gamma^{\mu}) + \frac{C_4^V}{M_N^2} (g^{\alpha\mu} q \cdot p' - q^{\alpha} p'^{\mu}) + \frac{C_5^V}{M_N^2} (g^{\alpha\mu} q \cdot p - q^{\alpha} p^{\mu}) \right] \gamma_5 \\ + \frac{C_3^A}{M_N} (g^{\alpha\mu} \not{q} - q^{\alpha} \gamma^{\mu}) + \frac{C_4^A}{M_N^2} (g^{\alpha\mu} q \cdot p' - q^{\alpha} p'^{\mu}) + C_5^A g^{\alpha\mu} + \frac{C_6^A}{M_N^2} q^{\alpha} q^{\mu}$$

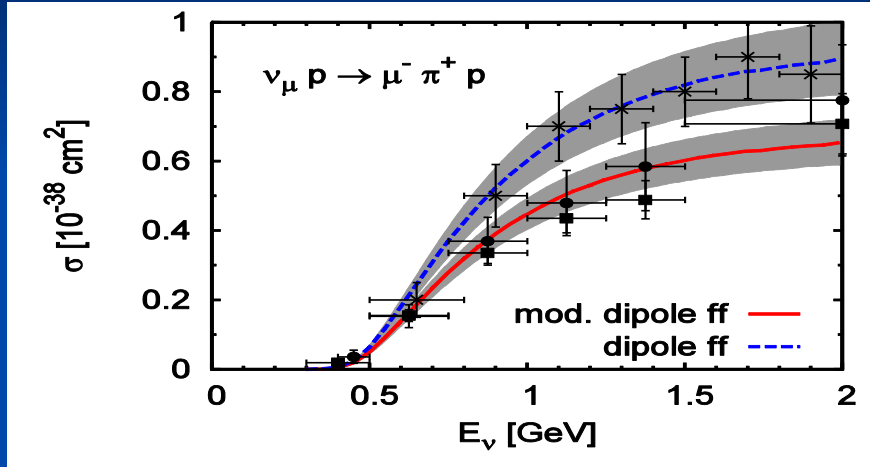
- 13 resonances with $W < 2$ GeV, non-resonant single-pion background, DIS
- pion production dominated by **$P_{33}(1232)$ resonance**:
- **C^V** from electron data (MAID analysis with CVC)
- **C^A** from fit to neutrino data (experiments on hydrogen/deuterium), so far only C_5^A determined, for other axial FFs only educated guesses

Pions

- Pion production amplitude
= resonance contrib + background (Born-terms)
- Resonance contrib
- V determined from e-scattering (MAID)
- A from PCAC ansatz
- Background:
 - Up to about Δ obtained from effective field theory
 - Beyond Δ unknown
 - 2 pi BG totally unknown



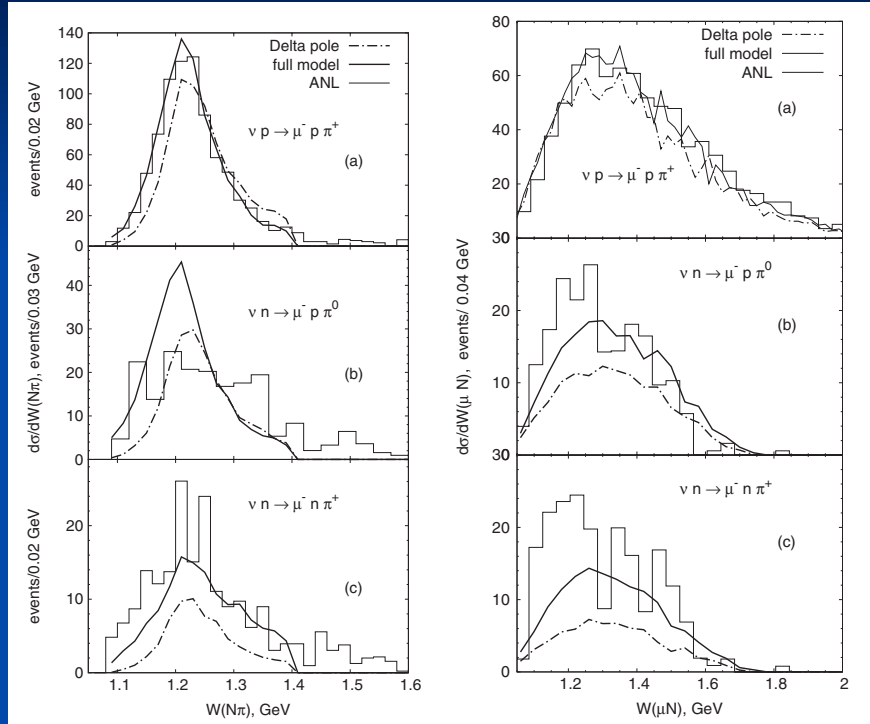
Pion Production



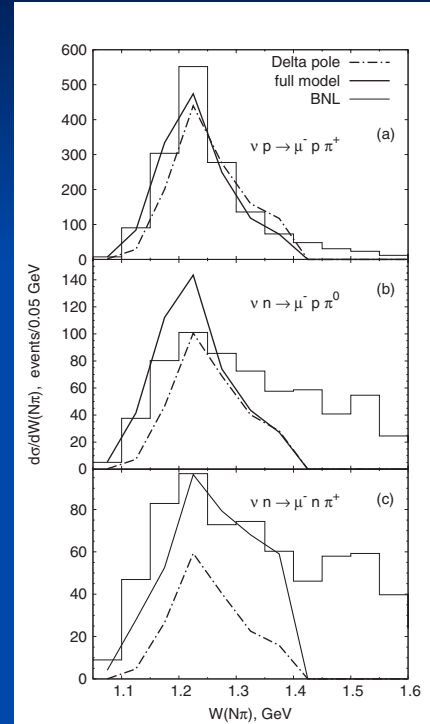
data:
PRD 25, 1161 (1982), PRD 34, 2554 (1986)

discrepancy between elementary data sets
→ impossible to determine 3 axial formfactors

π -N inv. Mass Distributions



ANL data



BNL data

Lalakulich et al.,
Phys. Rev. D 82,
093001 (2010)



Hadronization

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Observables, Experiments

■ multiplicity ratio

$$R_M^h(z_h, \dots) = \frac{\left(\frac{N_h(z_h, \dots)}{N_e(\dots)}\right)_A}{\left(\frac{N_h(z_h, \dots)}{N_e(\dots)}\right)_D}$$

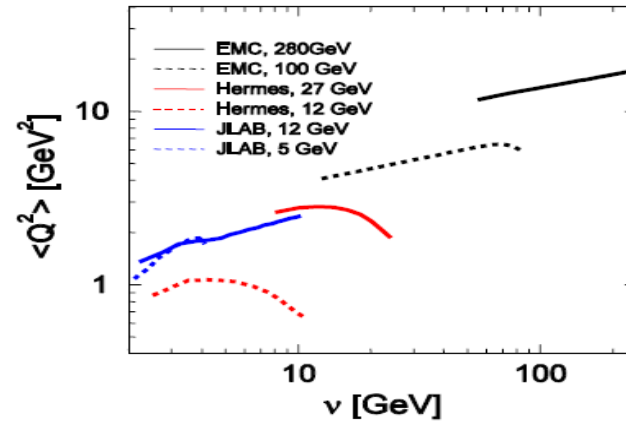
■ hadronic: $z_h = \frac{E_h}{\nu}$, p_\perp , ...

■ photonic: ν , Q^2 , W , x_B , ...

■ Experiments

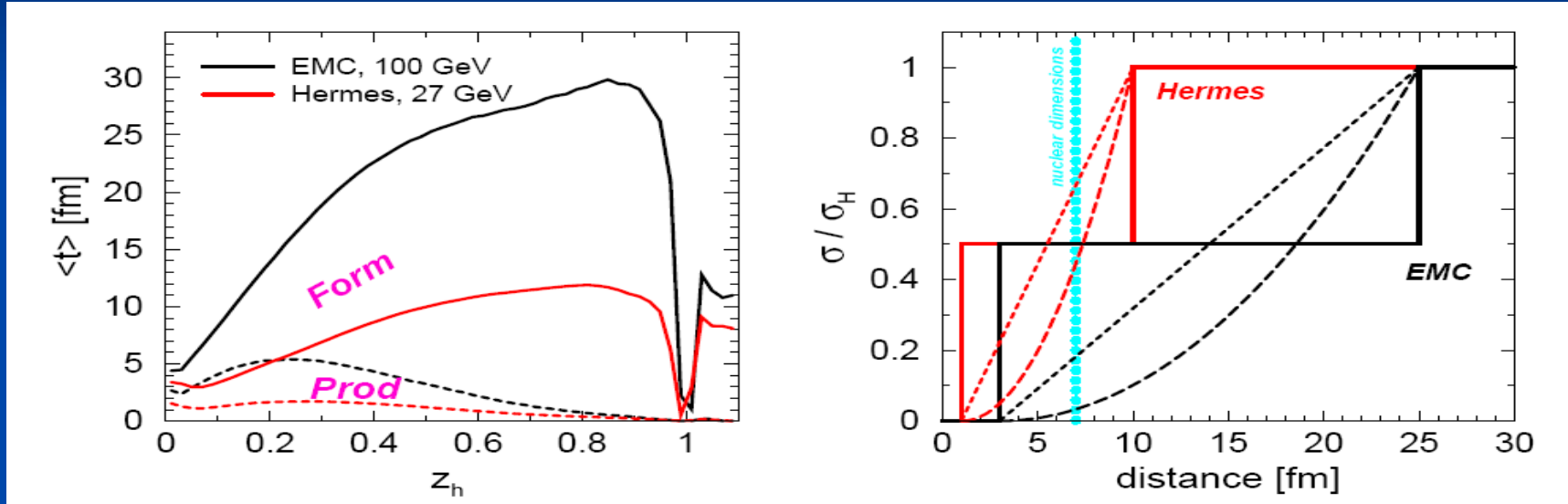
	$E_{\text{lepton}} =$
■ EMC	100...280 GeV
■ Hermes	27 GeV
■ Hermes	12 GeV
■ CLAS	12 GeV
■ CLAS	5 GeV

...multiple combinations of targets



Production and Formation Times from PYTHIA

$$z_h = E_h/v$$



All times in lab (nucleus) frame, from Falter & Gallmeister, Phys.Lett.B630:40-48,2005

Times at low (< 1 GeV) energies

- Physics dominated by isolated nucleon resonances, e.g.:



- Lifetime of Δ determines production time of pion, formation time is zero (because hadrons are produced in their ground states, due to phase-space limitation)

Times at Low Energies

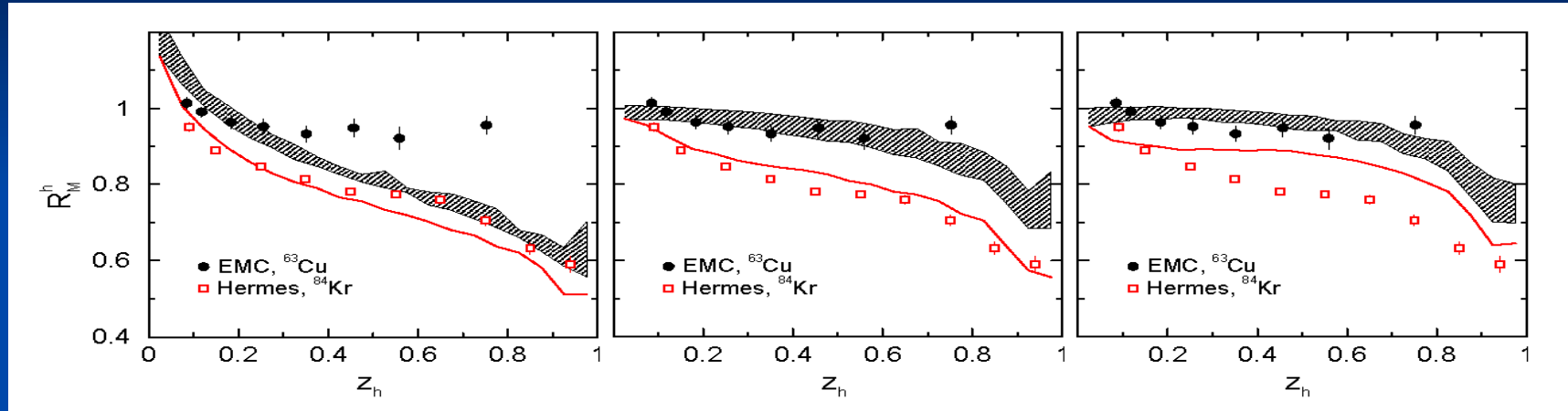
- Naive guess for production time:

$$\tau_p = 1/\Gamma_0 \quad (\Gamma_0 = \text{free resonance width})$$

- Educated guess:

$$\tau_p = 1/(\Gamma_0 + \Gamma_{\text{coll}}) \text{ with } \Gamma_{\text{coll}} = \rho v \sigma$$

Attenuation: EMC and HERMES



$\sigma_{\text{pre}} =$

const (0.5)

linear

quadratic

Attenuation Data are sensitive to details of prehadronic interactions!



Prehadronic Cross Section

- From now on quantum diffusion model

(Farrar et al.)

$$\sigma_{\text{eff}} = \sigma_{\text{hN}} \left[\left(\frac{\#}{Q^2} \right) \left(1 - \frac{t}{t_f} \right) + \left(\frac{t}{t_f} \right) \Theta(t_f - t) + \Theta(t - t_f) \right]$$

- $1/Q^2$ dependence not essential,
linear dependence on time is essential



Summary of Formation Times

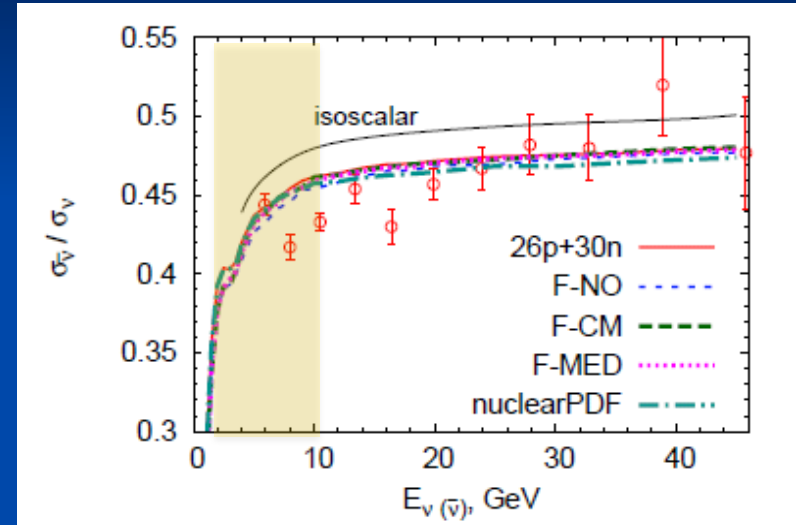
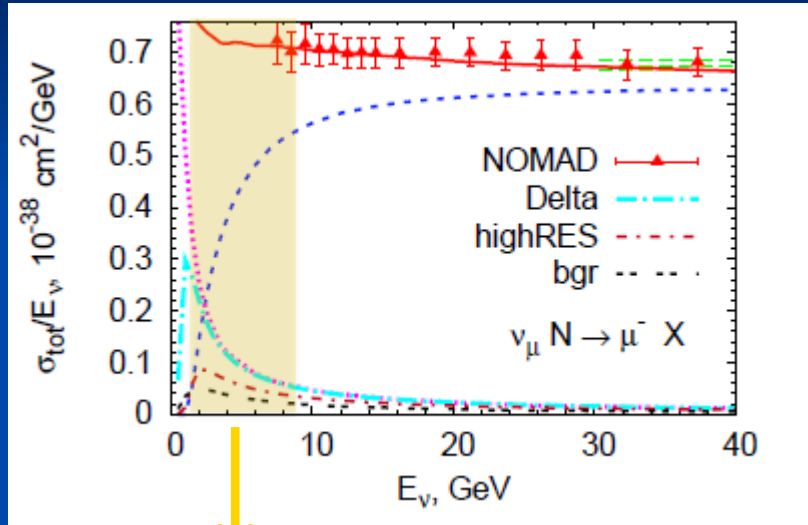
■ Times

- At low energies, resonance regime:
 $t_f = \text{lifetime of resonance} \rightarrow N + \text{hadron}$
- At high energies, QCD regime,
 t_f from string-fragmentation

■ Interactions

- At low energies: collisional broadening of resonances
 \rightarrow cross sections are density dependent!
- At high energies: nuclear attenuation

SIS – DIS by PYTHIA



Shallow Inelastic Scattering,

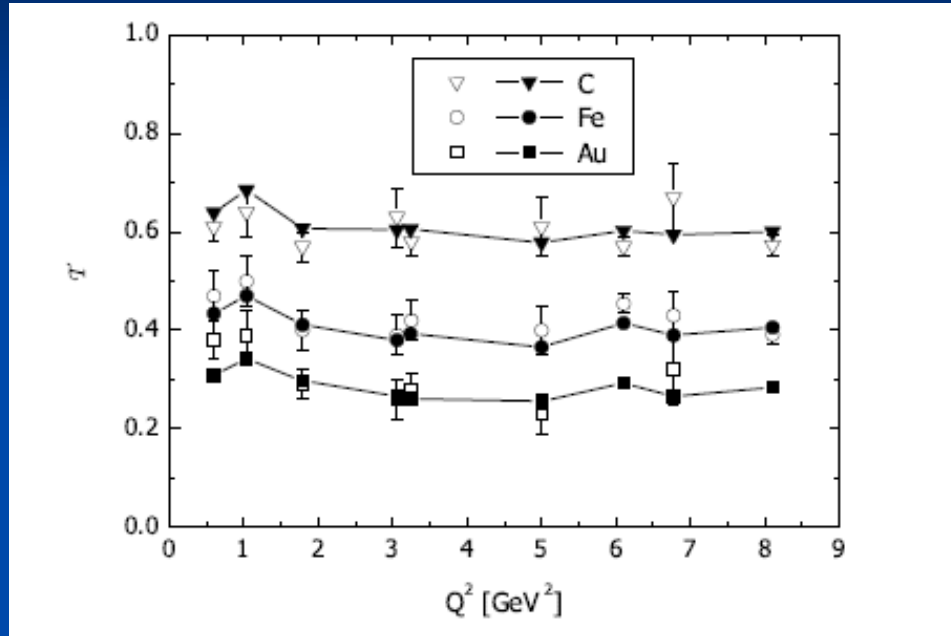
interplay of different reaction mechanisms

→ Ambiguity to switch from one mechanism to the other

Code and Theory Checks



Check: protons



Curves: GiBUU

Proton transparency

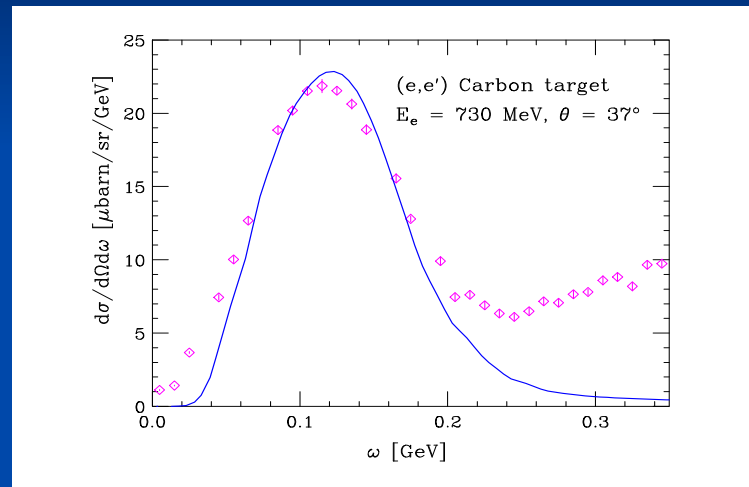
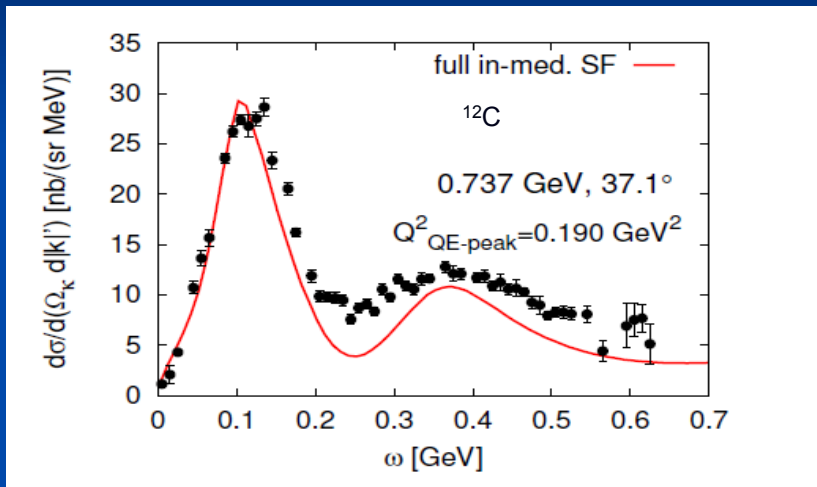
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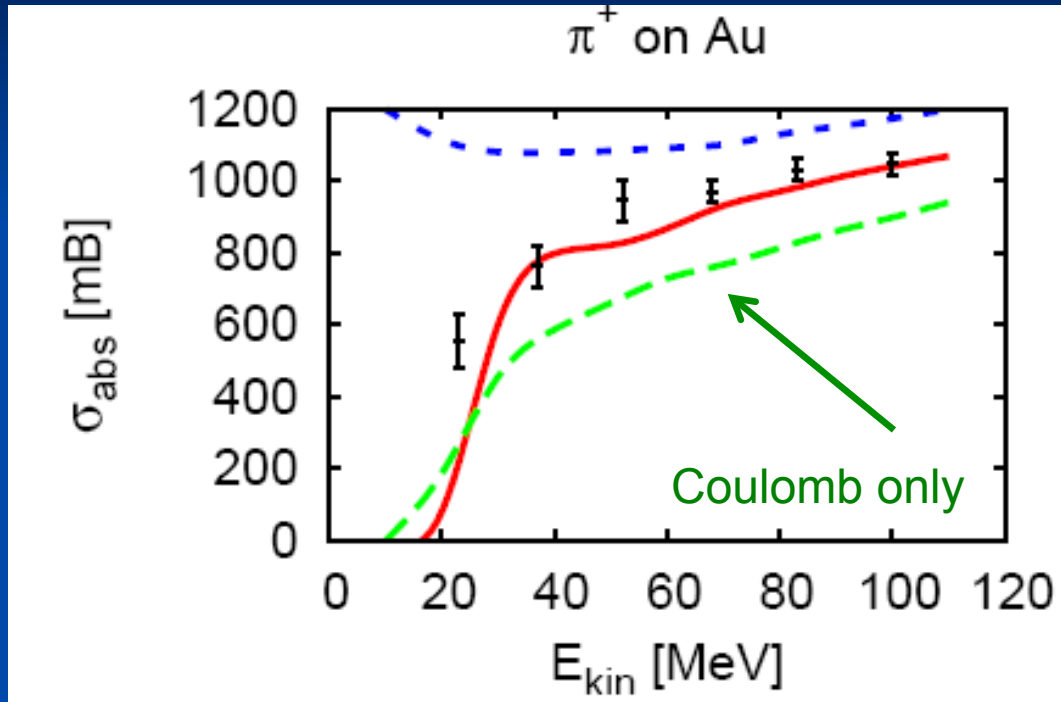
Electrons as Benchmark for GiBUU



No free parameters!
no 2p-2h, contributes
in dip region and under Δ

O. Benhar, spectral fctn

Check: Pion Absorption



Pion potential essential,
as well as Coulomb

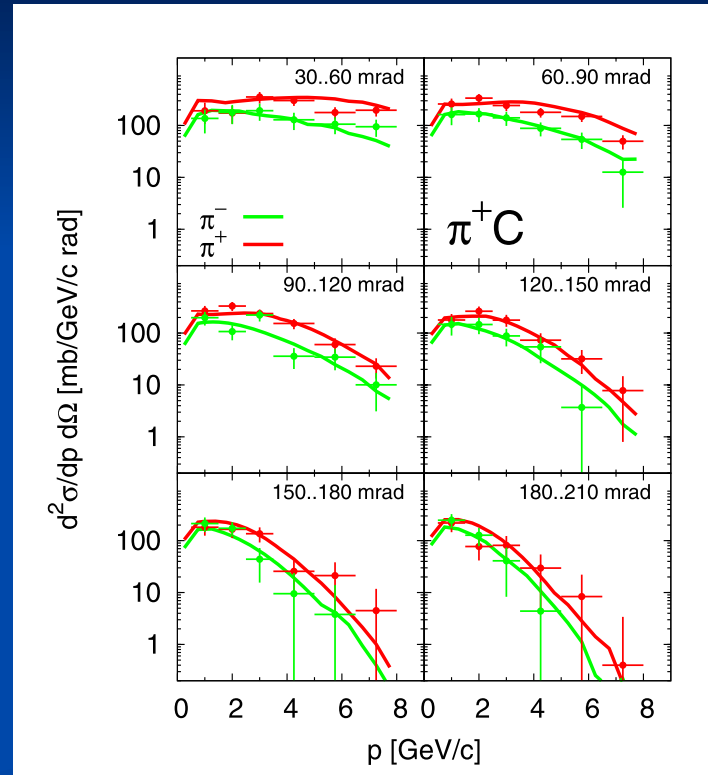
Note: Pion absorption
does not provide a
sensitive test for fsi with
nucleons

Check: pions in HARP

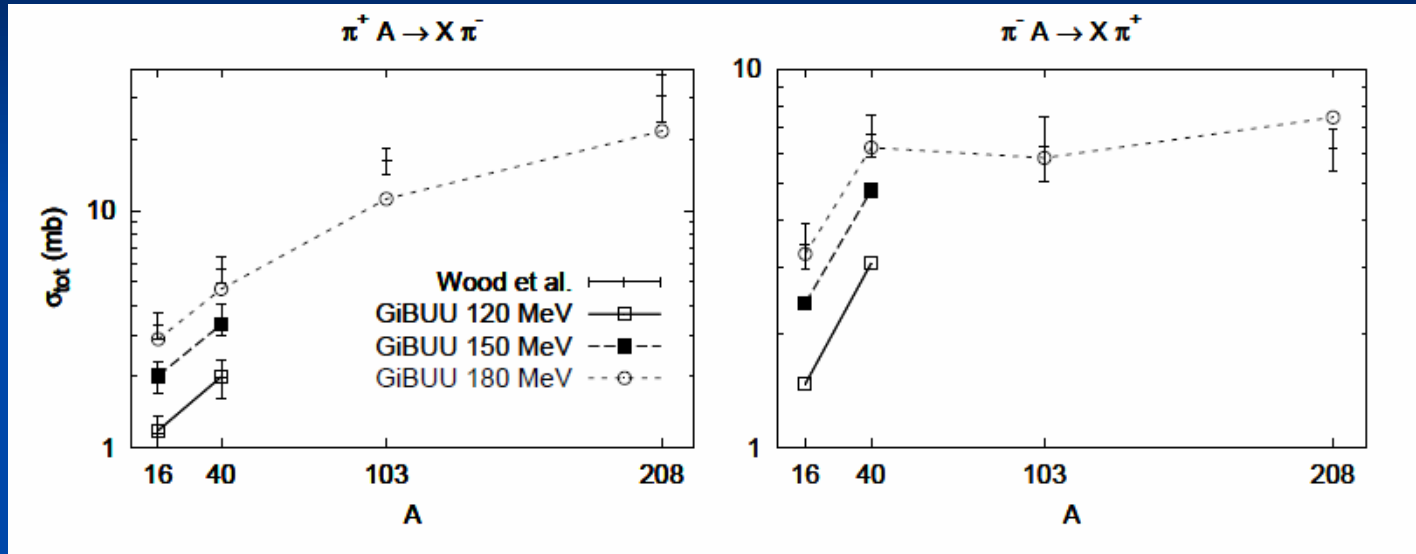
HARP small angle analysis
12 GeV protons

Curves: GiBUU

K. Gallmeister et al, NP A826 (2009)



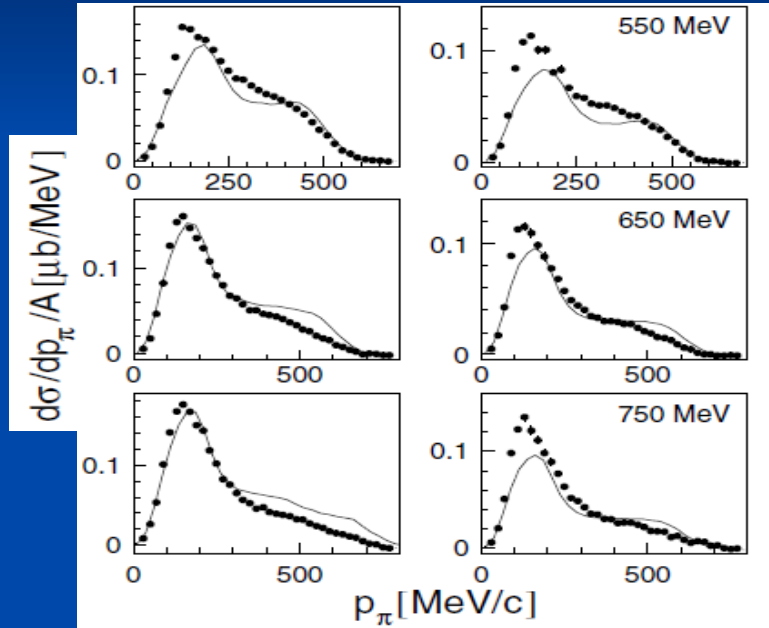
Check: Pion DCE



Data: Wood et al, GiBUU: Buss et al, **Phys.Rev. C74 (2006) 044610**

Check: Pions in Nuclei

$\gamma \rightarrow \pi^0$ on Pb

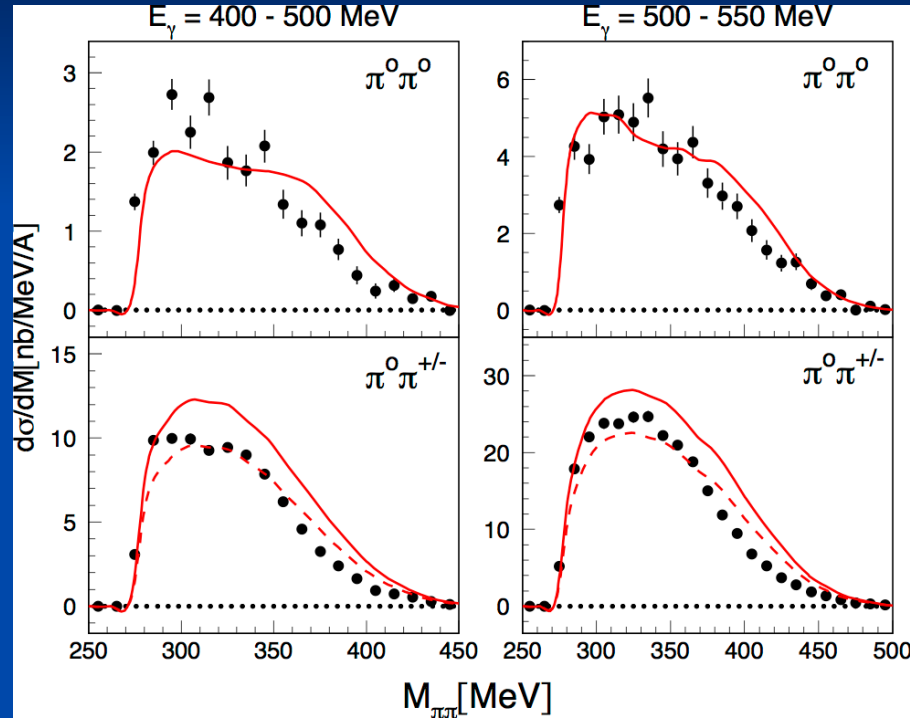


Photons illuminate the whole nucleus,
test various pion mean free paths

Data: TAPS, Krusche et al

As in neutrino-induced reactions pions
are produced inside the nucleus,
more sensitive than pion absorption checks

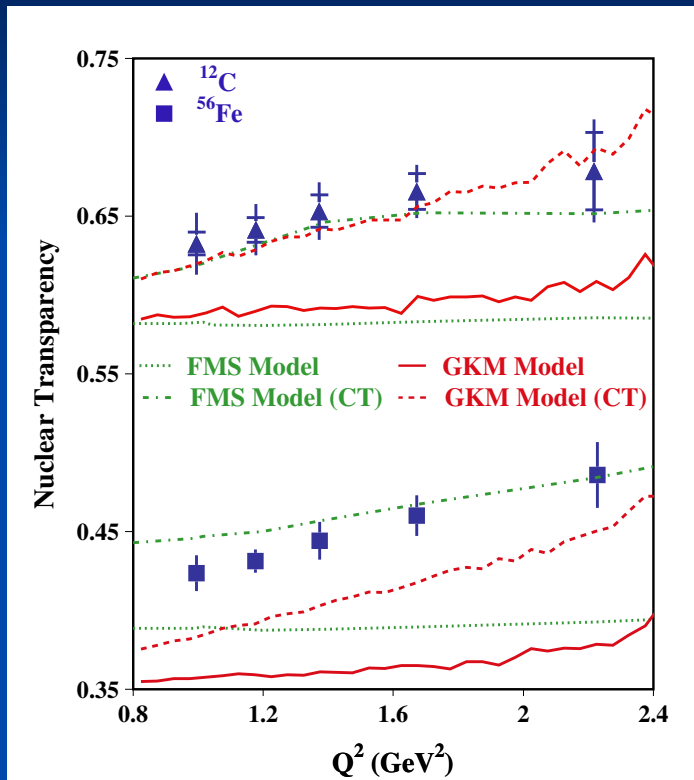
Check: Pions in Nuclei



Data:
TAPS
Krusche et al

Target: Ca

JLAB ρ Production

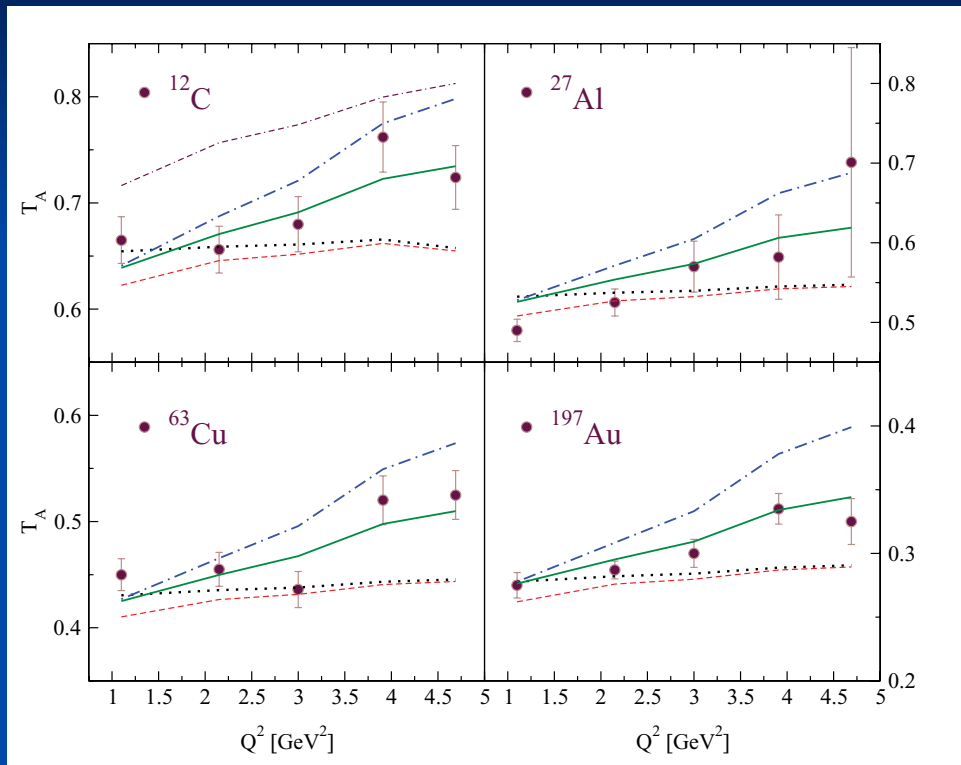


Exp: Hafidi et al, Hall B
Phys.Lett. B712 (2012) 326-330

GiBUU: Gallmeister et al.
Phys.Rev. C83 (2011)



Pion Production at JLAB

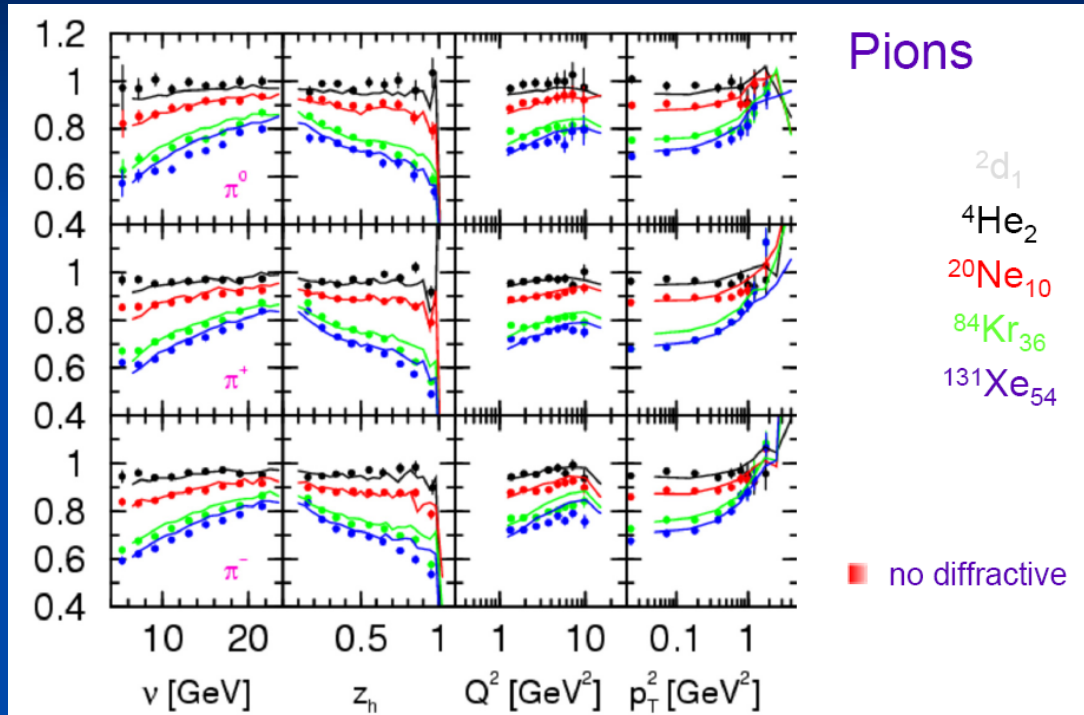


Exp: B. Clasie et al., Hall C
Phys. Rev. Lett. 99, 242502 (2007).

GiBUU: Kaskulov et al,
Phys.Rev. C79 (2009) 015207

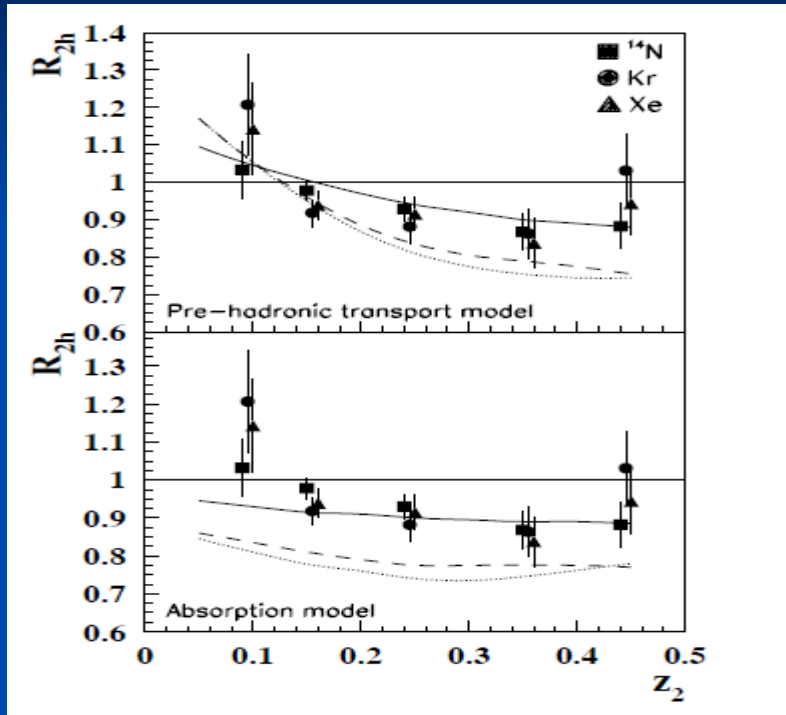


Pions from HERMES at 27 GeV



Data:
Airapetian et al
Curves: GiBUU
Nucl.Phys. A801
(2008) 68-79

Double Hadron Attenuation



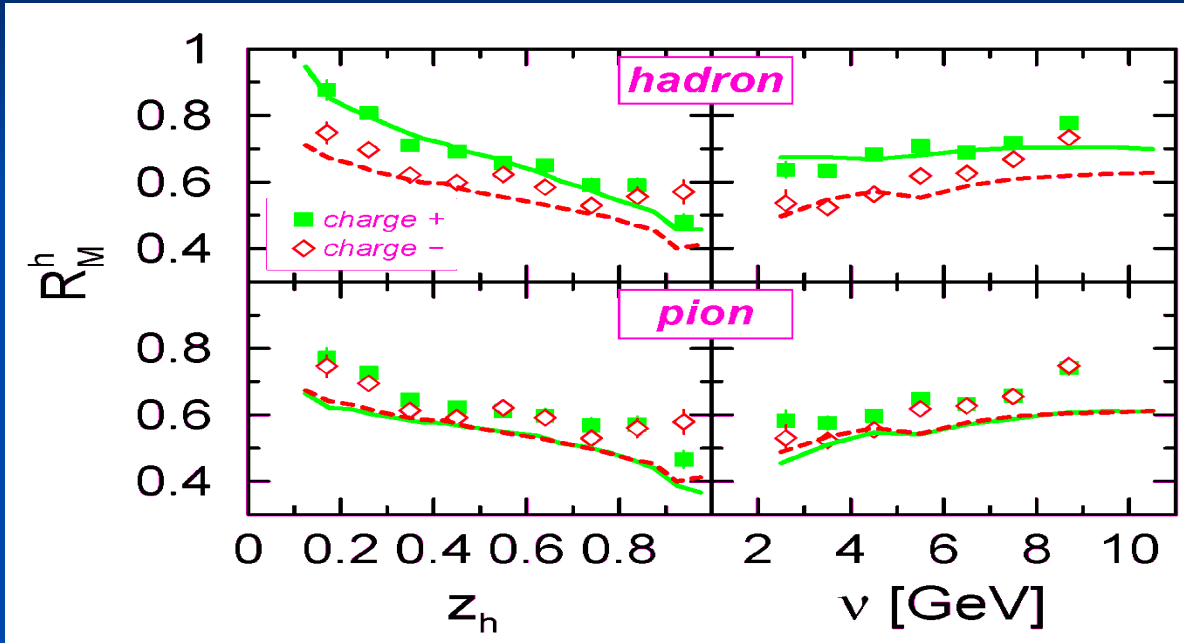
Glauber: fails at low z_2 .

Low z hadrons show pile-up through final state interactions

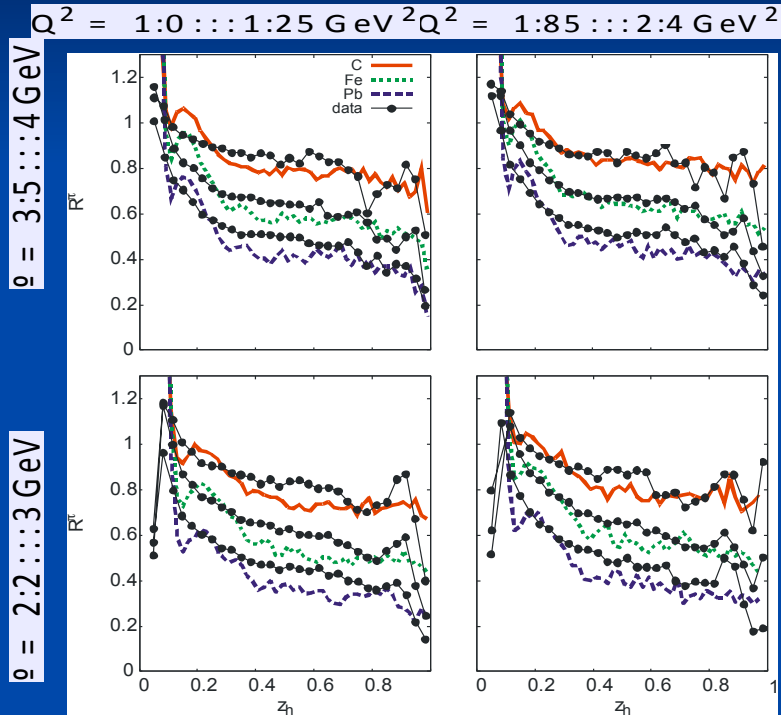
Implication for $(e,e'2p)$?



HERMES@12 GeV



JLAB π^+ production



Data: W. Brooks et al., JLAB

Same parameters as for HERMES



Now to Neutrinos

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Experimental Verification of 2p2h

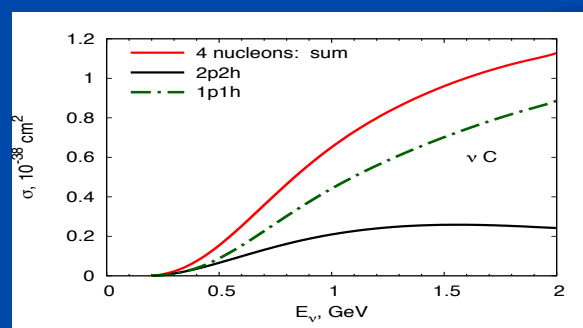
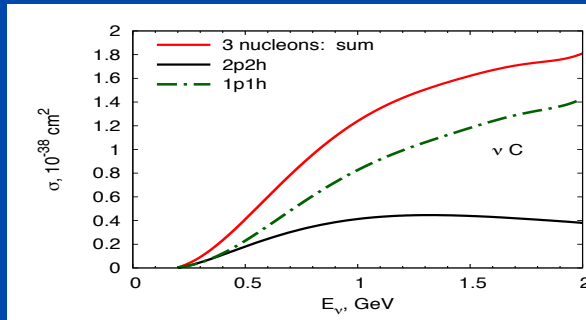
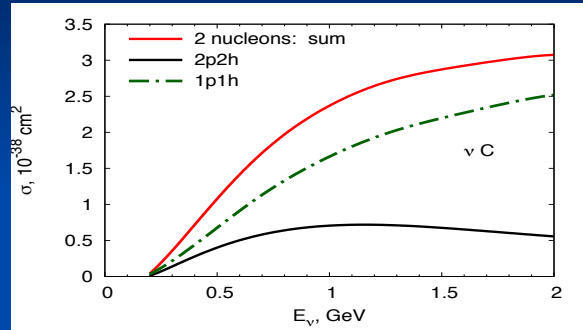
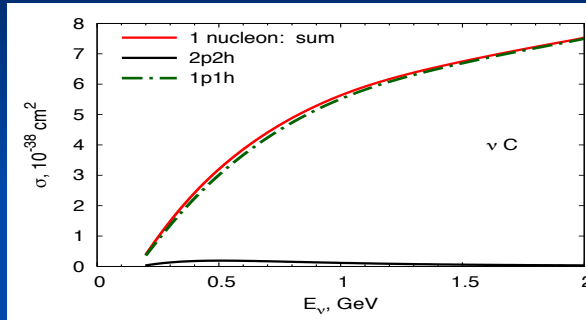
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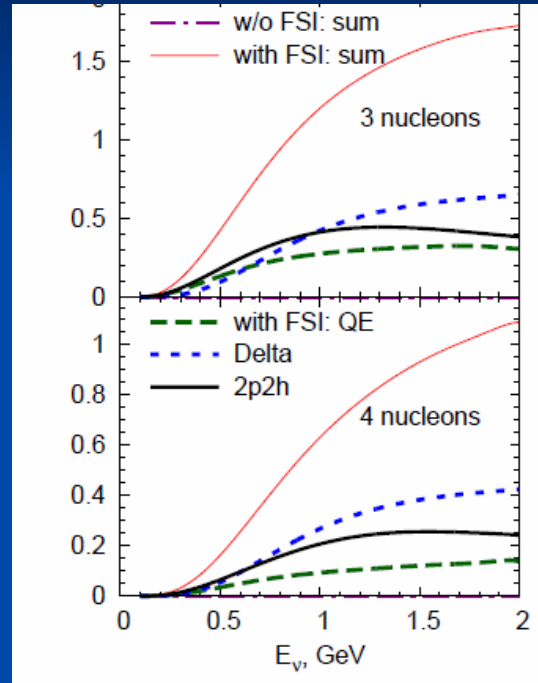
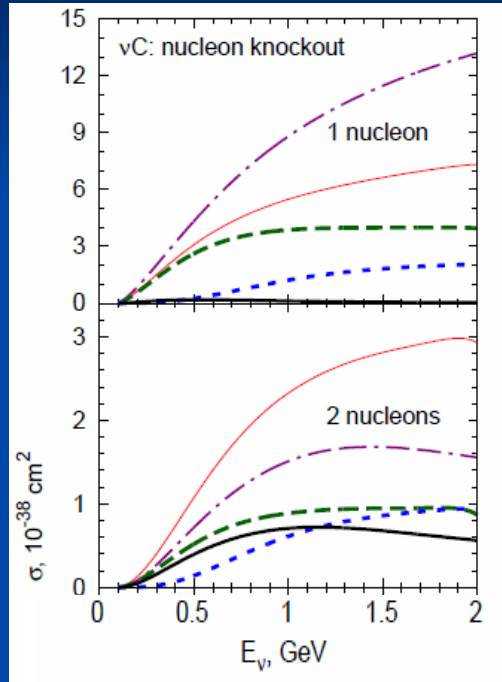
Nucleon Knock-Out for various processes



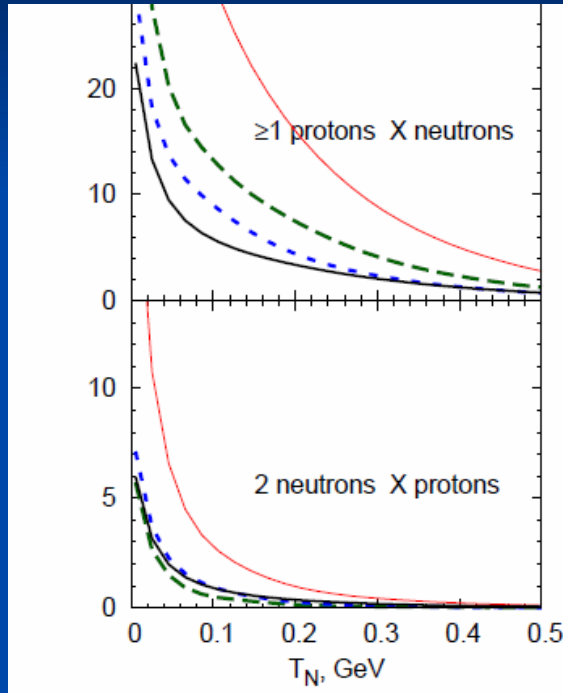
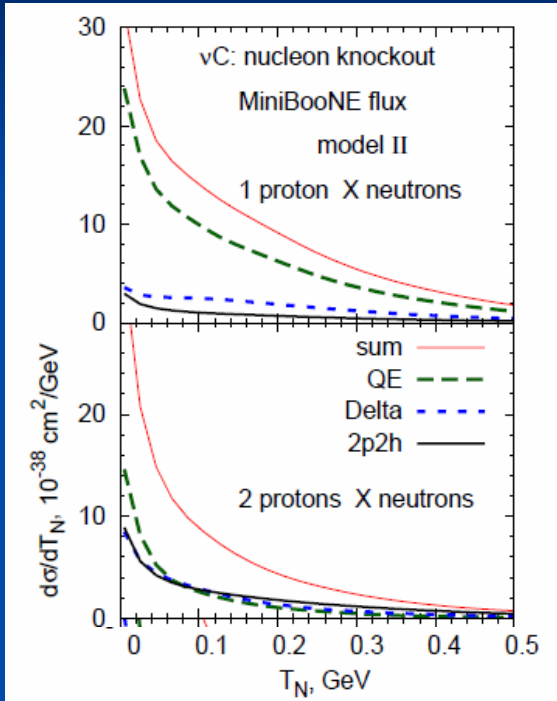
Only true QE
can be identified

Avalanching shadows
Initial reaction

Nucleon Knock-out and 2p-2h



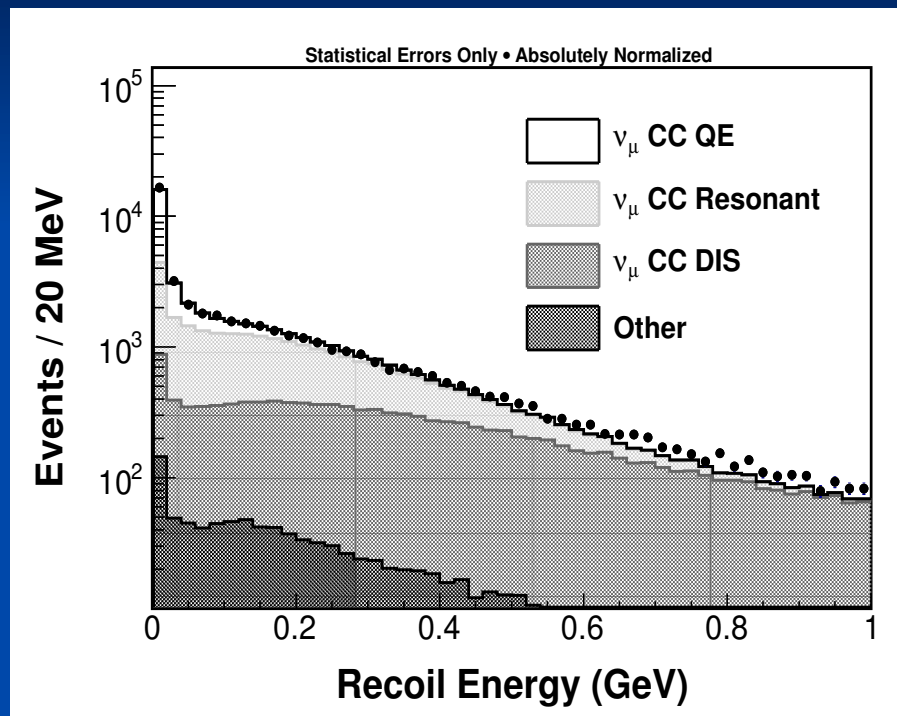
Nucleon Knock-out and 2p-2h



MB flux

Only 1pXn channel
is reasonably close to
true QE

MINERvA QE Analysis



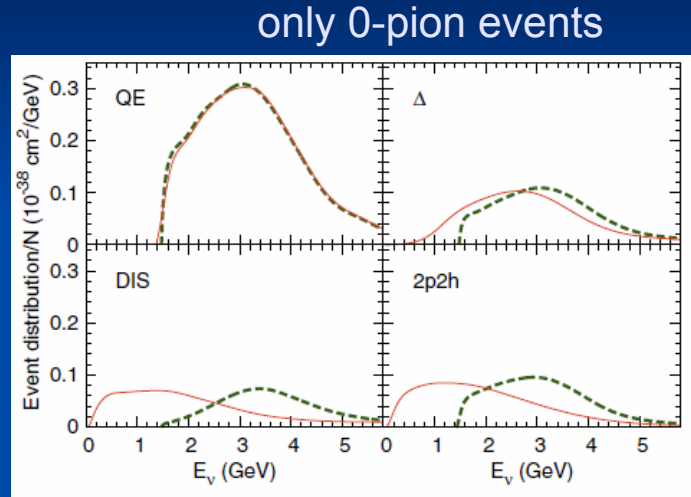
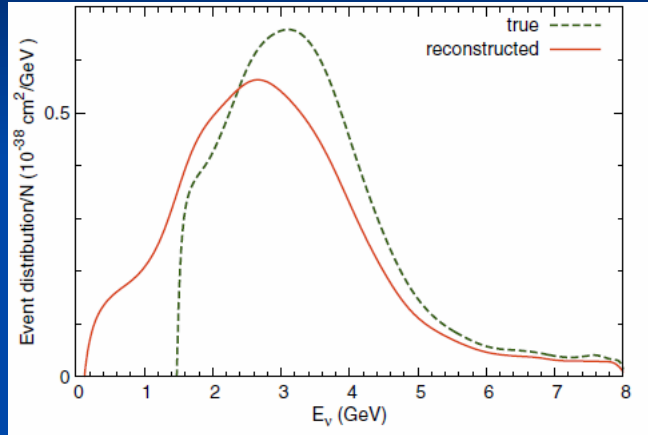
QE is a small part of the X-section over a large X-section

Background identification depends on generator



QE signal
generator-dependent

MINERvA Analysis



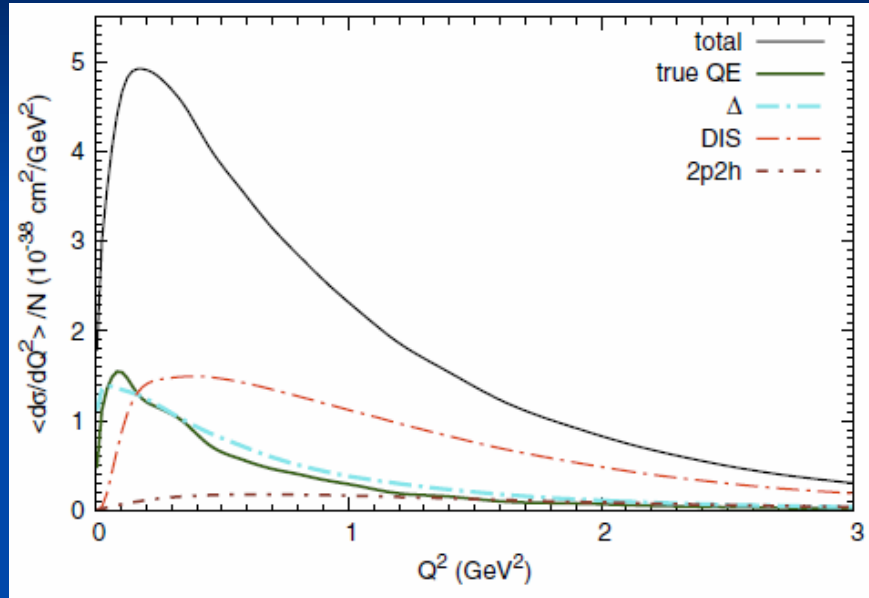
Mosel et al.,
PR D89 (2014) 093003

Flux cuts are dangerous:
distort true distribution!
Minerva cuts out (too?) large part

Energy reconstruction
strongly affected by
all channels, not just 2p2h!



Minerva Q^2 Reconstruction



Dominant:
QE, DIS, Δ

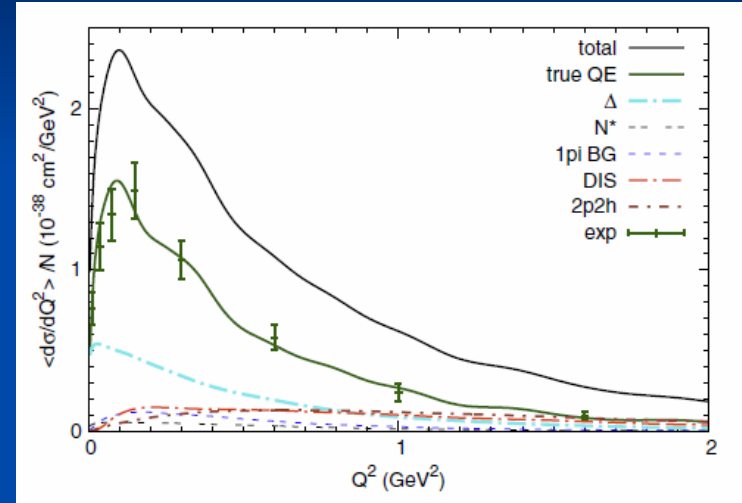
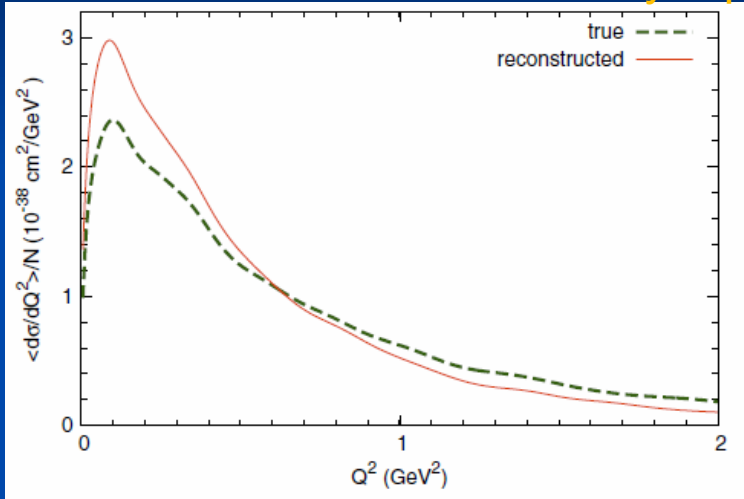
Δ and true QE very
similar,
difficult to separate

Mosel et al.,
PR D89 (2014) 093003

True Q^2 distribution, *all* events

MINERvA Q^2 Reconstruction

Only 0-pion events

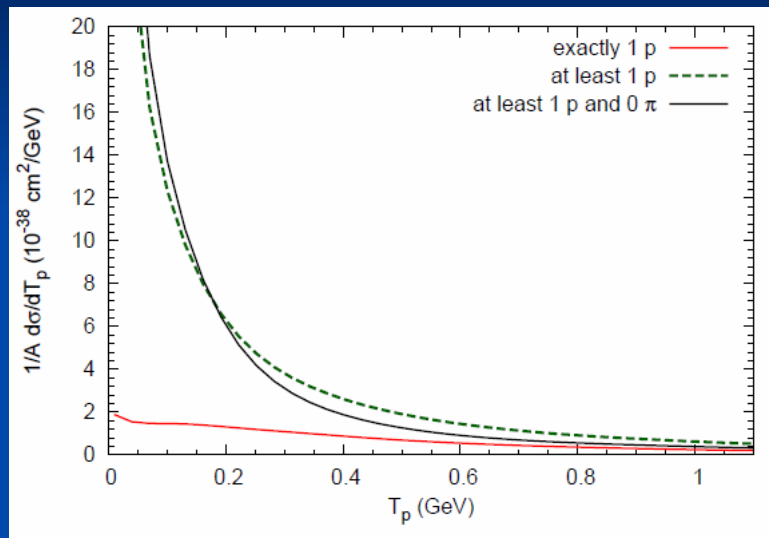


Dramatic sensitivity to reconstruction in peak area: can be removed with generator,
But: how good is your generator? accuracy of 'data'??

Mosel et al.,
PR D89 (2014) 093003



Nucleon Knock-out at MINERvA



Extremely strong fsi:
fast initial proton becomes many low-energy nucleons

Pion Production

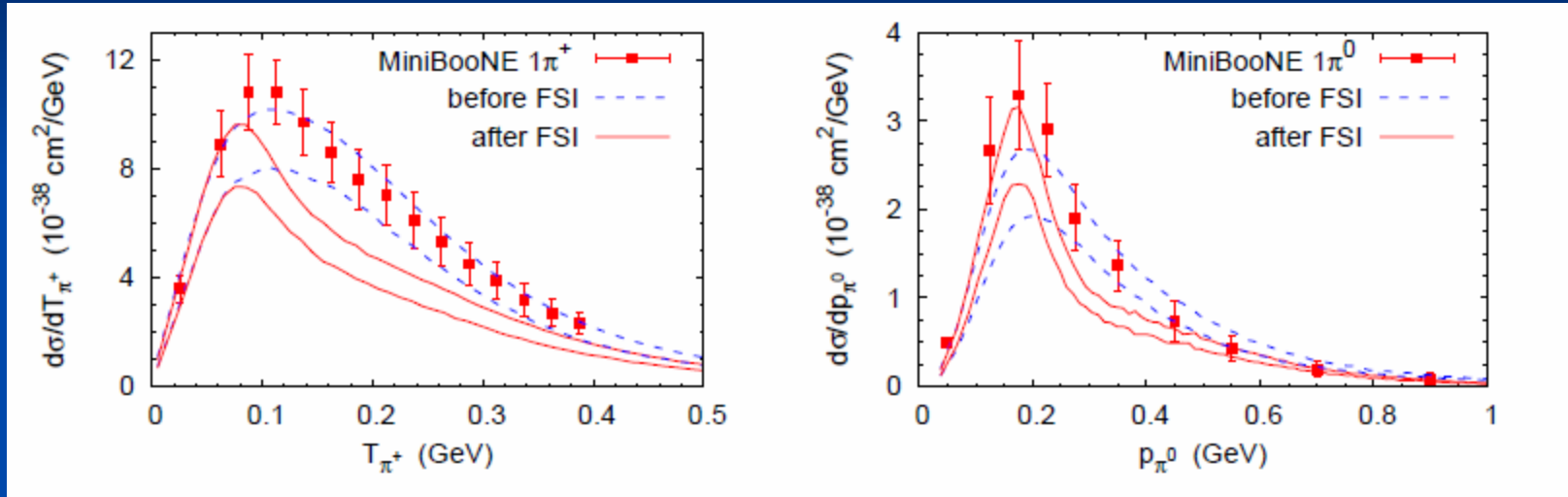
from: Phys.Rev. C87 (2013) 014602

1p-1h-1 π X-section:

$$d\sigma^{\nu A \rightarrow \ell' X \pi} = \int dE \int \frac{d^3 p}{(2\pi)^3} P(\mathbf{p}, E) f_{\text{corr}} d\sigma^{\text{med}} P_{\text{PB}}(\mathbf{r}, \mathbf{p}) F_{\pi}(\mathbf{q}_{\pi}, \mathbf{r}) .$$

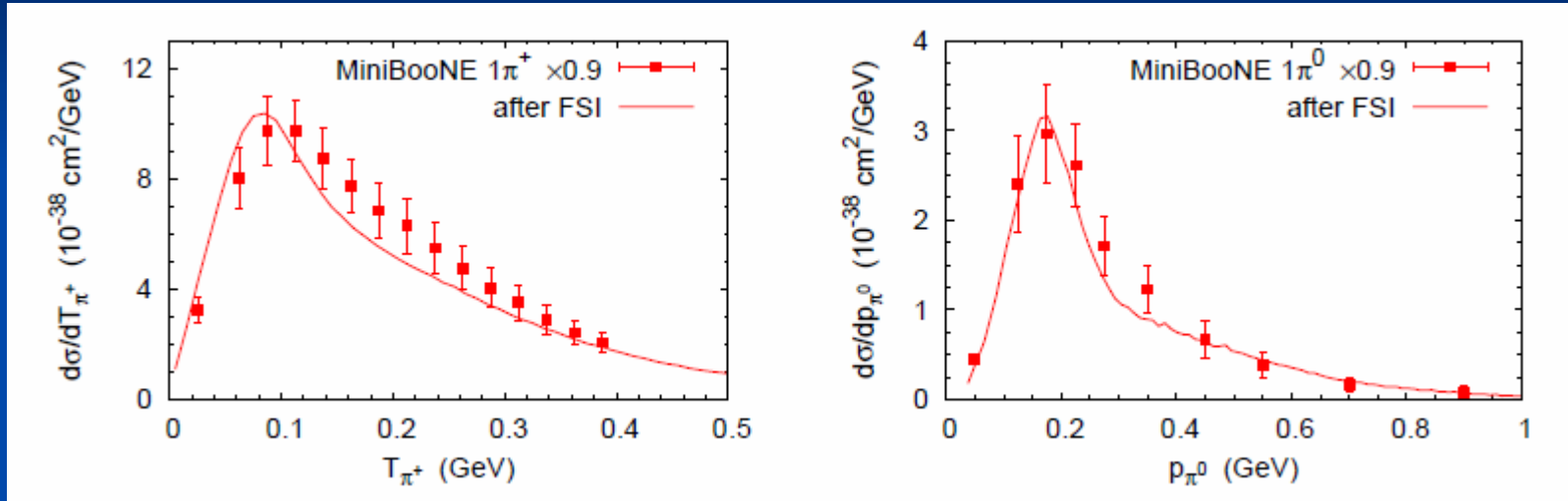
Pion fsi (scattering, absorption, charge exchange) handled by transport,
Includes Δ transport, consistent width description

Pion Production in MB



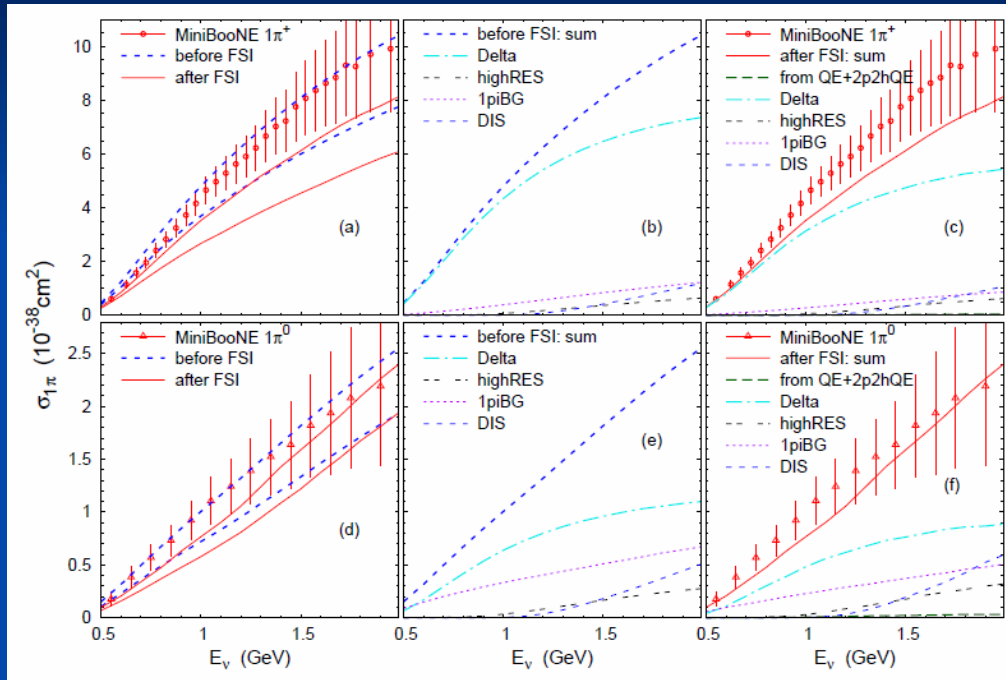
Spectral shape determined by pi-N-Delta dynamics in nuclei,
spectral disagreement due to choice of Bayes prior distributions???

Pion Production in MB



Flux renormalization (data $\times 0.9$ (cf. Nieves QE analysis))

Pion Production



Upper line: BNL input
 Lower line: ANL input

Tendency for theory too low, more so for π^+ , at $E > 1 \text{ GeV}$

DIS and higher resonances contribute for $E > 1 \text{ GeV}$

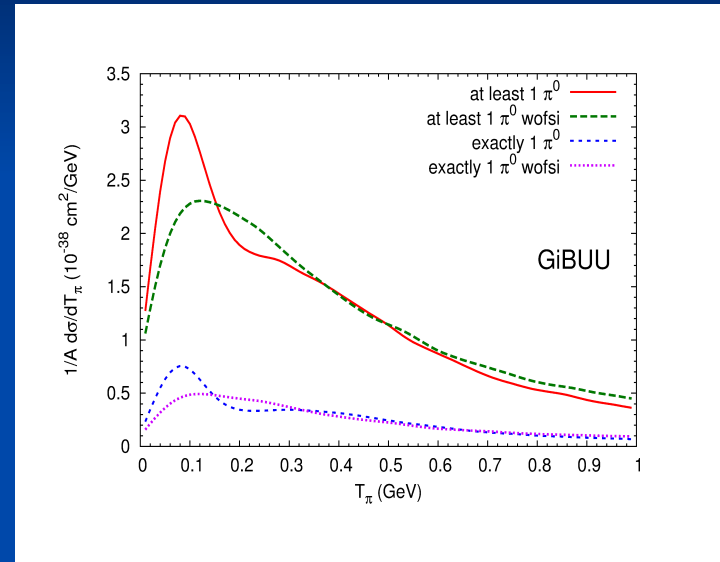
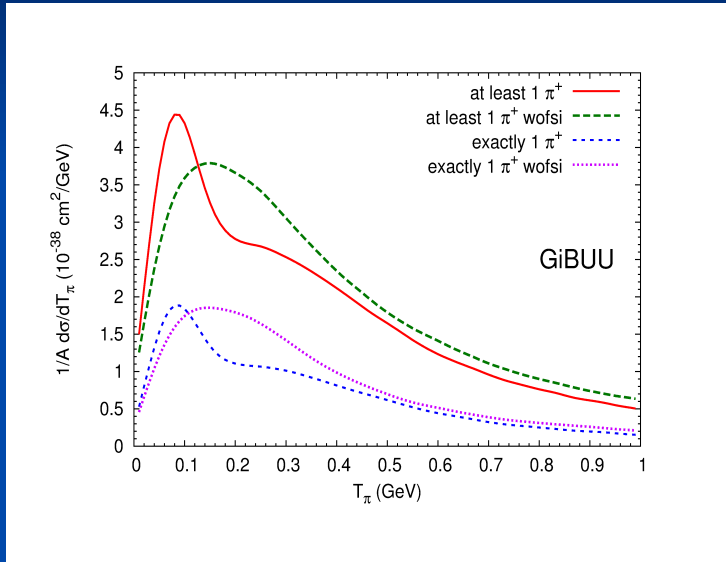
Discrepancy mainly in tail of flux distributions (large uncertainty)

Pions at MB

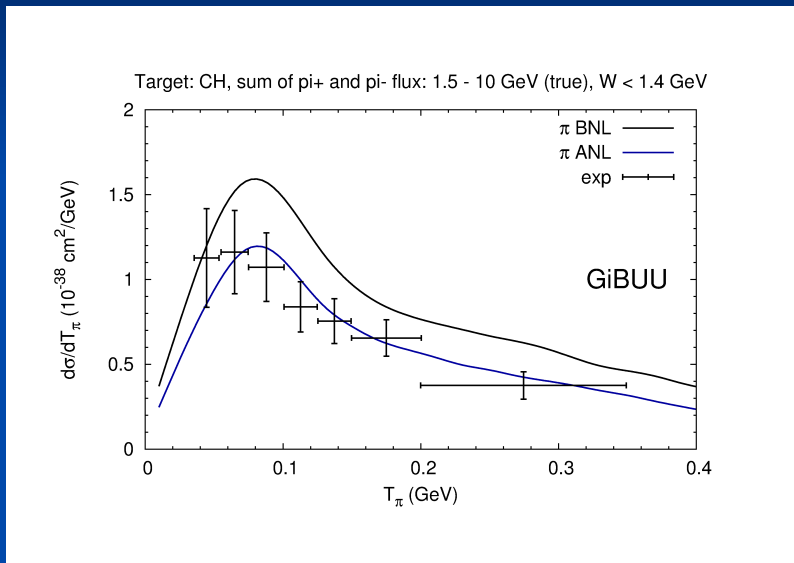
- Pions at MiniBooNE are compatible only with the (higher) BNL input



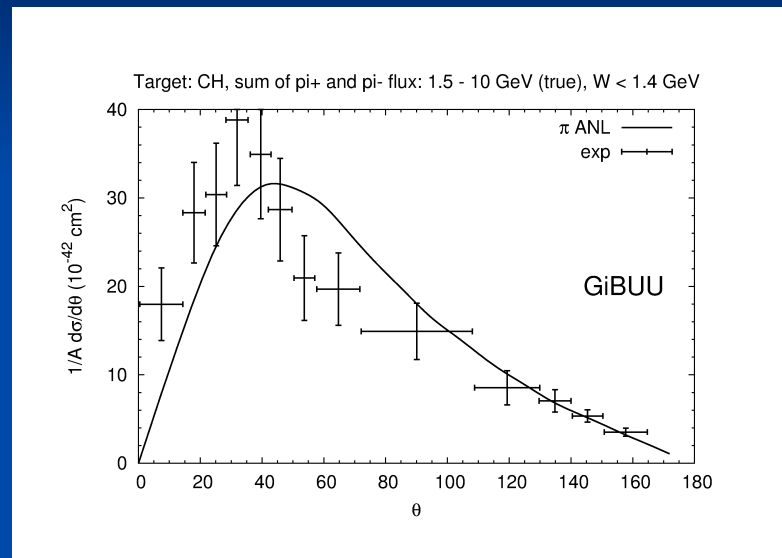
Pion FSI at MINERvA



MINERvA Pions



Data: Eberly et al



GiBUU preliminary

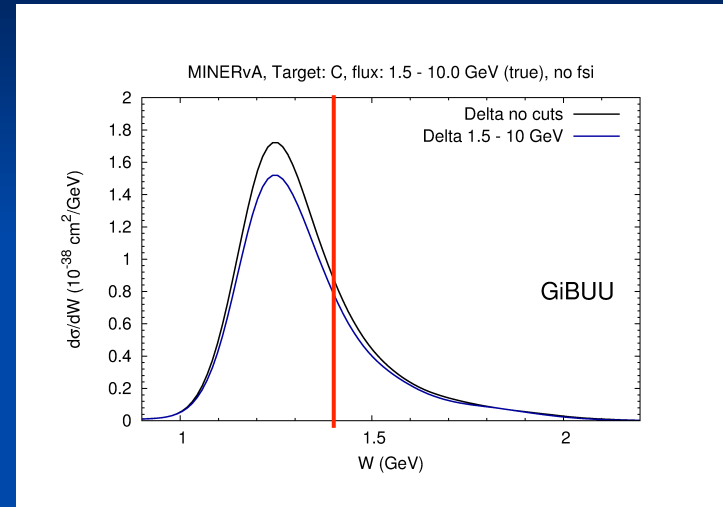
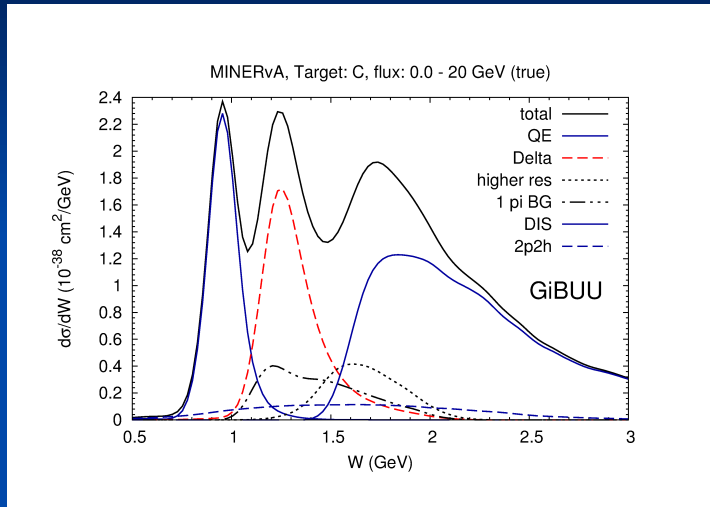
Pions at MINERvA compatible only with lower ANL data

MINERvA Pions

- MINERvA cuts flux from 1.5 – 10 GeV
→ Generator Dependence
- MINERvA cuts invariant mass $W > 1.4$ GeV
→ Generator Dependence

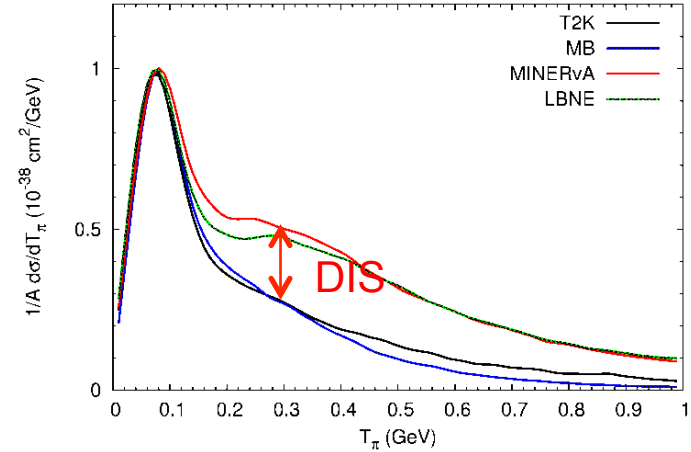
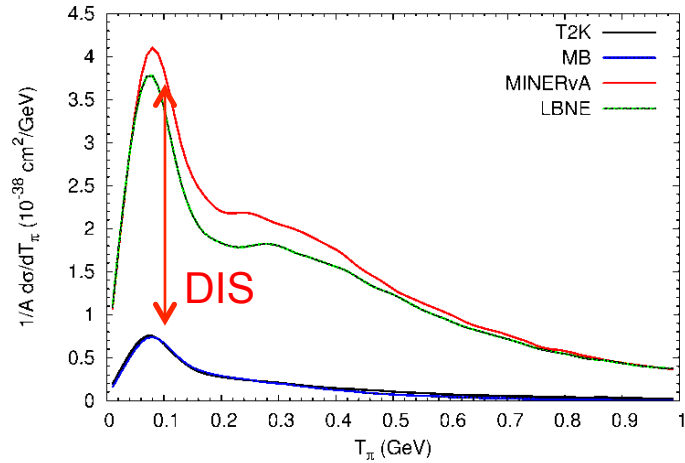


Effects of cuts



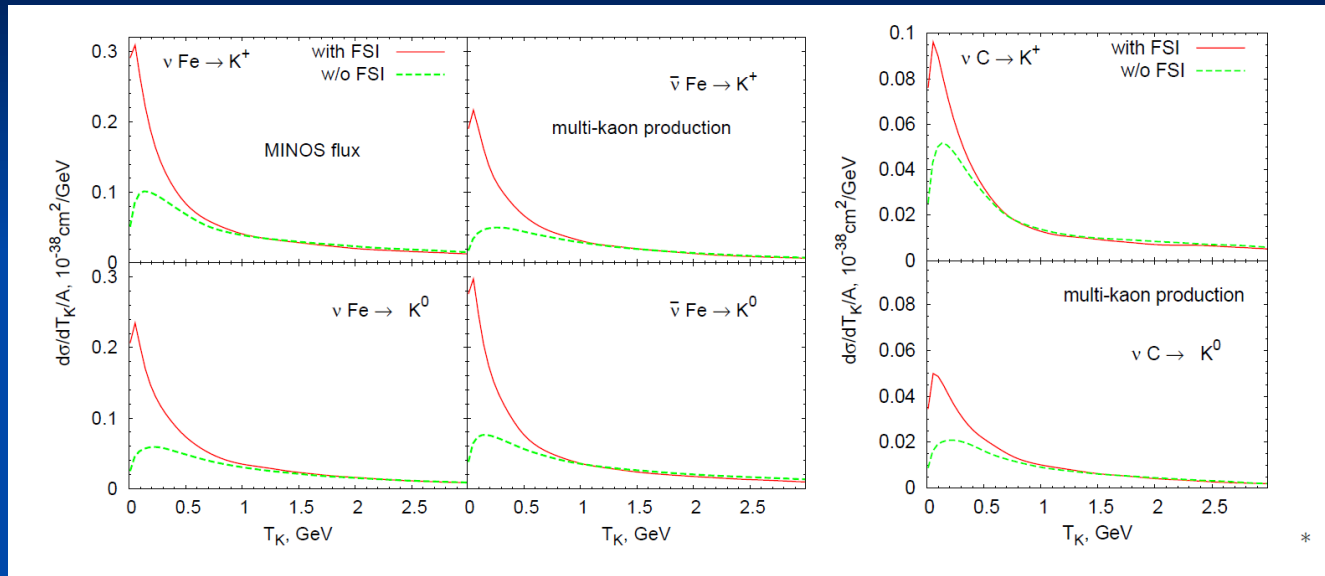
W distribution for Δ is significantly broadened due to Fermi-motion,
 Cut at 1.4 GeV cuts away 25% of total strength
 Note: $W^2 = M^2 + 2 M \nu - Q^2$.ne. $(p + q)^2$

Pions at various experiments



Multi π^+ , target: C for MB, T2K and MINERvA, Ar for LBNE

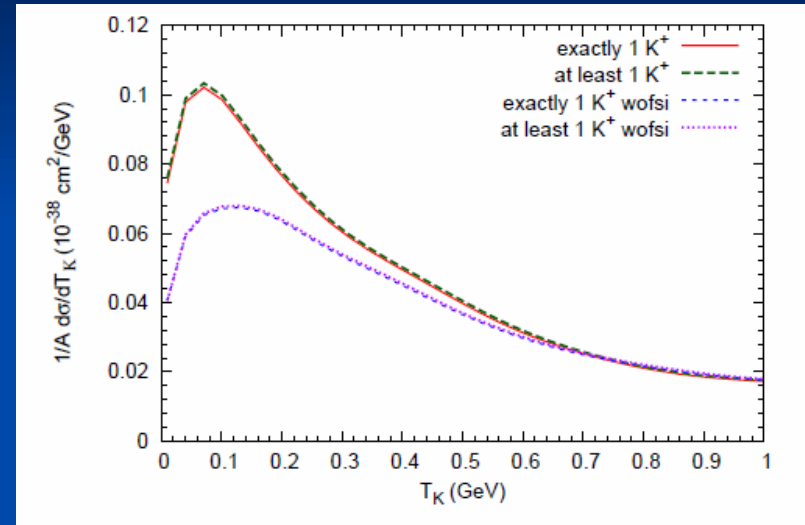
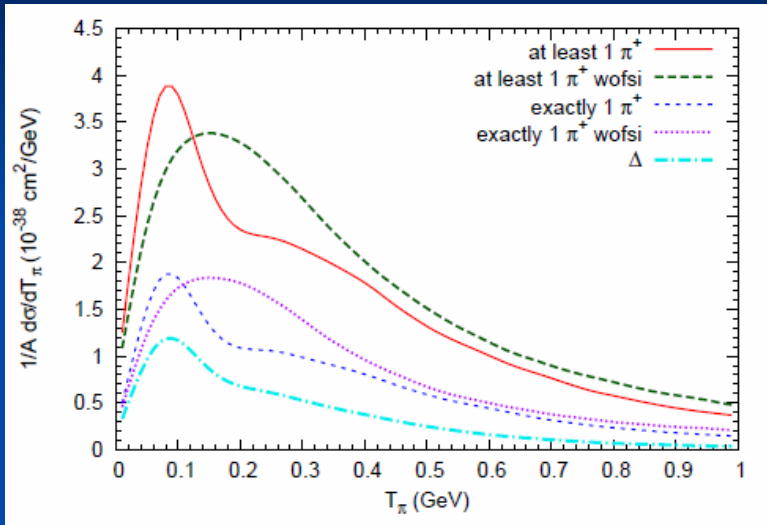
Kaons at MINOS and NOvA



Lalakulich et al,
PR D86, 014607
(2012)

FSI increase the cross section!
Semi-inclusive X-sections much larger than exclusive ones
(1 order of magnitude, cf. Athar, Alvarez-Ruso)

MINERvA



Fsi are most important, but different, for pions and kaons
Elementary kaon vertices 'shielded' by secondary production:
 $\pi + N \rightarrow K + \Lambda$

Coherent Pion Production

- ***Coherent pion production:***
not really part of a MC generator, since coherent process.

Nakamura, Sato and Lee (PRC81 (2010) 035502) have given (nearly) correct theory. Supersedes oversimplified earlier models, but nowhere used. **WHY???**

Conclusions

- Elementary pion data still uncertain, MiniBooNE and MINERvA data show tension
- Kaons at higher energies are dominantly produced in DIS events, together with pions. Secondary kaon production large → elementary kaon production difficult in MINERvA
- A plea to the experimentalists: show data with as little model (generator) dependence as possible. Flux cuts and W cuts introduce generator dependence into data.



Importance of Generators

- A good generator does not have to fit the data, provided it is right (meaning: theoretically correct and consistent)
- A good generator does not have to be right, provided it fits the data
- Let us strive for the right generator that is as much state-of-the-art as the experimental equipment!

