

## Element Uniqueness: a special case

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**Problem** Given a read-only array containing  $n$  integers from the set  $\{1, 2, \dots, n\}$ , determine whether it is a permutation of  $(1, 2, \dots, n)$ , that is, whether there are any duplicate elements. Design an efficient algorithm which uses only  $O(\log n)$  bits as its work space.

An  $O(n \log n)$ -time algorithm [1] is known. It uses  $O(\log n)$  work space (more exactly, work space of  $O(\log^2 n)$  bits). It is not known whether there is an algorithm which runs in  $O(n \log n)$  time using only  $O(\log n)$  bits.

### References

- [1] F. E. Fich and J. I. Munro and P. V. Poblete, “Permuting In Place,” *SIAM Journal on Computing*, 24, pp.266-278, 1995.