Worksheet 9

There is a quiz of basic understanding for lectures 8 and 9 on Keats.

1) [\star] What would you use as the boundary conditions to price a digital call option? Use the implicit scheme for the heat equation to price a digital call option.

(Solution: see the file priceDigitalCallByHeatEquationImplicit.m in lecture9.zip)

2) [\star] Implement the Crank-Nicolson scheme for the heat equation and use it to price a call option.

(Solution: see the file priceCallByHeatEquationCrankNicolson.min lecture9.zip)

3) [*] Plot a graph of the convergence of the Crank-Nicolson scheme against δt keeping λ fixed.

(Solution: see the file plotConvergence.m in lecture9.zip)

4) Implement the Jacobi method and test that you can use it to solve an equation of the form Ax = b with A a positive definite, symmetric, tridiagonal matrix.

- 5) Repeat the previous exercise with the Gauss-Seidel method
- 6) Repeat the previous exercise with Successive Over Relaxation (SOR) (Solution: see the file solveBySOR.m in lecture9.zip)

7) $[\star]$ What methods have we covered to price derivatives in this course? Draw a table showing which methods you can apply to each of the following types of derivative:

- European call option
- European digital call option
- Asian option
- Knockout option

• American put option